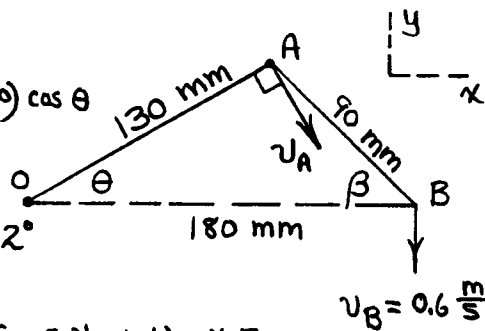


5/65

$$90^2 = 180^2 + 130^2 - 2(180)(130)\cos\theta$$

$$\theta = 28.3^\circ$$

$$\frac{130}{\sin\beta} = \frac{90}{\sin 28.3^\circ}, \beta = 43.2^\circ$$



$$\underline{v}_A = \underline{v}_B + \underline{v}_{A/B} : \underline{\omega}_{OA} \times \underline{r}_{OA} = \underline{v}_B + \underline{\omega}_{AB} \times \underline{r}_{BA}$$

$$\omega_{OA} \underline{k} \times 0.130 (\cos 28.3^\circ \underline{i} + \sin 28.3^\circ \underline{j}) = -0.6 \underline{j} + \omega_{AB} \underline{k} \times 0.090 (-\cos 43.2^\circ \underline{i} + \sin 43.2^\circ \underline{j})$$

$$\underline{i} : -0.0617 \omega_{OA} = -0.0617 \omega_{AB}$$

$$\underline{j} : 0.1144 \omega_{OA} = -0.6 - 0.0656 \omega_{AB}$$

Solve simultaneously to obtain

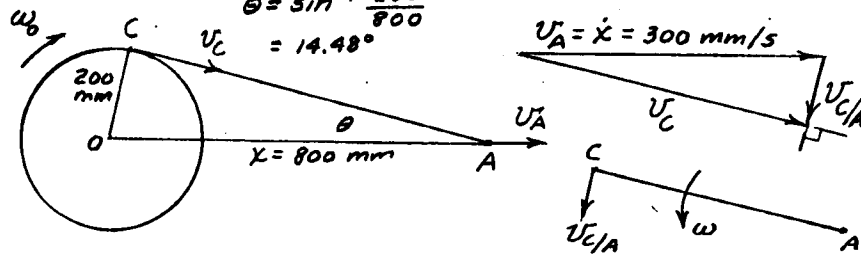
$$\omega_{AB} = \omega_{OA} = -3.33 \text{ rad/s}$$

$$\text{So } \underline{\omega}_{OA} = -3.33 \underline{k} \text{ rad/s}$$

5/72 $\vec{V}_C = \vec{V}_A + \vec{V}_{C/A}$, $V_A = 300 \text{ mm/s}$

$\theta = \sin^{-1} \frac{200}{800}$

$\theta = 14.48^\circ$



$V_C = 300 \cos 14.48^\circ$
 $= 300(0.9682) = 290 \text{ mm/s}$

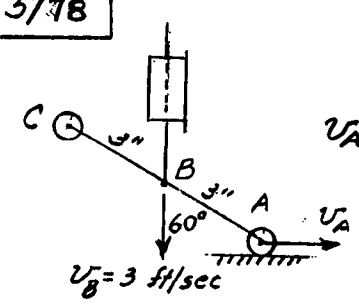
$V_{C/A} = 300 \sin 14.48^\circ = 300/4 = 75 \text{ mm/s}$

$\bar{CA} = 800 \cos 14.48^\circ = 775 \text{ mm}$

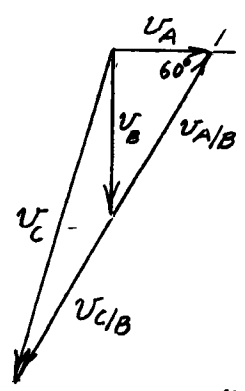
$\omega_{AB} = V_{C/A} / \bar{CA} = 75/775 = \underline{0.0968 \text{ rad/s CCW}}$

$\omega_0 = V_C / \bar{CO} = 290/200 = \underline{1.452 \text{ rad/s CW}}$

5/78



$$\begin{aligned} \underline{v}_A &= \underline{v}_B + \underline{v}_{A/B} \\ \underline{v}_C &= \underline{v}_B + \underline{v}_{C/B} \\ v_{A/B} &= \overline{AB}\omega \\ &= \overline{CB}\omega \\ &= v_{C/B} \end{aligned}$$



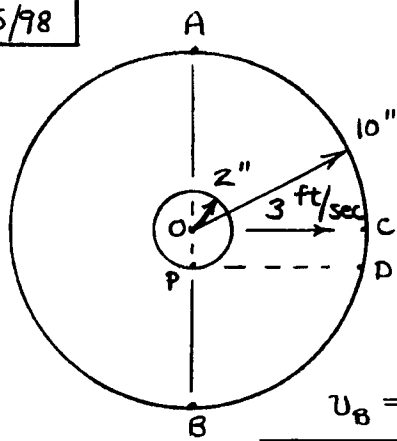
From geometry

$$v_{A/B} = 3 / \sin 60^\circ = 3.46 \text{ ft/sec}, \quad v_A = 3 / \tan 60^\circ = 1.732 \frac{\text{ft}}{\text{sec}}$$

$$v_{C/B} = 3.46 \text{ ft/sec}$$

$$v_C = \sqrt{(3+3)^2 + (1.732)^2} = \sqrt{39} = 6.24 \text{ ft/sec}$$

5/98



Point P is the instantaneous center

$$v_o = \overline{OP} \omega, \quad \omega = \frac{3}{2/12}$$

$$\omega = 18 \text{ rad/sec CW}$$

$$v_A = \overline{AP} \omega = \frac{12}{12} (18)$$

$$= 18 \text{ ft/sec } \rightarrow$$

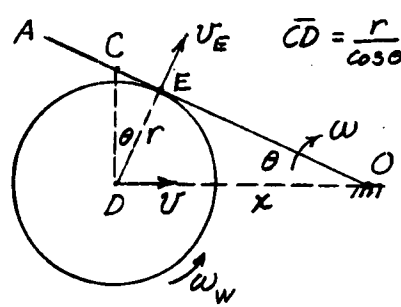
$$v_B = \overline{BP} \omega = \frac{8}{12} (18) = 12 \frac{\text{ft}}{\text{sec}} \leftarrow$$

$$v_c = \overline{CP} \omega = \sqrt{\left(\frac{2}{12}\right)^2 + \left(\frac{10}{12}\right)^2} (18) = 15.30 \text{ ft/sec}$$

$$\alpha = \tan^{-1} \frac{2}{12} = 9.46^\circ \downarrow$$

$$v_D = \overline{DP} \omega = \frac{10}{12} (18) = 15 \text{ ft/sec } \downarrow$$

5/110



$$\overline{CD} = \frac{r}{\cos\theta}, \quad \overline{CE} = r \tan\theta$$

C = instantaneous center of zero velocity for wheel

$$\omega_w = \frac{v_D}{\overline{CD}} = \frac{v}{r/\cos\theta}$$

$$= \frac{v \sqrt{x^2 - r^2}}{r x}$$

$$\omega = \omega_{AO} = \frac{v_E}{\overline{EO}} = \frac{1}{\overline{EO}} v \frac{\overline{CE}}{\overline{CD}}$$

$$\omega_w = \frac{v}{r} \sqrt{1 - (r/x)^2}$$

$$= \frac{1}{\sqrt{x^2 - r^2}} v \frac{r \tan\theta}{r/\cos\theta} = \frac{v}{\sqrt{x^2 - r^2}} \frac{r}{x}, \quad \omega = \frac{v}{x \sqrt{(x/r)^2 - 1}}$$

5/114 C is the instantaneous center of zero velocity for DBA

From geometry,

$$\overline{AC} = \frac{5}{3}(120) = 200 \text{ mm}$$

$$\overline{BC} = 160 \text{ mm}$$

$$\overline{DC} = \sqrt{60^2 + 160^2}$$

$$= 170.9 \text{ mm}$$

$$\delta = \sin^{-1} \frac{120}{200} = 36.9^\circ$$

$$\alpha = \tan^{-1} \frac{60}{160} = 20.6^\circ$$

$$\beta = 90 - 36.9 - 20.6 = 32.6^\circ$$

$$v_D = \frac{v}{\cos \beta} = \frac{0.2}{\cos 32.6^\circ} = 0.237 \text{ m/s}$$

$$\frac{v_D}{\overline{DC}} = \frac{v_A}{\overline{AC}} ; v_A = \frac{200}{170.9} (0.237) = \underline{0.278 \text{ m/s}}$$

