

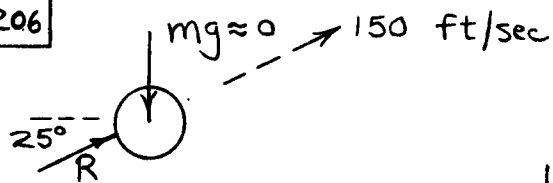
3/182 | No difference between cases (a) & (b).

$$G_1 = G_2: mv = (3m)v', \quad v' = \frac{v}{3}$$

$$T = \frac{1}{2}mv^2, \quad T' = \frac{1}{2}(3m)\left(\frac{v}{3}\right)^2 = \frac{1}{6}mv^2$$

$$n = \frac{T-T'}{T} = \frac{\frac{1}{2}mv^2 - \frac{1}{6}mv^2}{\frac{1}{2}mv^2} = \underline{\underline{\frac{2}{3}}}$$

3/206



$$\rightarrow R \Delta t = mv : R(0.001) = \frac{1.62/16}{32.2} (150)$$

$$R = 472 \text{ lb}$$

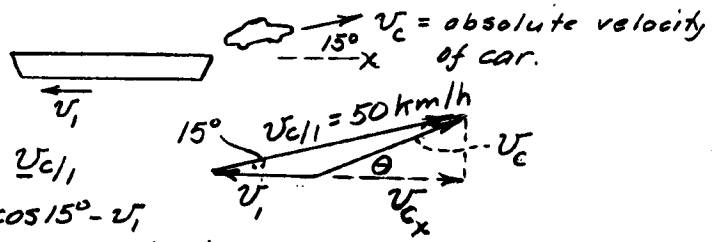
$$\rightarrow R = ma : 472 = \frac{1.62/16}{32.2} a$$

$$a = 150,000 \text{ ft/sec}^2 \text{ (4660g)}$$

$$v^2 - v_0^2 = 2ad : 150^2 - 0^2 = 2(150,000) d$$

$$d = 0.075 \text{ ft or } 0.900 \text{ in.}$$

3/218



$$\underline{v}_c = \underline{v}_1 + \underline{v}_{c1}$$

$$v_{c,x} = 50 \cos 15^\circ - v_1$$

$$= 48.296 - v_1 \text{ km/h}$$

$$\Delta G_x = 0; \quad 500 \times 10^3 v_1 = 1500(48.296 - v_1), \quad v_1 = 0.144 \frac{\text{km}}{\text{h}}$$

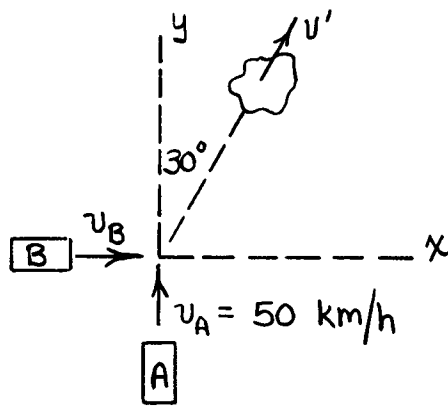
$$v_{c,x} = 48.152 \text{ km/h} \quad \text{or } v_1 = 40.1 \frac{\text{mm}}{\text{s}}$$

$$\Delta G_x = 0 \quad \underline{v}_2 \quad 1500(48.152) = 501500 v_2$$

$$v_2 = 0.144 \text{ km/h}$$

$$\text{or } \underline{v}_2 = 40.0 \text{ mm/s}$$

3/260



$$G_{1x} = G_{2x}: m_B v_B + 0 = (m_A + m_B) v' \sin 30^\circ$$
$$1600 v_B = 2800 v' \left(\frac{1}{2}\right) \quad (1)$$

$$G_{1y} = G_{2y}: m_A v_A + 0 = (m_A + m_B) v' \cos 30^\circ$$
$$1200 (50) = 2800 v' (0.866) \quad (2)$$

$$\text{From (2): } v' = 24.7 \text{ km/h}$$

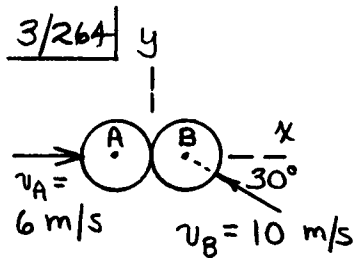
$$\text{From (1): } \underline{v_B = 21.7 \text{ km/h}}$$

3/261 Let v_s and v_b stand for rebound velocities from steel and brass plates.

$$\text{Impact speed} = \sqrt{2gh} = \sqrt{2(9.81)(0.15)} = 1.716 \text{ m/s}$$

$$\left. \begin{array}{l} 0.6 = \frac{v_s}{1.716}, v_s = 1.029 \text{ m/s} \\ 0.4 = \frac{v_b}{1.716}, v_b = 0.686 \text{ m/s} \end{array} \right\} \omega = \frac{1.029 - 0.686}{0.60} = 0.572 \text{ rad/s}$$

C CW



$$v_{Ay}' = v_{Ay} = 0$$

$$v_{By}' = v_{By} = 10 \sin 30^\circ = 5 \text{ m/s}$$

$$m_A v_{Ax} + m_B v_{Bx} = m_A v_{Ax}' + m_B v_{Bx}' \quad (1)$$

$$6 - 10 \cos 30^\circ = v_{Ax}' + v_{Bx}'$$

$$e = \frac{v_{Bx}' - v_{Ax}'}{v_{Ax} - v_{Bx}} : 0.75 = \frac{v_{Bx}' - v_{Ax}'}{6 - (-10 \cos 30^\circ)} \quad (2)$$

Solve Eqs. (1) & (2) :

$$\begin{cases} v_{Ax}' = -6.83 \text{ m/s} \\ v_{Bx}' = 4.17 \text{ m/s} \end{cases}$$

Magnitudes and directions θ - x

$$v_A' = 6.83 \frac{\text{m}}{\text{s}} @ \theta_A = 180^\circ$$

$$v_B' = 6.51 \frac{\text{m}}{\text{s}} @ \theta_B = 50.2^\circ$$

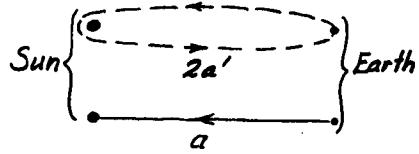
Initial: $T_1 = \frac{1}{2} m (6^2 + 10^2) = 68 \text{ m}$

Final: $T_2 = \frac{1}{2} m (6.83^2 + 6.51^2) = 44.5 \text{ m}$

$$n = \frac{68 - 44.5}{68} (100\%) = \underline{34.6\%}$$

3/282

Radius of actual orbit around the sun is a , which is the major axis $2a'$ of the degenerate ellipse.



R = radius of sun

g = gravitational accel. on surface of sun

Orbital period Eq. 3/40

$$\text{For actual orbit } \tau = 2\pi \frac{a^{3/2}}{R\sqrt{g}}$$

$$\text{For degenerate ellipse } \tau' = 2\pi \frac{(a/2)^{3/2}}{R\sqrt{g}}$$

$$\text{so } \frac{\tau'}{\tau} = \frac{(\frac{1}{2})^{3/2}}{1}$$

$$\begin{aligned} \text{But time } t \text{ to fall is } t &= \frac{1}{2}\tau' = \frac{1}{2}\left(\frac{1}{2}\right)^{3/2}\tau = \frac{1}{4\sqrt{2}}365.26 \\ &= \underline{64.6 \text{ days}} \end{aligned}$$

3/283 | The apogee speed at C is

$$\begin{aligned}v_a &= R \sqrt{\frac{g}{a}} \sqrt{\frac{r_{\min}}{r_{\max}}} \\&= 6371 (10^3) \sqrt{\frac{9.825}{(2 \cdot 6371 + 240 + 320) 1000 / 2}} \sqrt{\frac{6371 + 240}{6371 + 320}} \\&= 7697 \text{ m/s}\end{aligned}$$

The circular orbit speed at $h = 320$ km is

$$v_{\text{circ}} = R \sqrt{\frac{g}{r_{\max}}} = 7720 \text{ m/s}$$

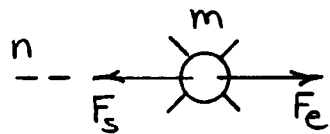
$$\Delta v = v_{\text{circ}} - v_a = 7720 - 7697 = 23.25 \text{ m/s}$$

$$F \Delta t = m \Delta v: 2(30000)(\Delta t) = 85000(23.25)$$

$$\underline{\Delta t = 32.9 \text{ s}}$$

The burn to increase speed is at C.

*3/300



F_s : force exerted on spacecraft by sun

F_e : force exerted on spacecraft by earth

$$\Sigma F_n = ma_n: F_s - F_e = m \frac{v^2}{r} = m r \omega^2 \\ = m (D-h) \left(\frac{2\pi}{T} \right)^2$$

where D is the earth-sun distance and T is the earth orbital period.

$$\frac{G m_s m}{(D-h)^2} - \frac{G m_e m}{h^2} = m (D-h) \left(\frac{2\pi}{T} \right)^2$$

With $G = 3.439 (10^{-8}) \frac{\text{ft}^4}{\text{lb-sec}^2}$, $m_s = 333,000 m_e$,
 $m_e = 4.095 (10^{23})$ slugs, $D = 92.96 (10^6) (5280)$ ft,
and $T = 365.26 (24) (3600)$ sec, solve numerically
for h as $h = 4.87 (10^9)$ ft or 922,000 mi