

# **Chapters 17**

# **Composites**

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# Composite

## Definition

Material made by purposefully combining two or more distinct materials, to offer combined property better than a single material

## Examples:

Low density and high modulus & strength composites

Carbon fiber reinforced polymer composite

Glass fiber reinforced polymer composite

### Tennis racket



<https://www.sourcifychina.com/tennis-racket-custom/>

### Wind turbine blades



<https://www.windssystemsmag.com/fundamentals-of-wind-turbines/>

# Composite Structure & Classification

## Two (or more) parts in general

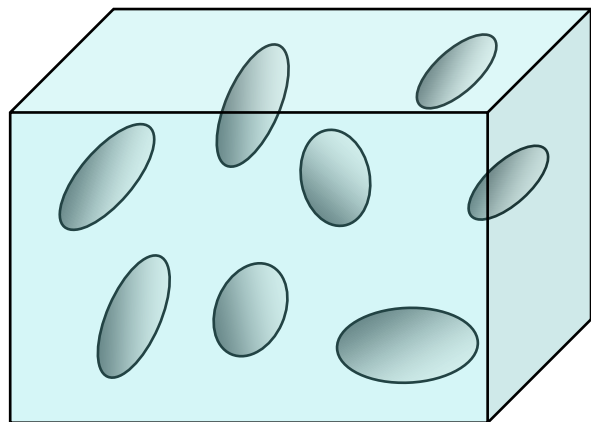
### Matrix – continuous phase

- Contain the dispersed phase and, in some cases, protect it
- Transfer the load (e.g., stress) to the dispersed phase
- **MMC**/metal matrix composite, **CMC**/ceramics matrix composite, **PMC**/polymer matrix composite

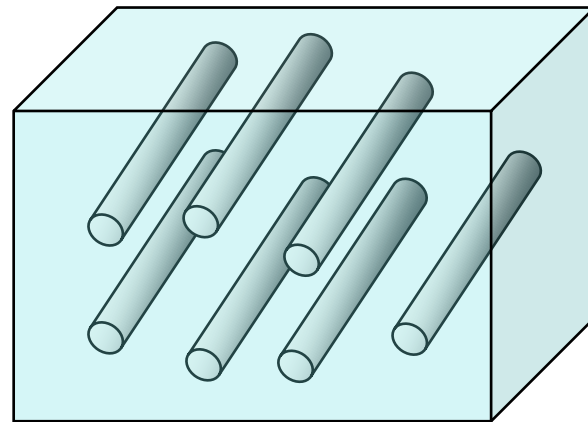
### Dispersed phase – phase(s) separated and surrounded by the matrix

- Strengthen the overall material by carrying the load/stress

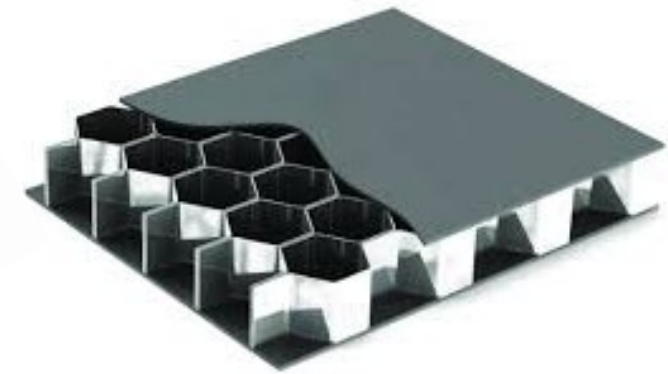
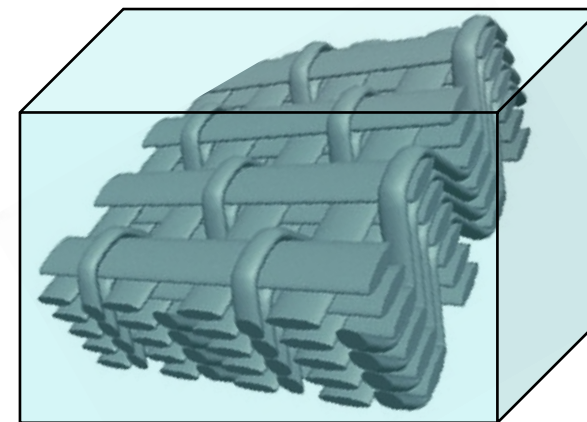
**Particulate** reinforced



**Fiber** reinforced



**Structural Composite**

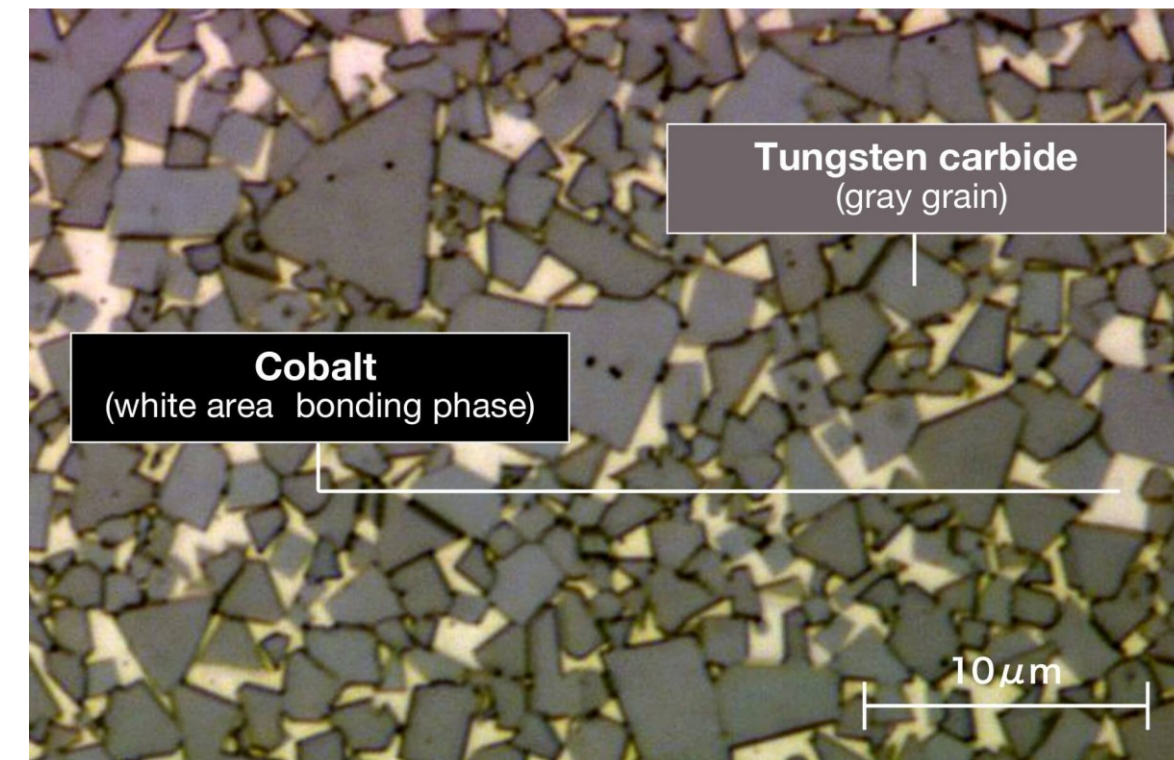


# Particulate Composites (1)

- For improved hardness, strength, and wear resistance, while preserving decent toughness
- Example WC-Co composite for cutting/machining

Material	E (GPa)	Hardness (HRc)	Flexural strength (MPa)	$K_{ic}$ (MPa $\cdot$ m <sup>0.5</sup> )
AISI4340 steel	203	46	1365	79-91
Ti-6Al-4V Ti alloy	113	41	950	45
IN 718 superalloy	211	36	1050	> 90
D2 tool steel	206	60	3200	33
Si <sub>3</sub> N <sub>4</sub> ceramics	304	70	850	3.5 – 6
<b>WC-10%Co cermet</b>	<b>552</b>	<b>72</b>	<b>3545</b>	<b>15</b>
<b>WC-6%Co cermet</b>	<b>641</b>	<b>77</b>	<b>3151</b>	<b>12</b>

## WC-Co cemented carbide cutting tool



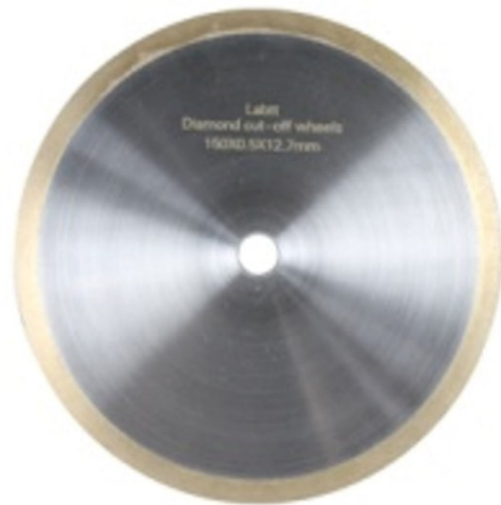
*Chandran, Nano and Structural Design of Advanced Materials (2003), p.157*

<https://www.betalentcarbide.com/products/carbide-cutting-tools/>

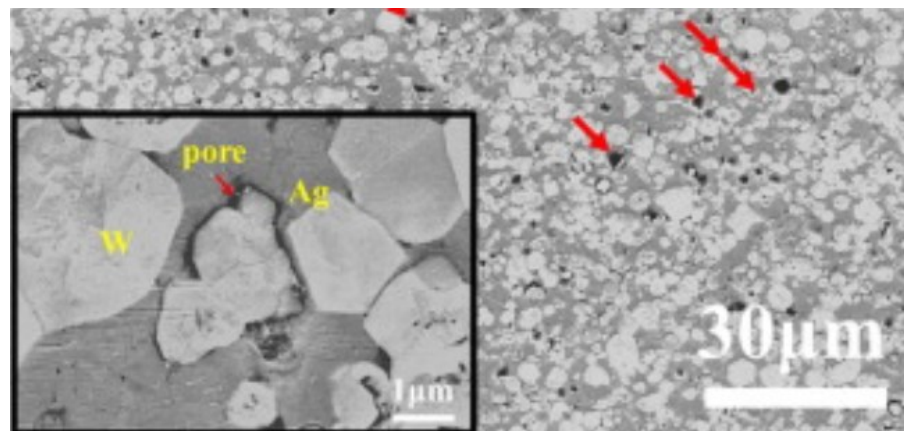
[https://www.nhm.co.jp/english/technical\\_info/whatis/](https://www.nhm.co.jp/english/technical_info/whatis/)

# Particulate Composites (2)

**Diamond cutting wheel**  
w/ diamond embedded in metal for high hardness of toughness



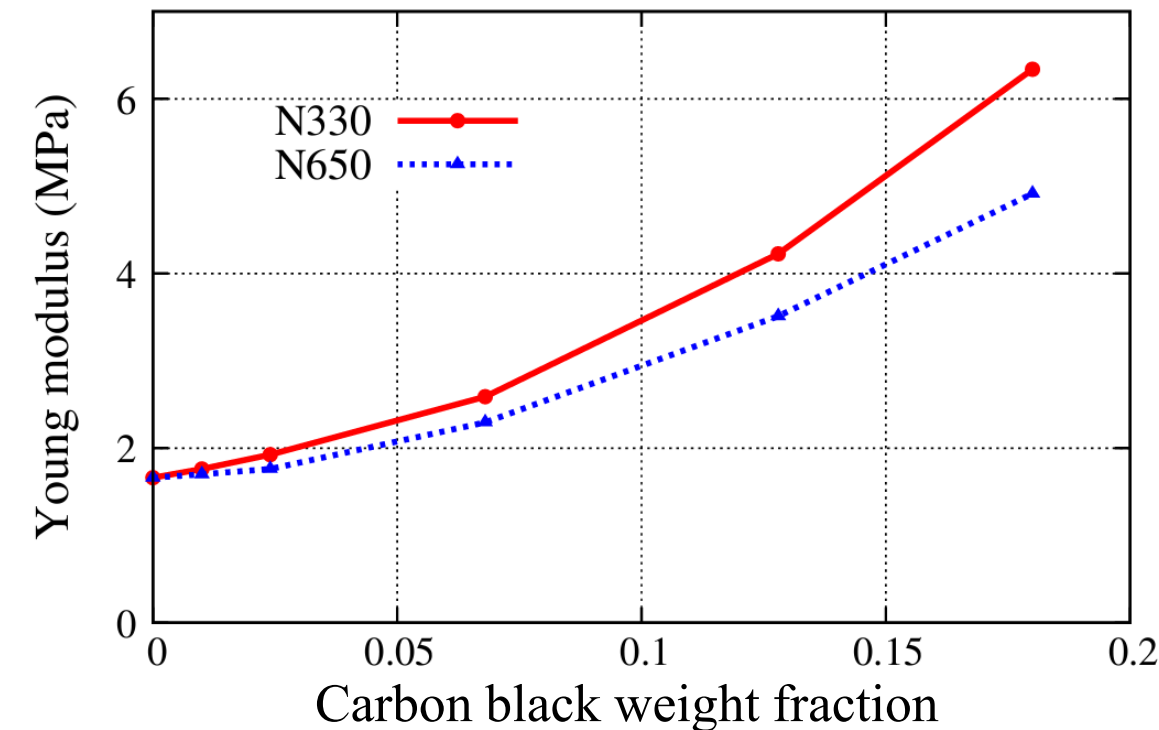
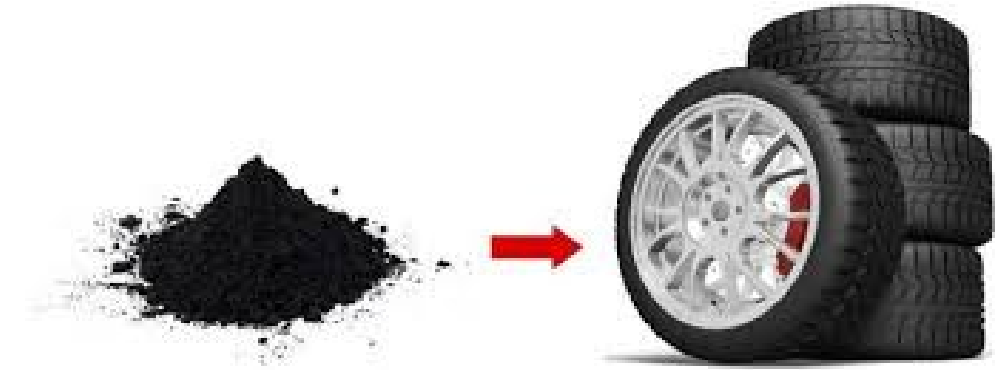
**W-Ag composite for electrical contact** w/ high wear resistance, while maintaining high electrical conductivity



<https://www.samaterials.com/tungsten-alloy-composites/138-tungsten-silver.html>

[Luo et al., Materials & Design, v219, p110733 \(2022\)](#)

**Carbon-black reinforced rubber**  
for higher elastic modulus & wear resistance

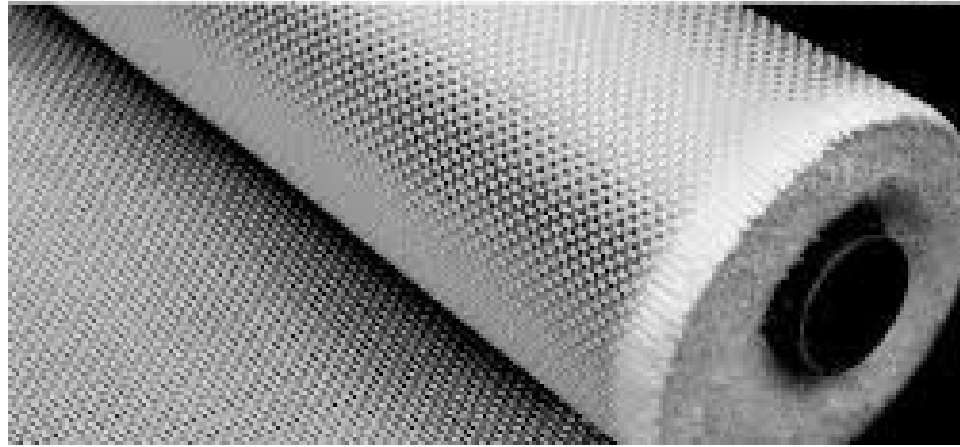
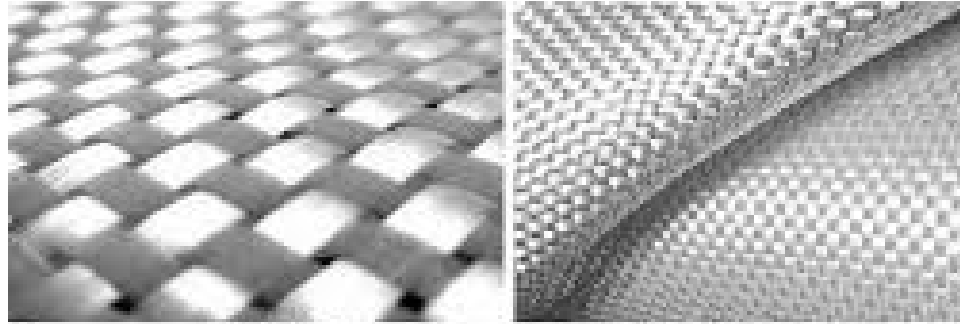


[Omnes, et al., Composites Part A: Applied Science and Manufacturing, v39 \(7\), p. 1141 \(2008\)](#)

<https://www.intechopen.com/chapters/44966>

# Fiber Reinforced Composites (1)

➤ For significantly improved strength and modulus, over the matrix



# Type of Fibers

## Whiskers (short fiber)

Single crystal w/ large  $L : d$  ratio (only  $\mu\text{m}$  to  $\text{mm}$  long)

- SiC,  $\text{Si}_3\text{N}_4$
- Extremely strong
- Costly, difficult to disperse



[https://www.hwnanomaterial.com/beta-sic-whiskers-for-strength-and-toughness-enhancement-of-plastic-metal-ceramic\\_p1102.html](https://www.hwnanomaterial.com/beta-sic-whiskers-for-strength-and-toughness-enhancement-of-plastic-metal-ceramic_p1102.html)

## Fibers (long)

Polycrystalline or amorphous w/ very large  $L : d$  ratio

- Polymers or ceramics (graphite, E-glass, boron, etc.)

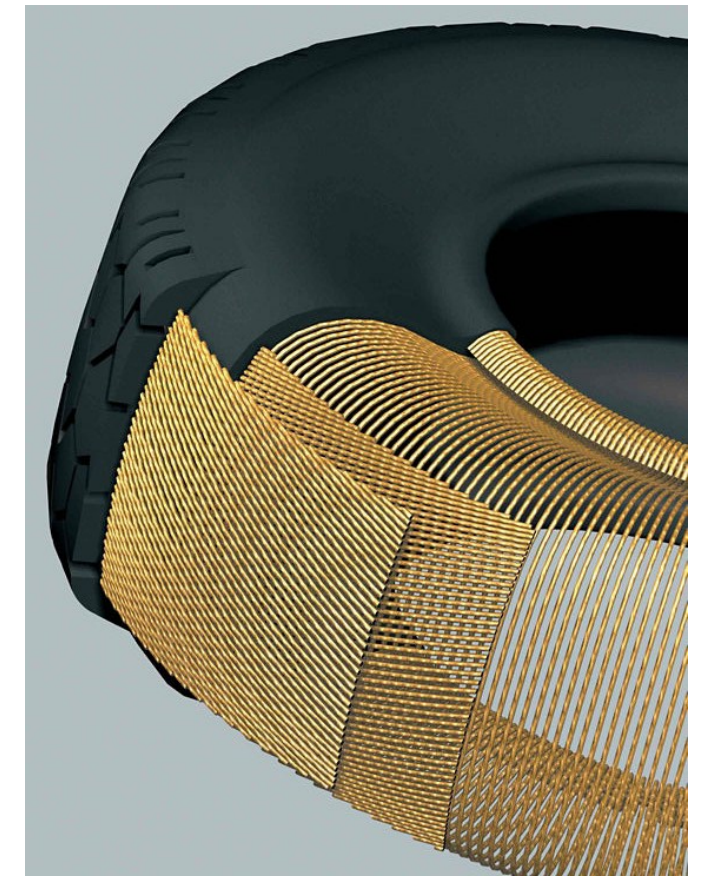


<https://www.fiberglassfiber.com/s-glass-fiber-high-strength-product/>  
<https://www.teijin.com/products/carbon-fiber/>

## Wires

Often metals (steel, Mo, W, etc.)

- Strong

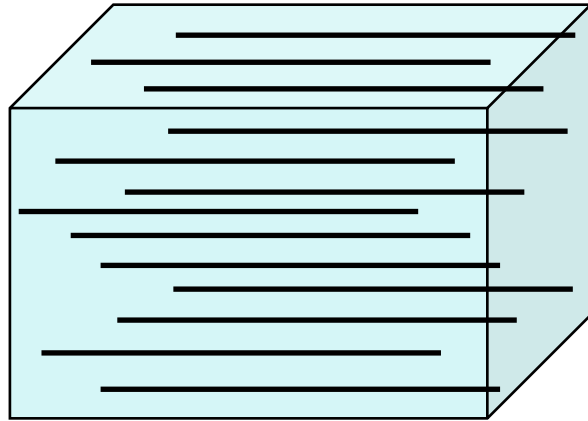


<https://www.bekaert.com/en/products/automotive/exterior/steel-cord-for-tire-reinforcement>

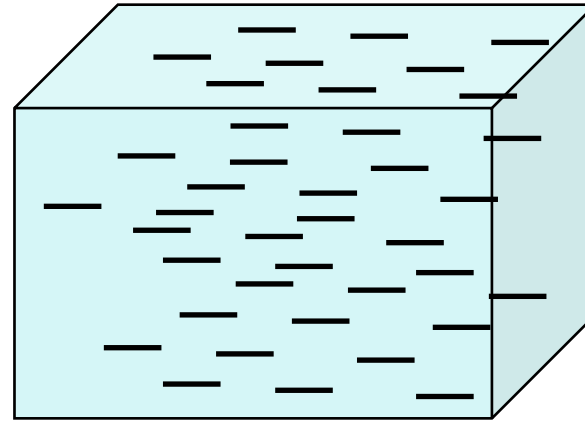
# Fiber Alignment Feature & Rule of Mixture (ROM)

- Effects of strengthening depends on fiber alignment

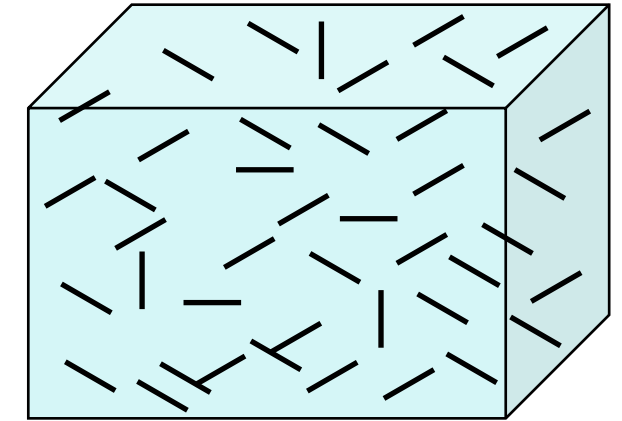
Aligned long fiber



Aligned short fiber



Random short fiber



- For aligned long-fiber reinforced composites,

Elastic modulus along fiber direction,  $E_{c, parallel}$ , follow rule-of-mixture (ROM)

$$E_{c, parallel} = V_m E_m + V_f E_f$$

$E_m$  Elastic modulus for matrix

$E_f$  Elastic modulus for fiber

$V_m$  Volume fraction for matrix

$V_f$  Volume fraction for fiber

Same for some other properties such as tensile strength, electrical conductivity, etc.

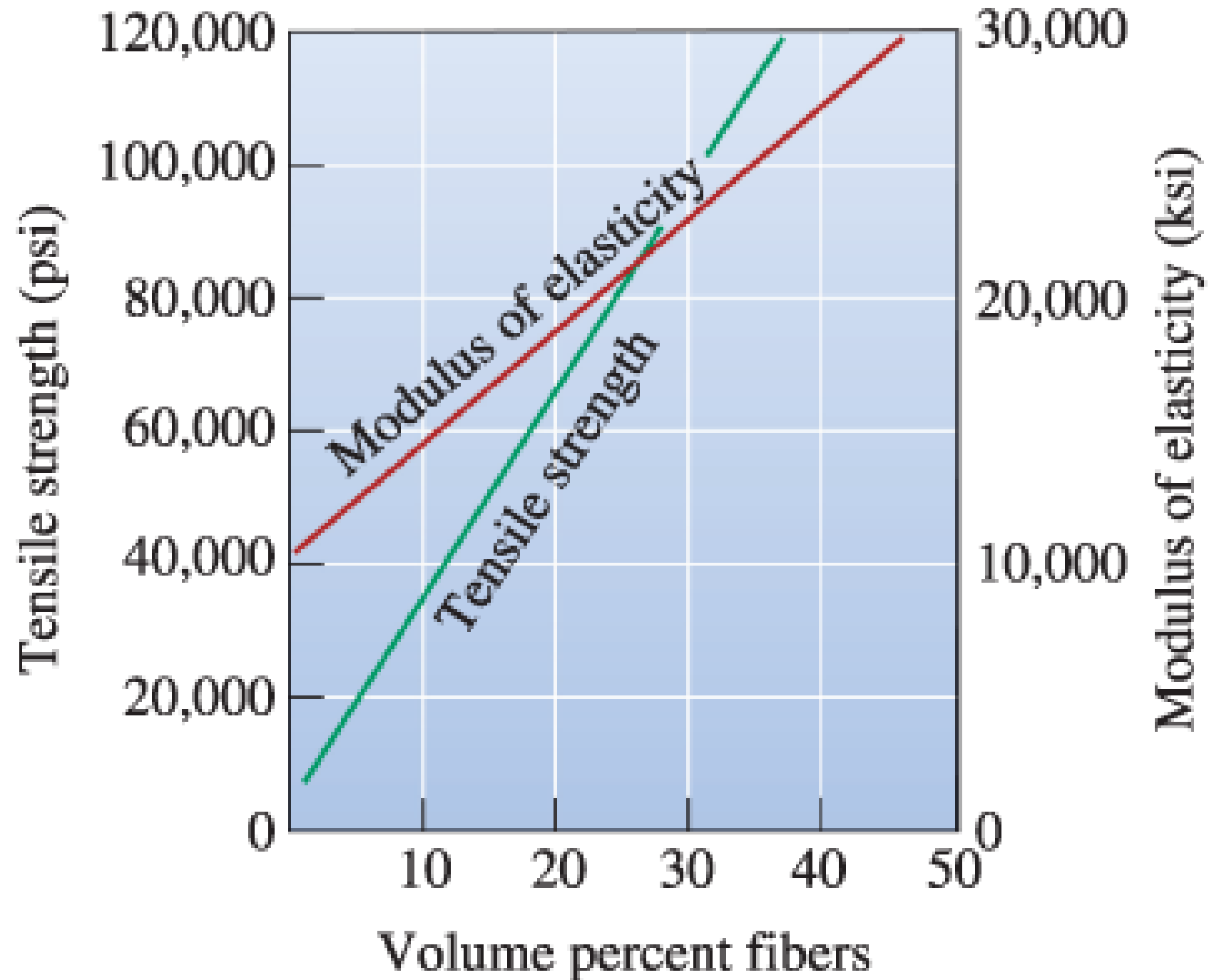
# Strengthening of $E$ and $\sigma$ for Fiber Reinforced Composites

- Linear increase in  $E$  and  $\sigma_U$  with increasing fiber (SiC in this case) volume content

$$E_{c,parallel} = V_m E_m + V_f E_f$$

$$\sigma_{U_c,parallel} = V_m \sigma_{U_m} + V_f \sigma_{U_f}$$

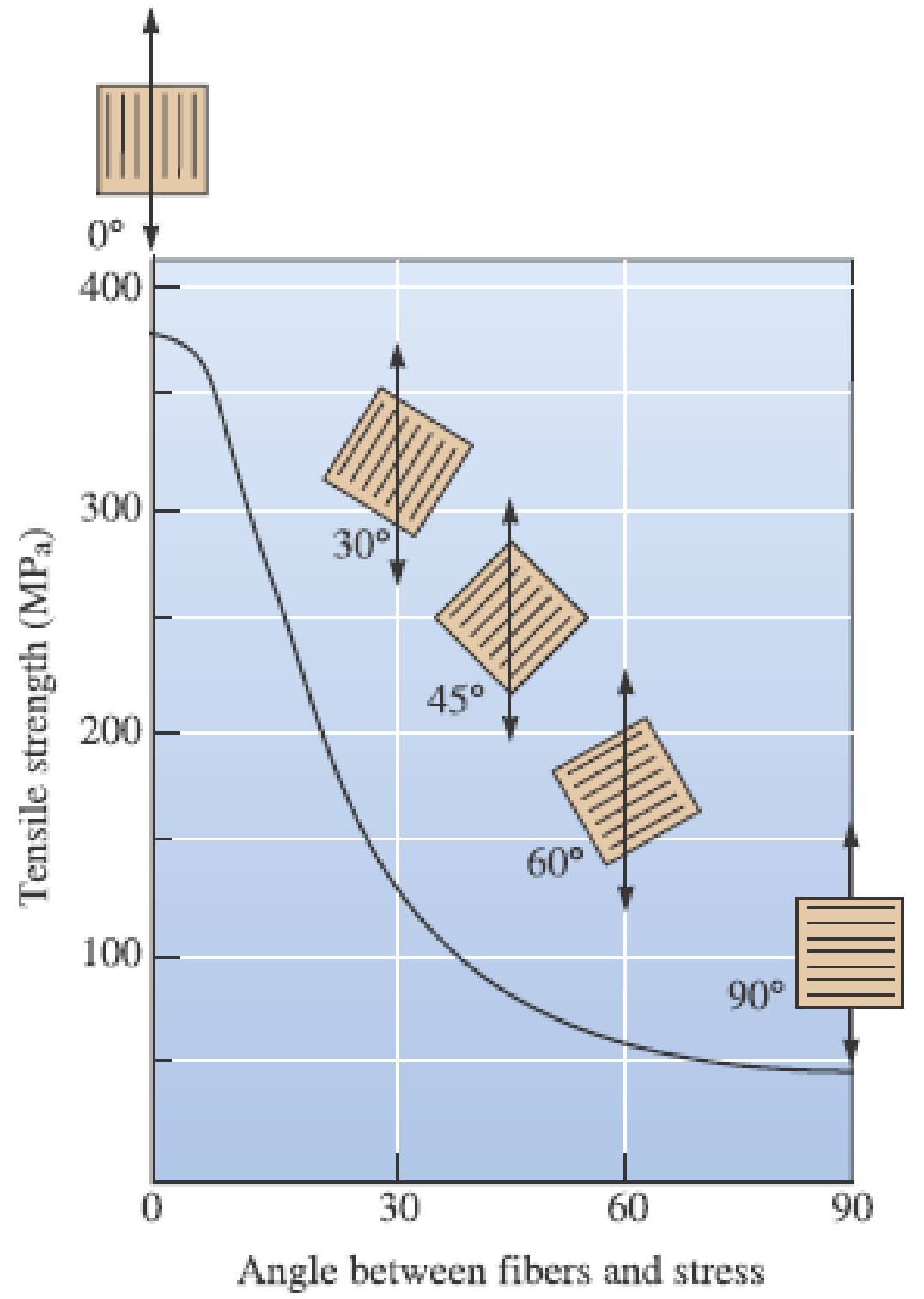
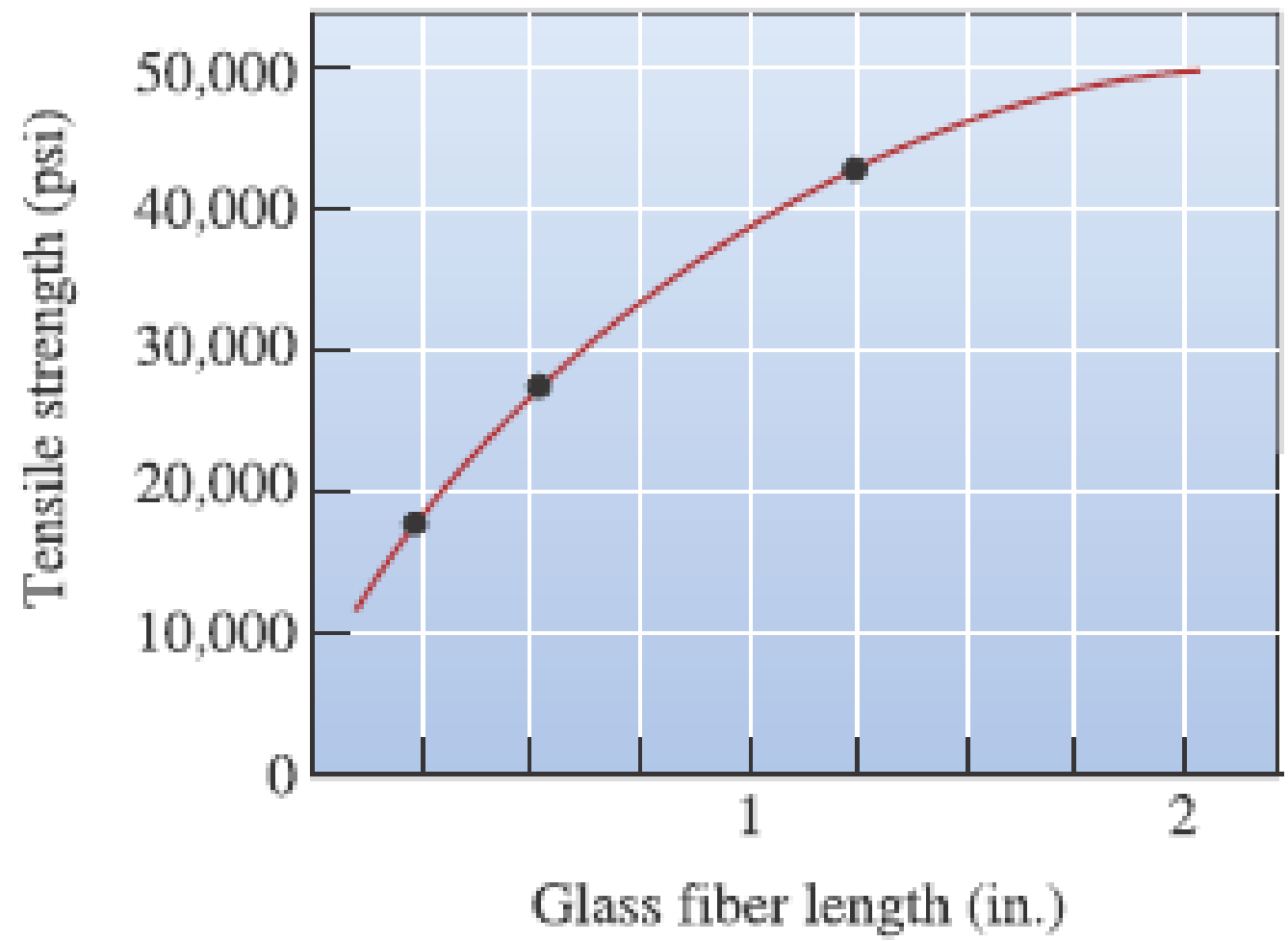
SiC fiber reinforced Al composite



# Length & Orientation for Fibers in Composite

➤ Increasing fiber length makes strengthening effect more effective

## E-glass fiber reinforced epoxy



➤ Alignment of fiber with stress/load direction also impacts strengthening

# Common Models to Estimate Composites' Properties

For property  $P$ , if volume fraction for each phase is  $V_1$  and  $V_2$ , with  $V_1 + V_2 = 1$

**Upper limit** (often thought of “parallel”):  $P_{comp} = V_1 P_1 + V_2 P_2$

- Density;
- Elastic modulus & tensile strength (assuming same strain);
- Electrical & thermal conductivity (assuming same electrical field or temperature gradient)

**Lower limit** (often thought of “in series”):  $\frac{1}{P_{comp}} = \frac{V_1}{P_1} + \frac{V_2}{P_2}$   $P_{comp} = \frac{1}{\frac{V_1}{P_1} + \frac{V_2}{P_2}}$

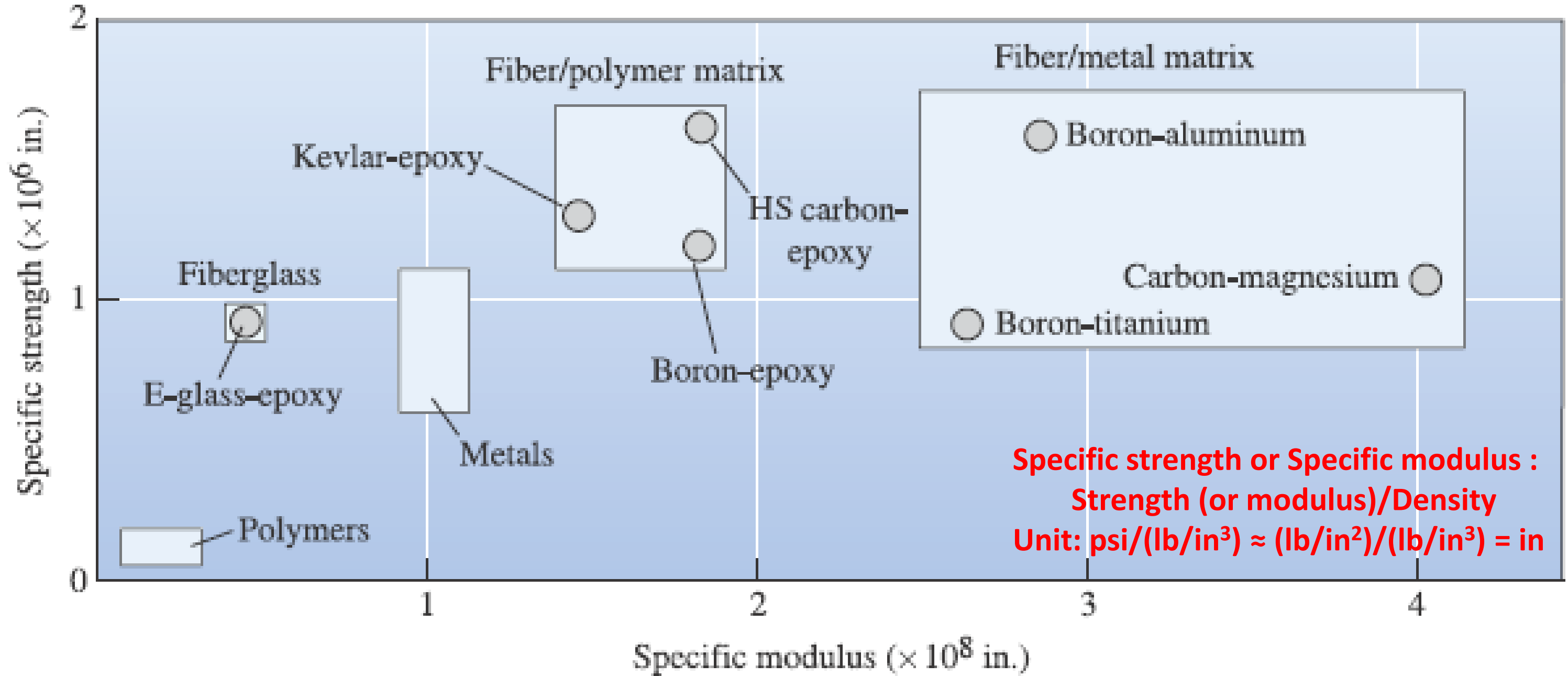
- Elastic modulus & tensile strength (assuming same stress);
- Electrical & thermal conductivity (assuming same current density or heat flux)

**Arithmetic mean**:  $P_{comp} = \frac{P_1 + P_2}{2}$

**Geometric mean**:  $P_{comp} = P_1^{V_1} \cdot P_2^{V_2}$

- Many other models
- Need experimental verification

# Advantages of Composites



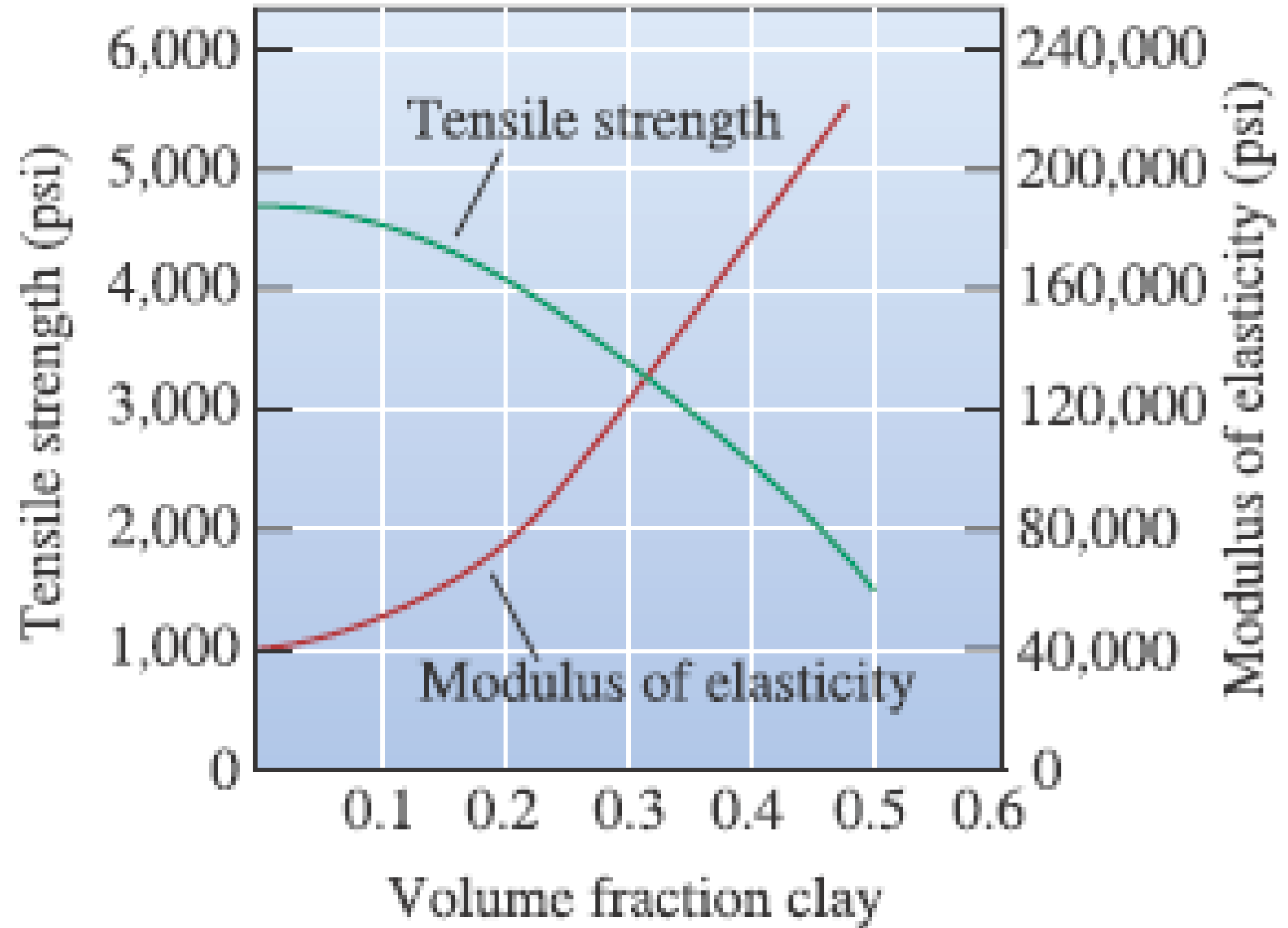
➤ (Often) drastically improved strength, modulus, or hardness, while maintaining relatively low density

# Composites (Always) Lead to Some Compromises

## Example 1

Clay addition to polyethylene

- Modulus  $E$  increase
- But tensile strength decrease!



END

# Homework 0

Carefully review chapter 17 lecture slides and, if interested, read textbook sections of Askeland 17 and give an honor statement confirming the reading

# Homework 17.1

A fully dense tungsten-silver (W – Ag) composite is made from 70 wt.% W – 30 wt% Ag. Knowing density is

19.2 g/cm<sup>3</sup> for W, 10.5 g/cm<sup>3</sup> for Ag

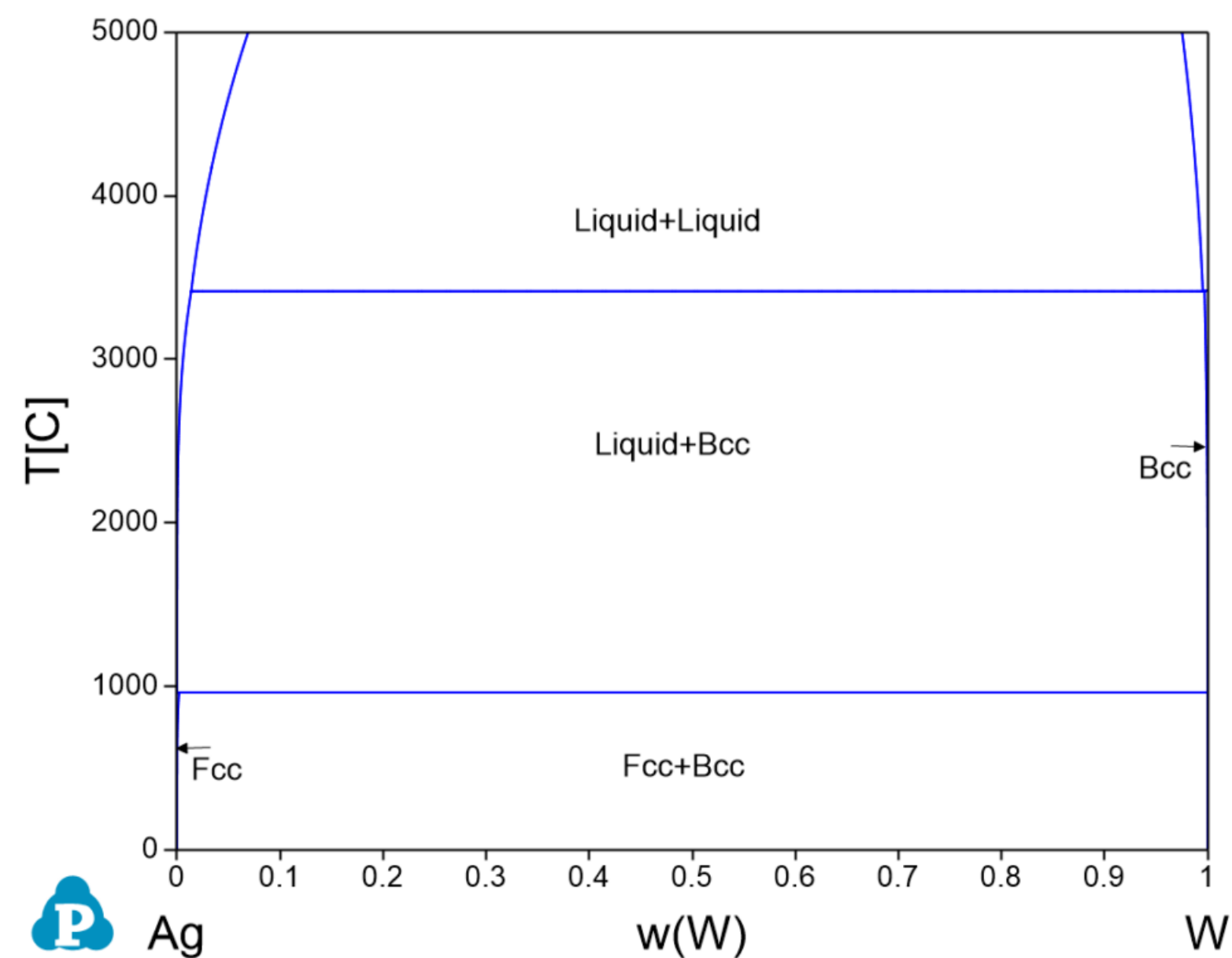
1) Based on W – Ag phase diagram, how many phases exist under equilibrium at 20°C? What is the volume fraction for each phase?

2) Calculate density of the composite

3) If the electrical conductivity  $\sigma$  for the 2-phase composite can be approximated by

$$\frac{1}{\sigma_{composite}} = \frac{V_1}{\sigma_1} + \frac{V_2}{\sigma_2}, \text{ please estimate the electrical conductivity for the composite}$$

if electrical conductivity is  $1.8 \times 10^7$  S/m for W and  $6.3 \times 10^7$  S/m for Ag



# Homework 17.2

For fully dense WC-10 wt% Co cemented carbide, knowing density, Young's modulus, and fracture toughness for each phase

	Density (g/cm <sup>3</sup> )	$E$ (GPa)	$K_{1C}$ (MPa·m <sup>0.5</sup> )
WC	15.6	700	~8
Co	8.9	209	~150

- 1) Calculate the volume fraction or  $V_i$  for each phase
- 2) Calculate density of the cemented carbide
- 3) If upper bound of the composite's Young's modulus is  $E_{composite} = V_1 E_1 + V_2 E_2$   
lower bound of the composite's Young's modulus is  $\frac{1}{E_{composite}} = \frac{V_1}{E_1} + \frac{V_2}{E_2}$   
Please give the range of the estimated Young's modulus of the cemented carbide.
- 4) Please estimate the fracture toughness of the WC-10 wt% Co using the geometric mean model, i.e.,  $K_{WC-10Co} = K_{WC}^{V_{WC}} \cdot K_{Co}^{V_{Co}}$

## Homework 17.3

A continuous and aligned long fiber-reinforced composite consisting of 60 vol.% of glass fiber with Young's modulus of 70 GPa and 40 vol% of polyester with Young's modulus of 3 GPa

- 1) Please estimate the modulus of elasticity of the composite along the fiber direction
- 2) Estimate the density of the composite, knowing glass fiber density of  $2.5 \text{ g/cm}^3$ , and epoxy density is  $1.25 \text{ g/cm}^3$
- 3) If an external tensile force of 10000 N is applied along the fiber direction, calculate the load carried by each of the fiber and matrix phase, if iso-strain condition is satisfied along that direction