

Chapter 7

Materials Mechanical Failures

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Mechanical Failure

Statics

Rigid body

No deformation

No failure

There are NO rigid bodies!

Mechanics of Solids
(or MECH331, CIVE360)

Practical engineering
materials

w/ deformation
(elastic/reversible or
plastic/irreversible)

Can (often) fail
(Fracture, Fatigue,
Creep)

A 1st Means of Mechanical Failure - Fracture

➤ Definition

A type of mechanical failure for materials, characterized by complete separation of a material into pieces and loss of mechanical integrity

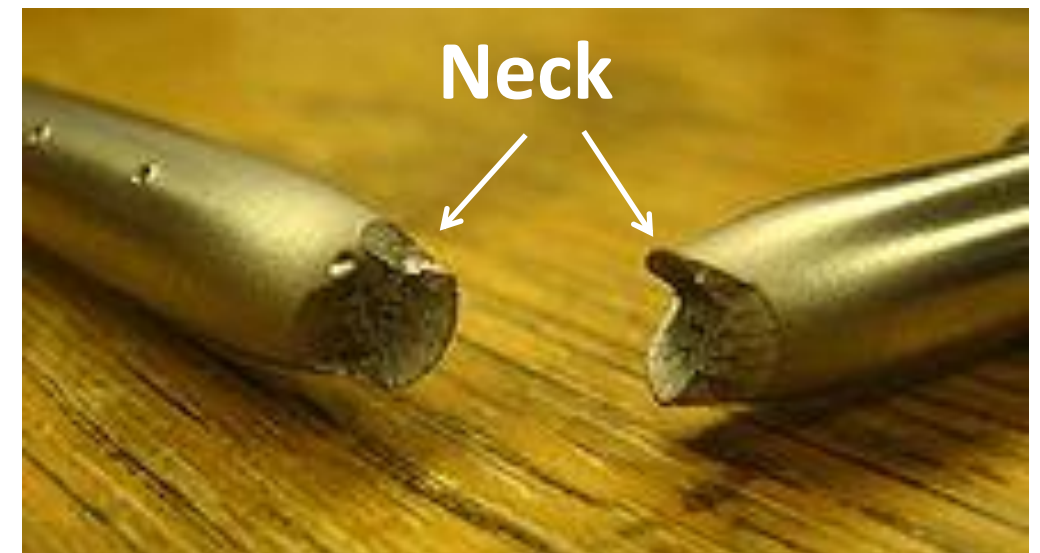
➤ Brittle fracture

- Little or no plastic deformation
- Often sudden & catastrophic
- Ceramics, glass, & some metals & polymers



➤ Ductile fracture

- Accompanied by significant plastic deformation
- More predictable
- Most metals & polymers, and, under special conditions (e.g., high T), ceramics/glass



Material's (Tensile) Fracture Strength << Theoretical Value

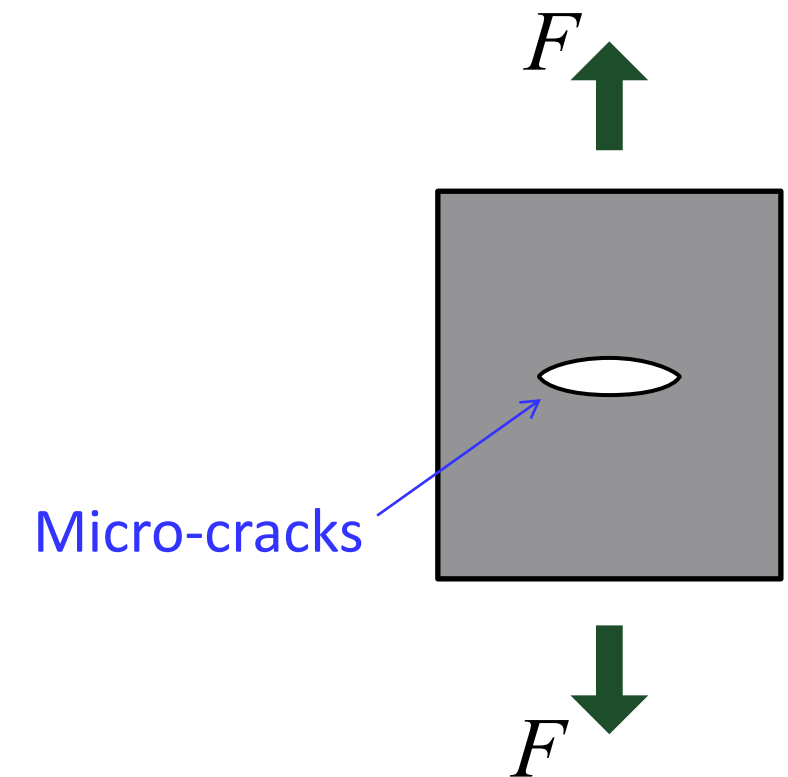
- Material ideal tensile strength, based on breaking all bonds simultaneously, is $\sim E/10$

Reference: https://en.wikipedia.org/wiki/Theoretical_strength_of_a_solid

- Practical materials' tensile strength much lower than ideal - by ~ 10 - 100 times!

Steel: $\sigma_{th} \sim 20$ GPa vs. $\sigma_U \sim 0.5$ - 2 GPa

- Much lower fracture strength for practical materials due to **flaws**, especially **microcracks**



Micro-cracks as Stress Concentrator

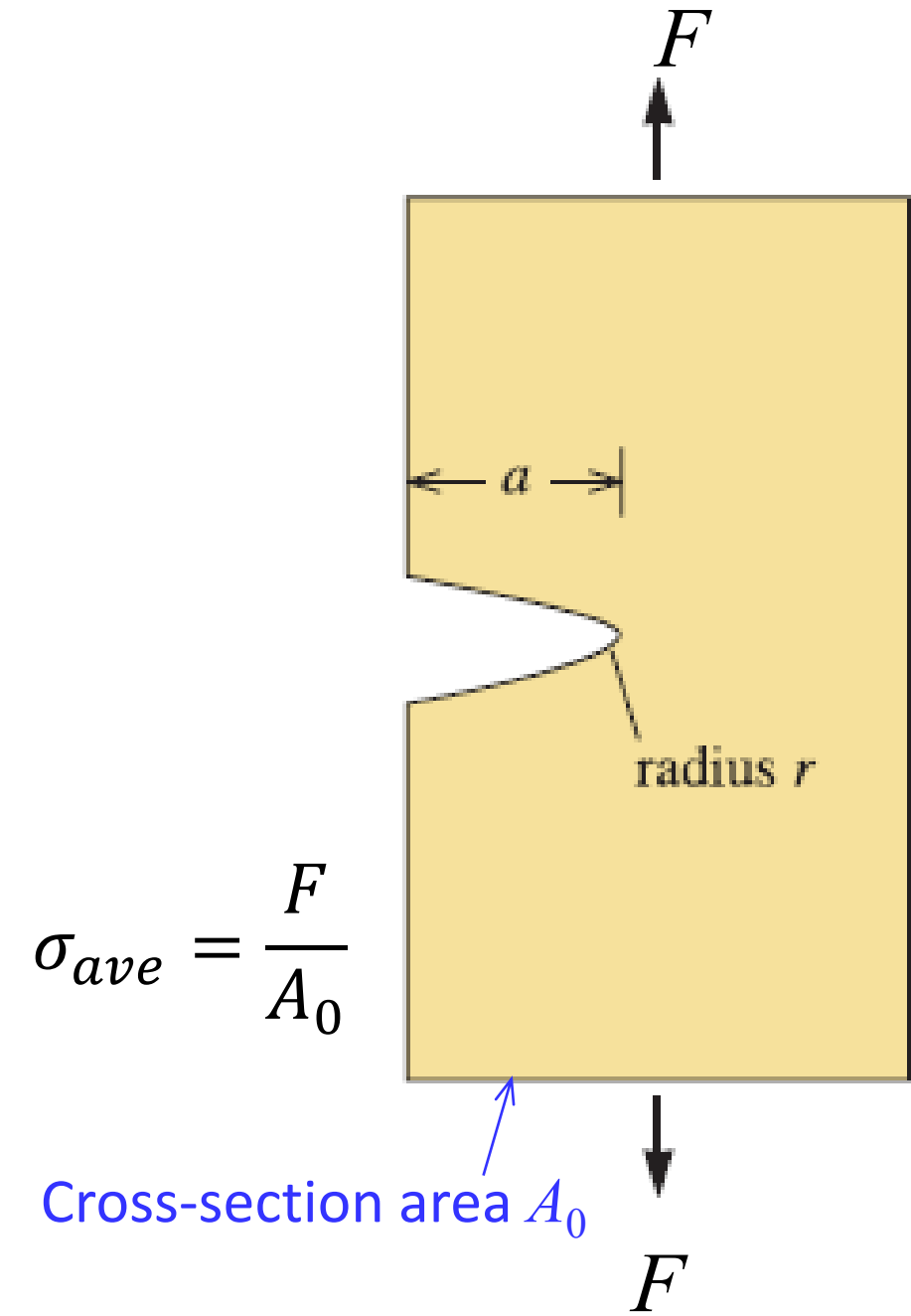
➤ Stress concentration:

Local (max) stress, at the **tip** of a flaw or microcrack, is much higher than average stress:

$$\sigma_{\max local} \approx 2\sigma_{ave} \sqrt{\frac{a}{r}} \gg \sigma_{ave}$$

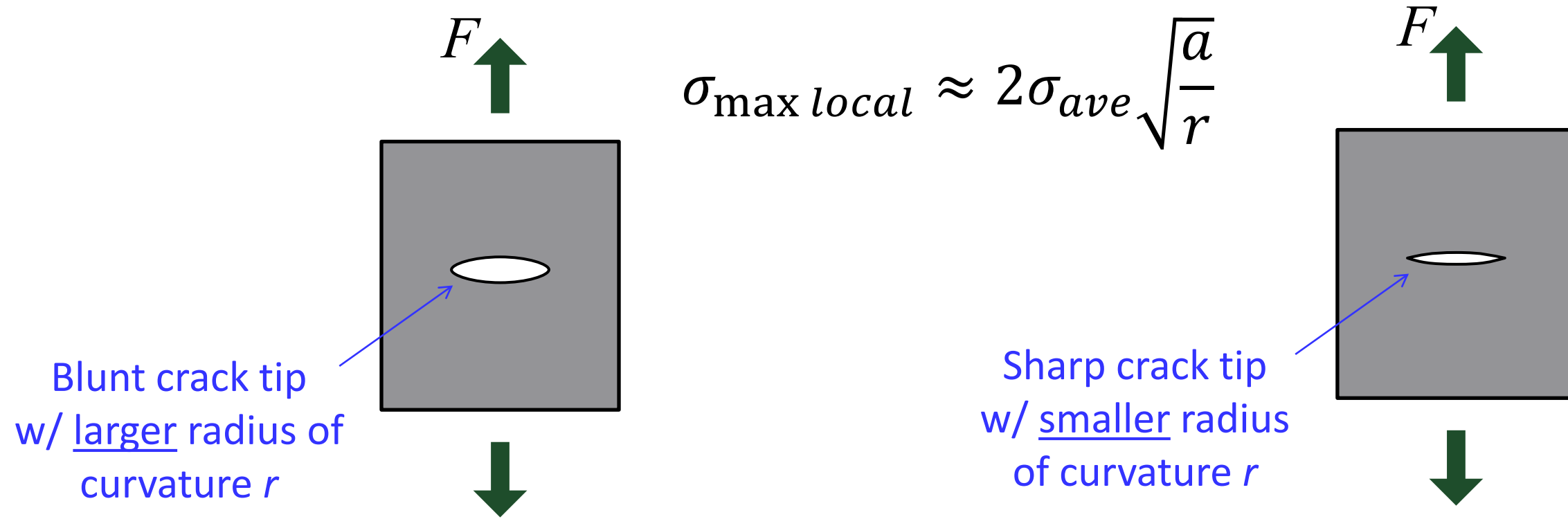
➤ Higher a/r ratio (i.e., longer crack or sharper tip) → greater crack-tip stress “concentration”

➤ When max local stress exceeds critical stress (i.e., when local bonds start to break significantly, e.g., $\sqrt{\frac{2E\gamma_s}{\pi a}}$ for brittle fracture), crack “propagate” or grow and materials fracture/fail



Crack Propagation/Growth

- Cracks w/ sharp tips grow faster than blunt tip



- Ductile material plastically deform at crack-tip, absorbing much more energy before crack can grow/propagate than brittle material



Brittle

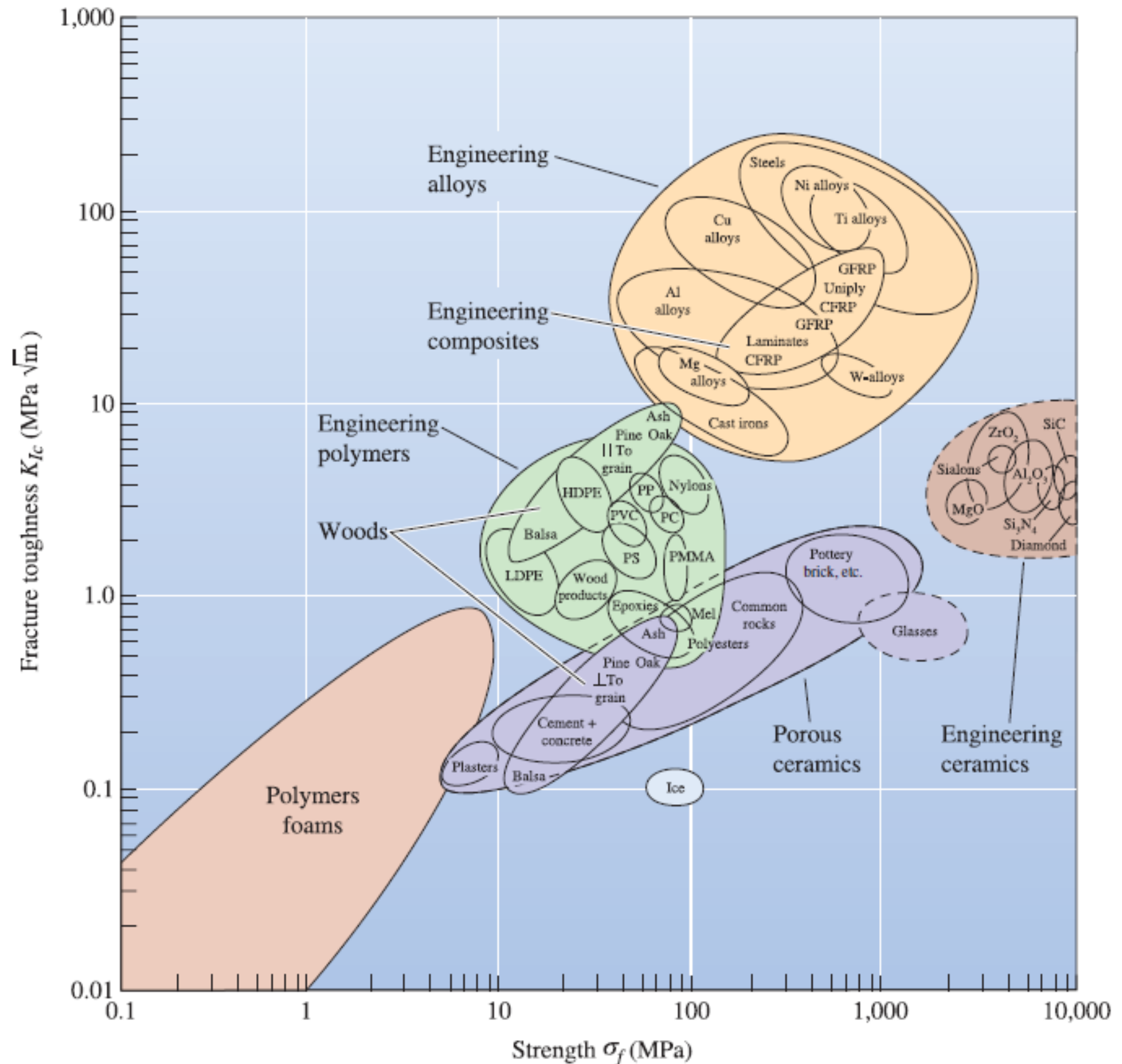


Ductile

(Plane Strain)

Fracture Toughness K_{1c}

- A parameter to represent a material's practical capability to resist fracture
- Unit **MPa • m^{0.5}**
- Often a range for a given material, due to difference in processing/flaws
- High for metals, especially **steel**
- Low for ceramics and common polymers

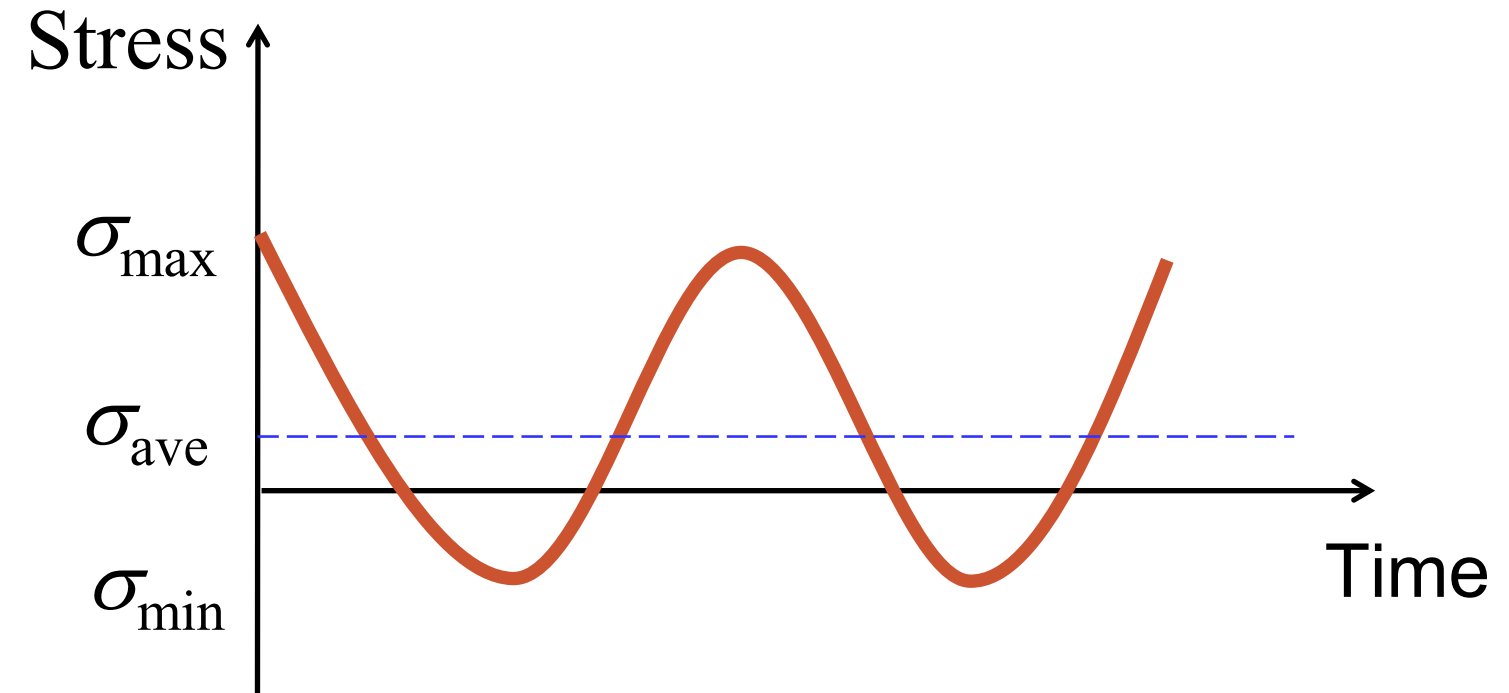


A 2nd Means of Mechanical Failure - Fatigue

Fatigue

Failure under repeated applied or cyclic stress (or load), **often below yield strength or tensile strength.**

- Lead to failure, even though $\sigma_{\max} \ll \sigma_y$
- ~ 90% of mechanical failures



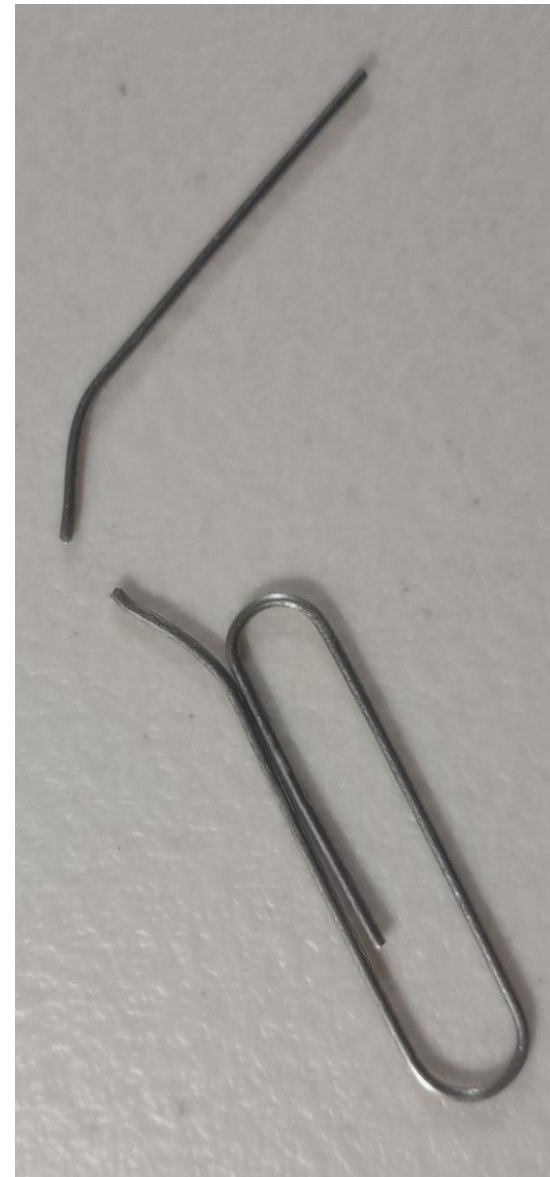
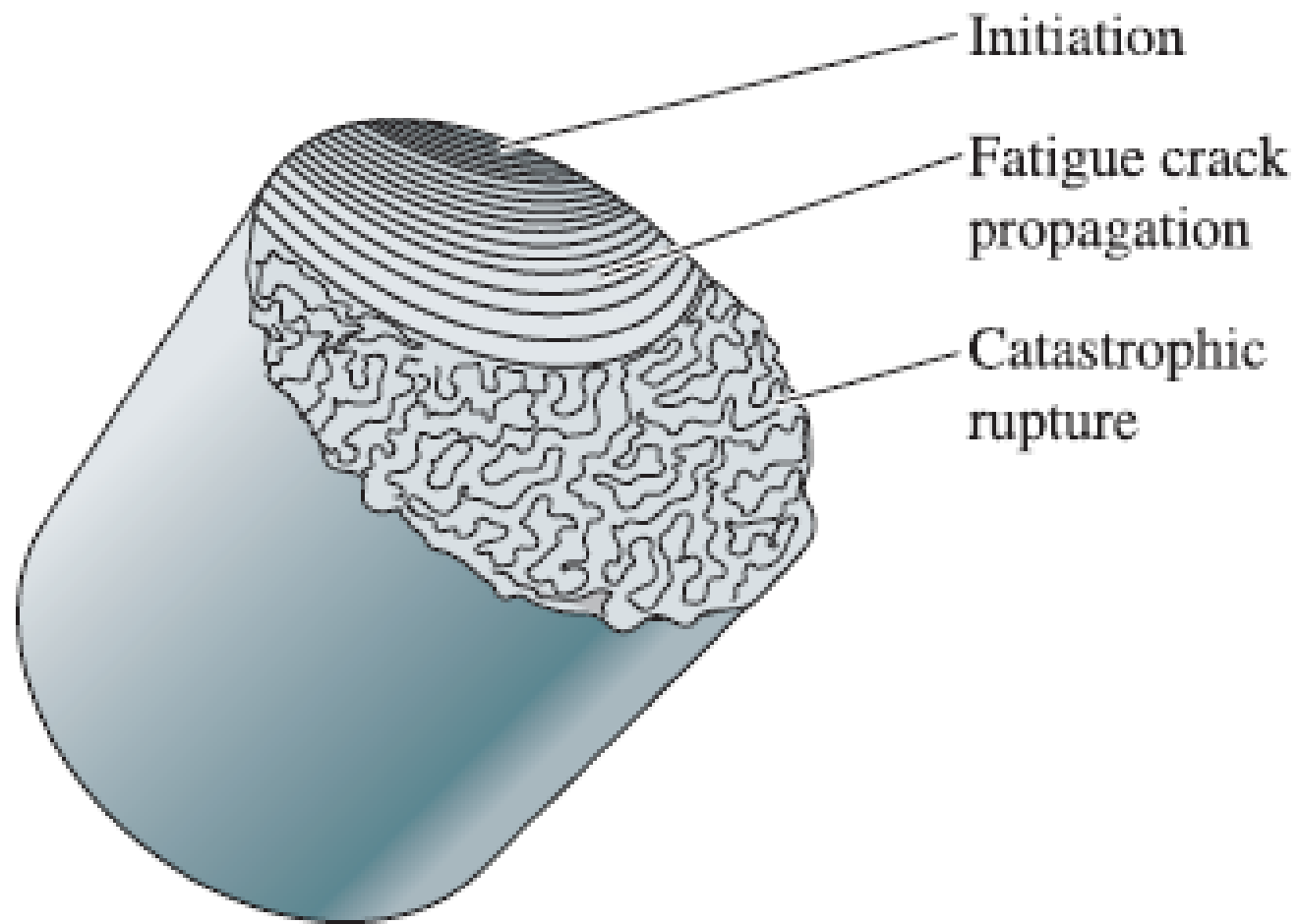
Key parameters of cyclic stress:

- Max and Min stress: σ_{\max} and σ_{\min}
- Average stress σ_{ave}
- Amplitude s
- Cycle frequency f or period T

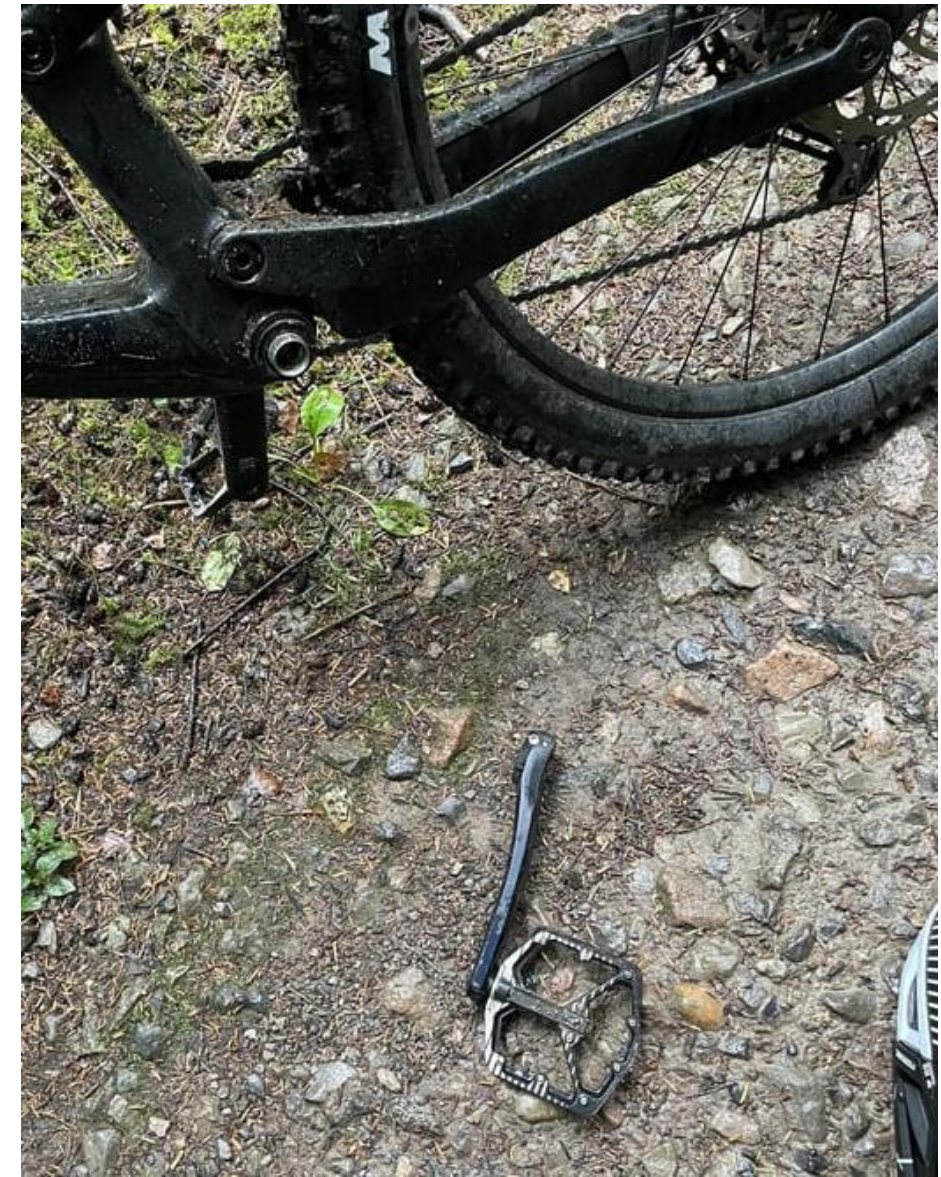
Higher frequency, higher stress (average, amplitude, or max), temperature \rightarrow faster/earlier failure

Microcrack Growth Leading to Fatigue Failure

- Microcracks grow (out of flaws), slowly, eventually leading to catastrophic rupture or fracture



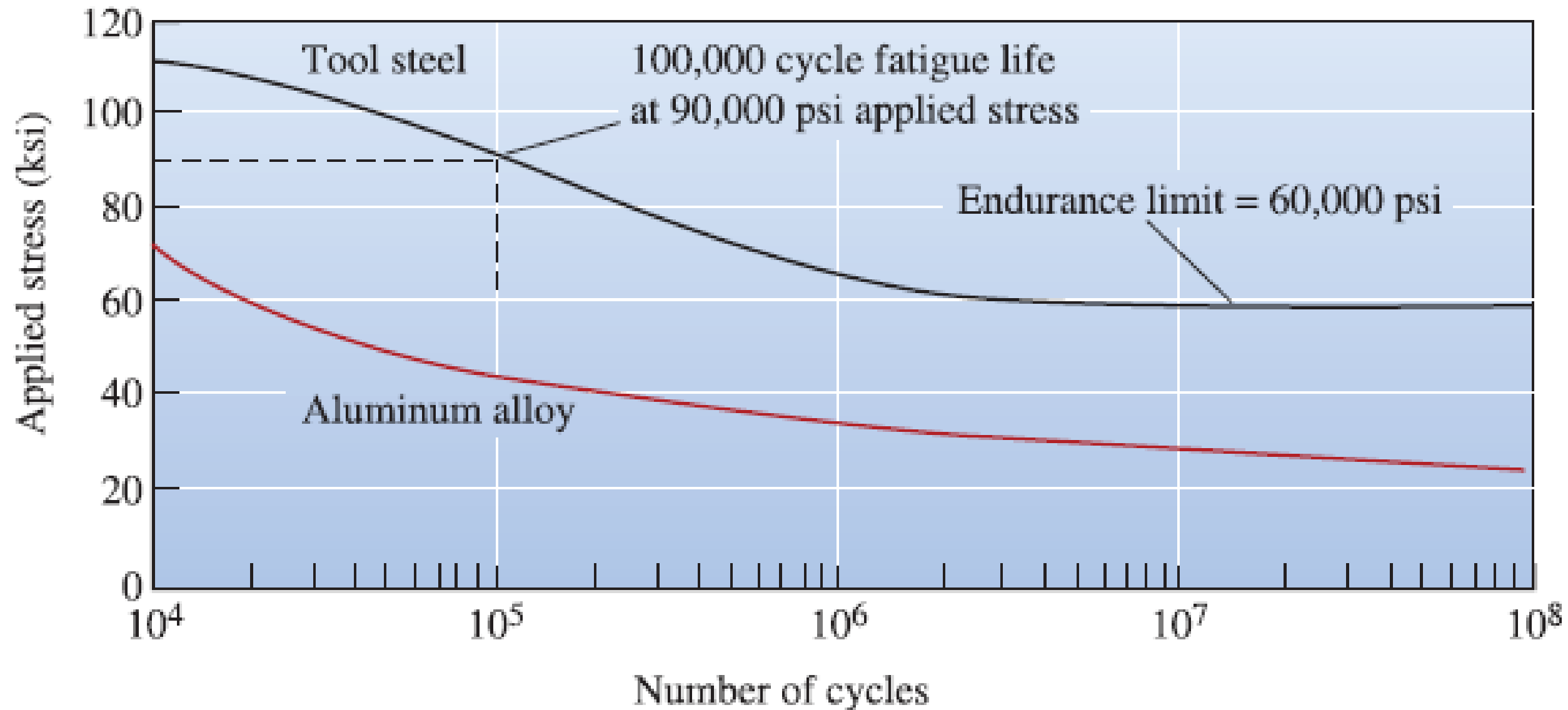
Ruptured paper clip due to fatigue



Ruptured bicycle pedal due to fatigue

Endurance Limit for Fatigue

- As cycle number increases, critical stress (e.g., the stress amplitude) tends to drop
- Critical stress may **stabilize** at some values, called **endurance limit**, for some metals like **steel**, but may **continue to drop** with no lower boundary for some other metal like **aluminum alloy**



Note:
Tool steel
 $\sigma_y \sim 200$ ksi

Aluminum
alloy
 $\sigma_y \sim 70$ ksi
(e.g., for
7075)

A 3rd Means of Mechanical Failure - Creep

Creep

Sample deformation/strain increase over time, at a constant stress (or load)

Primary Creep/1st stage:

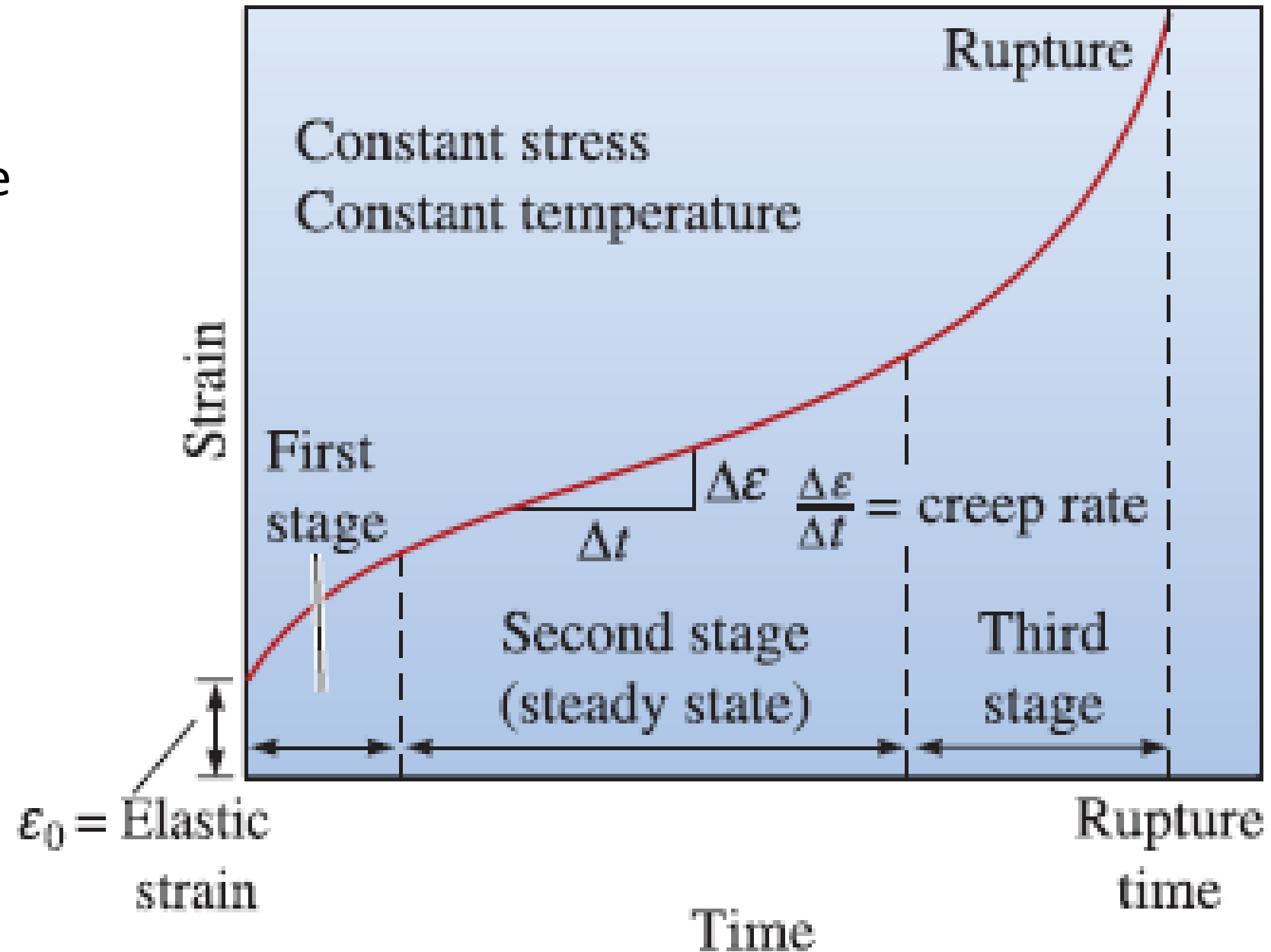
Slope (or creep rate, $\frac{d\epsilon}{dt}$) decreases with time

Secondary Creep/2nd stage:

Constant creep rate

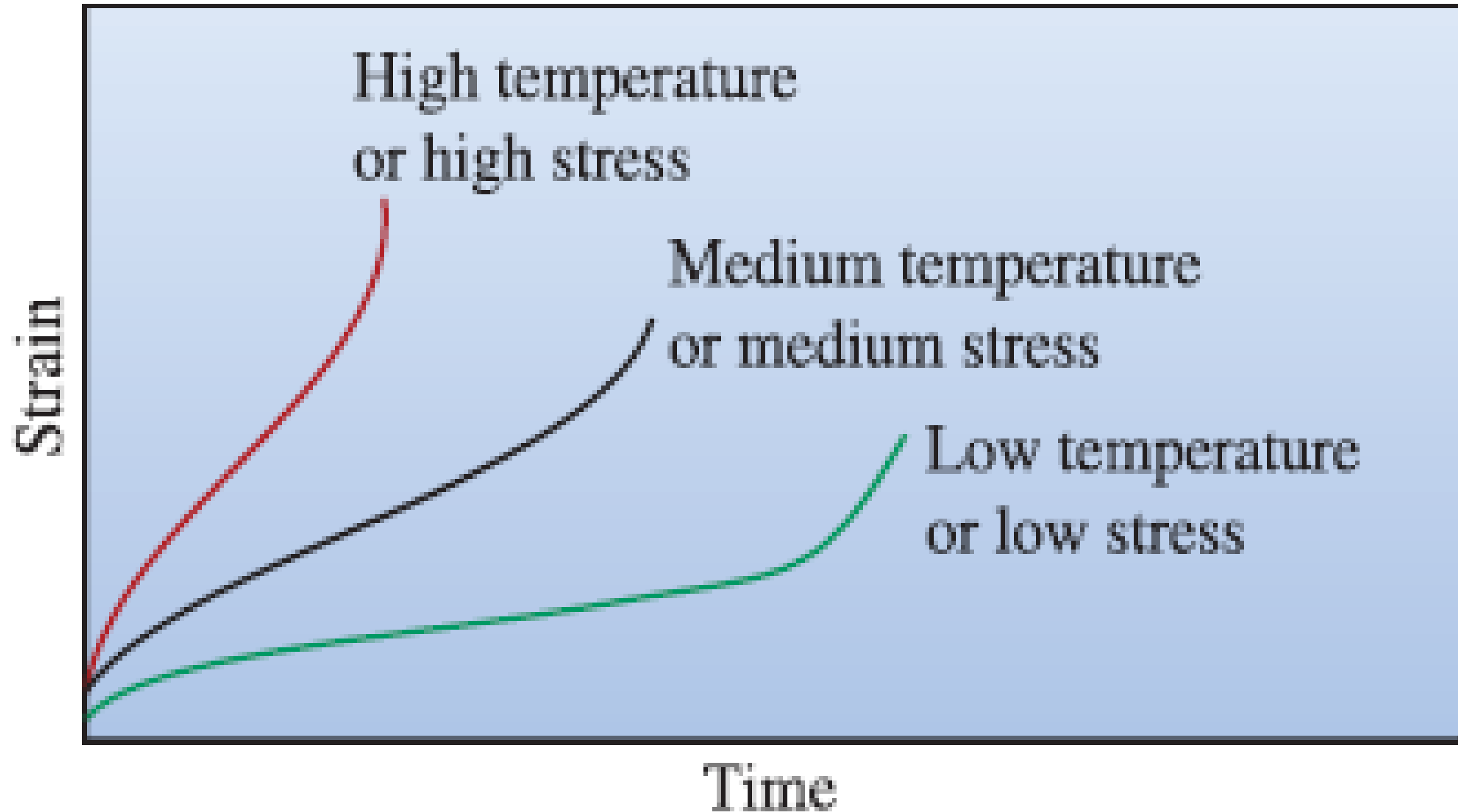
Tertiary Creep/3rd stage:

Creep rate increases with time



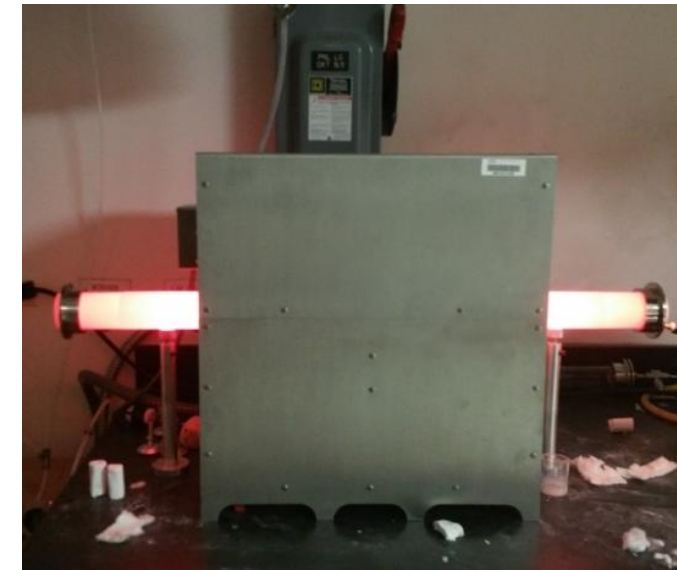
Temperature & Stress Effect on Creep

Above $\sim 0.4 T_m$ (in K), higher temperature or higher stress leads to faster creep



Example of Creep for Al_2O_3 Ceramics ($T_m = 2025\text{ }^\circ\text{C}$)

As received Al_2O_3 tube



After running at $>1400^\circ\text{C}$ for hours w/o proper mechanical support

Curved or fractured Al_2O_3 tube after creep



END

Homework 7.0

Carefully review chapter 7 lecture slides and, if time allows, read textbook sections of Askeland 7.1-7.4, 7.6, 7.9-7.10 (some numerical example problems such as 7-1 to 7-3, 7-10 could be omitted) and give an honor statement confirming the reading

Homework 7.1

- Please write down one question that you are not clear or feel interested about in this chapter (Chapter 7).
- Check for answers using any AI tool and give brief comments on **your challenge to or suspicion of** the answer given by the AI.