

# **Measurement & Evaluation of Packet Reordering Over Internet**

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# Outline

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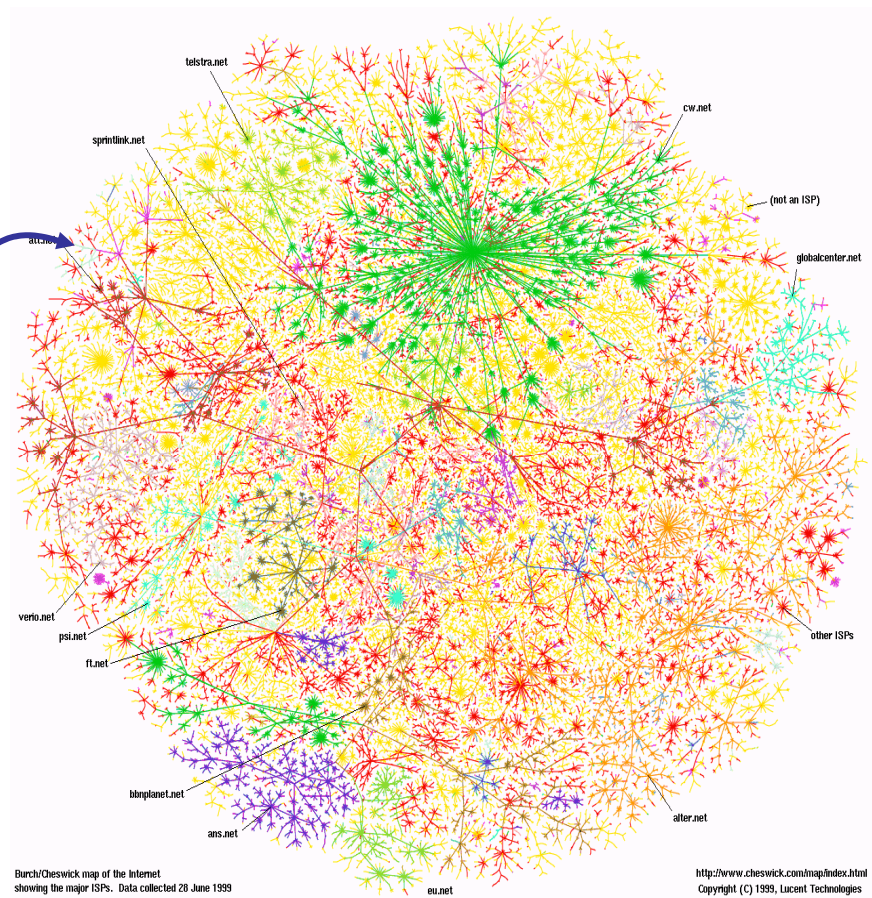
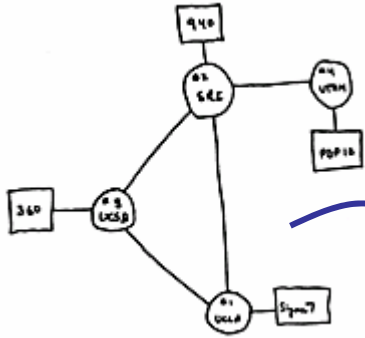
- Introduction
- Contribution
- Part I – Measurement of Packet Reordering over Internet
- Part II – Cascade of n Similar Subnet Problem
- Part III – Packet Reordering & Packet Delay
- Summary

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# Internet



Burch/Cheswick map of the Internet showing the major ISPs. Data collected 20 June 1999

<http://www.cheswick.com/map/index.html>  
Copyright (C) 1999, Lucent Technologies

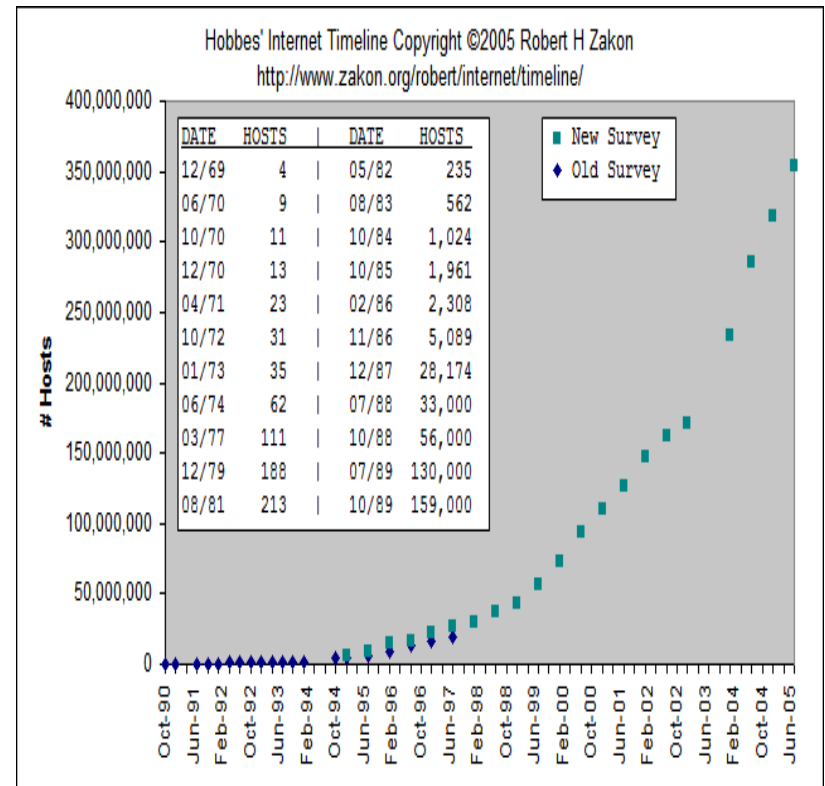
- Big
- Heterogeneity
- Time-varying Behavior

# Internet is still growing !

- Internet traffic growth

- Internet hosts growth

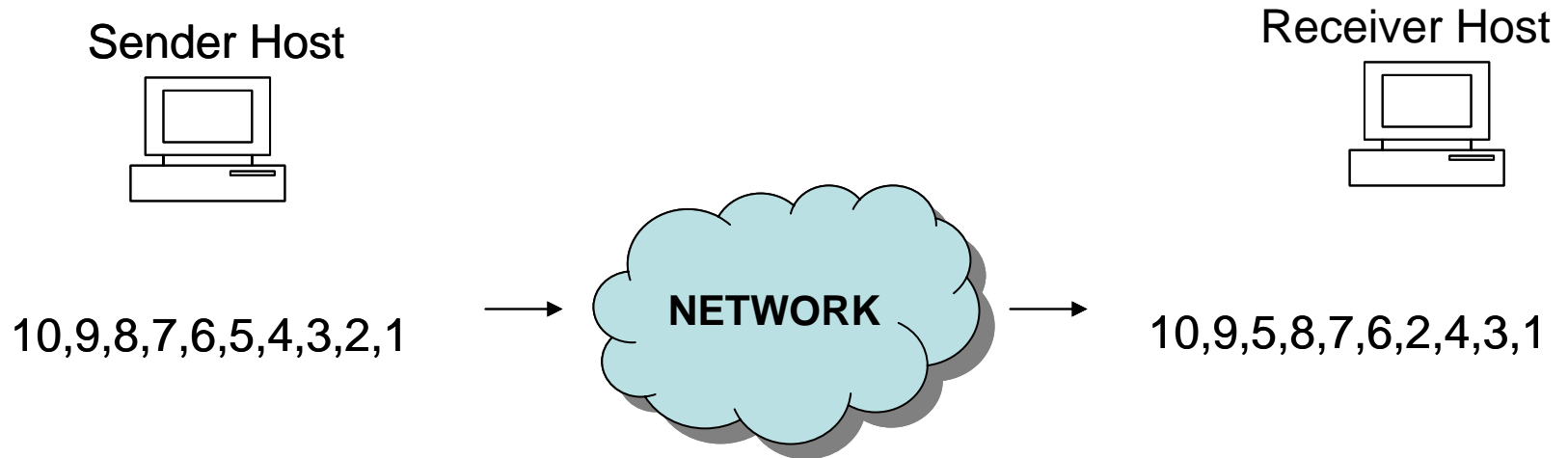
Trend	Doubling period
Semiconductor performance	18 months (Moore's law)
Internet traffic (1969-1982)	21 months
Internet traffic (1983-1997)	9 months
Internet traffic (1997 -2008)	6 months



# Packet Reordering

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- Packet send in order do not reach the receiver in order



# Effect of Reordering

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- Affects TCP performance
  - Forces TCP into false retransmissions
  - That reduces the congestion window size
  - That reduces the bandwidth utilization
- Affects UDP application performance
  - Applications have to re-sequence packets
  - Affects performance of real-time applications such as IP telephony and live streaming video

# Causes of Packet Reordering

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- Parallel processing
- Multi-path routing
- Diffserv Scheduling
- Mobile Ad-hoc network



# Reorder Density

Packet Reordering:

Arrival	1	2	4	5	3	7	6
Receive_index	1	2	3	4	5	6	7
Displacement ( $d_m$ )	0	0	-1	-1	2	-1	1

*m*      ( $m + d_m$ )

- Reorder Event  $r(m, d_m)$ : If the receive\_index assigned to packet  $m$  is  $(m+d_m)$ , with  $d_m \neq 0$  then a reordered event  $r(m, d_m)$  has occurred
- Earliness/Lateness: A packet is late if  $d_m > 0$ , and early if  $d_m < 0$

## Reorder Density – (2)

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- Packet Reordering: Packet reordering is completely represented by the union of reorder events,

$$R = \bigcup_m \{r(m, d_m) \mid d_m \neq 0\}$$

- For the above sequence  $R = \{(3, 2), (4, -1), (5, -1), (6, 1), (7, -1)\}$
- $D_T$ : A threshold on the displacement of packets that allows the metric (RD) to classify a packet as lost or duplicate.

## Reorder Density – (3)

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- Let  $S[k]$  be a subset of  $R$  s.t.

$$S[k] = \{r(m, d_m) \mid d_m = k\}$$

- Then

$$RD [k] = |S[k]| / N' \text{ for } k \neq 0$$

- Where  $N'$  is the total non-duplicate packets received and  $|S[k]|$  is cardinality of set  $S[k]$ .

$$RD[0] = 1 - \sum_{k \neq 0} |S[k]| / N'$$

# Properties of RD

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- Property 1 :

$$RD[i] \geq 0, \forall i \in Z$$

- Property 2:

$$\sum_i RD[i] = 1$$

- Property 3:

$$\sum_i (i \times RD[i]) = 0$$

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# Contribution

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- New singleton packet reordering metrics
  - $P_L$  and  $P_E$
  - $M_D$ ,  $M_L$  and  $M_E$
  - $E_R$
- Measurement of packet reordering over Internet for 336 hours
- Give the general expression of RD on CNSS problem
- Provide the estimation of  $E_R$  on CNSS problem
- Simulation study on the relation between end-to-end packet delay, end-to-end packet reordering and Inter Packet Gap
- Related Publications
  - B. Ye, A. P. Jayasumana and N. M. Piratla, "On End-to-End Monitoring of Packet Reordering over the Internet," Proc. International Conference on Networking and Services (ICNS 2006), Silicon Valley, USA, Jul. 2006 (BibTex).

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# Why we need more metrics?

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- Long time period observation, capture the variation of packet reordering
- Different angle
- Bridge to an existing theory



# Singleton Metrics (1)

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- Percentage of Late Packets ( $P_L$ )

$$P_L = \sum_{i=+1}^{i=D_T} RD[i]$$

- Percentage of Early Packets ( $P_E$ )

$$P_E = \sum_{i=-D_T}^{i=-1} RD[i]$$

## Singleton Metrics (2)

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- Mean displacement of packets ( $M_D$ )

$$M_D = \frac{\left| \sum_{i=-D_T}^{i=D_T} (|i| \times RD[i]) \right|}{\left| \sum_{i=-D_T}^{i=+D_T} RD[i] \right|}$$

## Singleton Metrics (3)

---

- Mean displacement of late packets ( $M_L$ )

$$M_L = \frac{\left[ \sum_{i=1}^{i=+D_T} (i \times RD[i]) \right]}{\left[ \sum_{i=1}^{i=+D_T} RD[i] \right]}$$

- Mean displacement of early packets ( $M_E$ )

$$M_E = \frac{\left[ \sum_{i=-D_T}^{i=-1} i \times RD[i] \right]}{\left[ \sum_{i=-D_T}^{i=-1} RD[i] \right]}$$

## Singleton Metrics (4)

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- Reorder Entropy ( $E_R$ )

$$E_R = (-1) \times \sum_{i=-D_T}^{i=+D_T} (RD[i] \times \log_e (RD[i]))$$

- When

$$RD[i] = \frac{1}{(2D_T + 1)}, i \in [-D_T, D_T]$$

- Maximum  $E_R$  :

$$E_R = \log_e (2D_T + 1)$$

# Websites for measurement

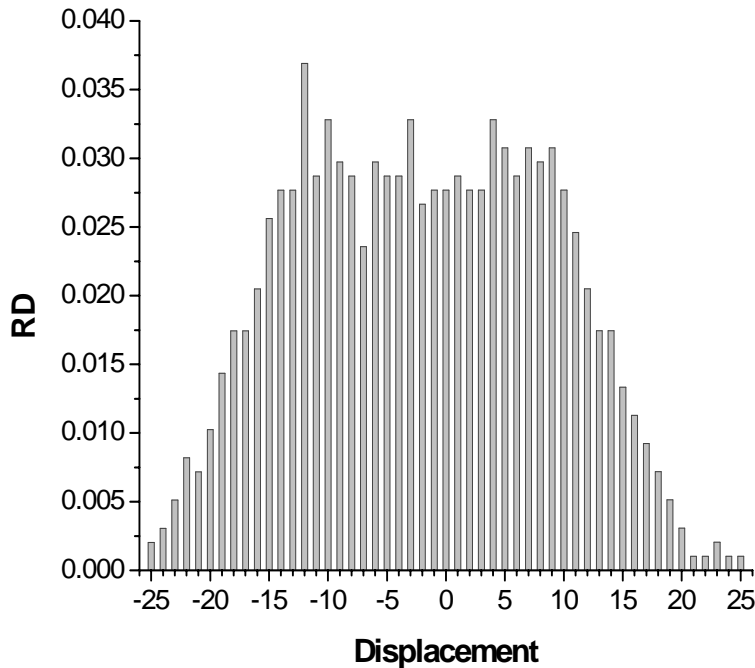
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Net	Destination	IP address	D	SD	Hop Count
1	ftp.chg.ru	193.233.9.194	181.56	3.68	13
2	ftp.debian.skynet.be	195.238.1.7	135	2	22
3	www.mara.org.za	196.21.144.10	317.36	22.6	17
4	informatics.nic.in	164.100.52.6	334.5	2.5	26
5	www.olympus.co.jp	203.178.83.188	144.56	1.05	13
6	Download.microsoft.com	4.78.212.30	3.78	0.59	9

Note: Mean RTT delay and standard deviation of delay in milliseconds, all the readings are obtained from lamar.colostate.edu at 9:05am (MST) 28th April, 2006.

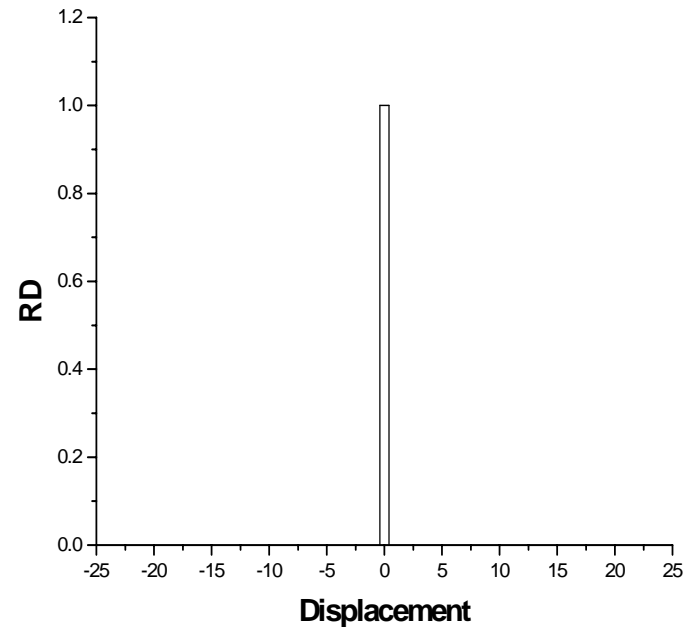
# Results (1)

- $E_R$  get the maximum value



Reorder Density on Net-5 observed at 9:52am  
August 26, 2005 (DT = 25)

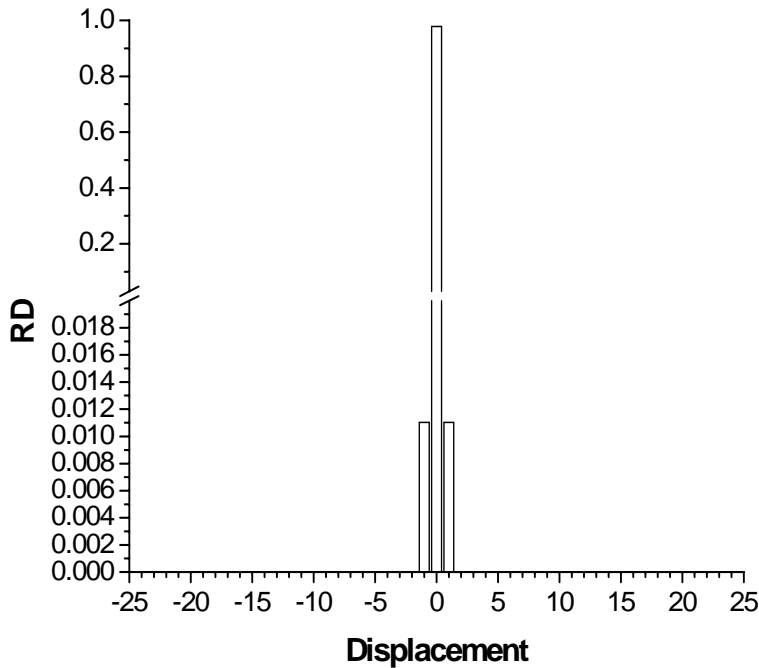
- $E_R = 0$



Reorder Density on Net-5 observed at 8:00am  
Sep 24, 2005 (DT = 25)

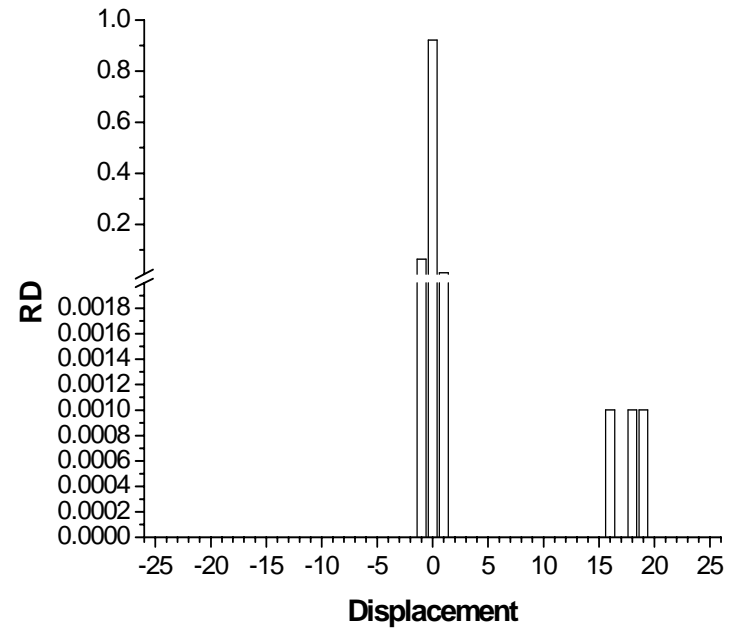
# Results (2)

- $M_L = M_E = 1$



**Reorder Density on Net-5  
observed at 8:00am Sep 24,  
2005 (DT = 25)**

- $M_L > M_E$



**Reorder Density on Net-5  
observed at 12:00am Sep  
24, 2005 (DT = 25)**

## Statistic Data about 5 Websites

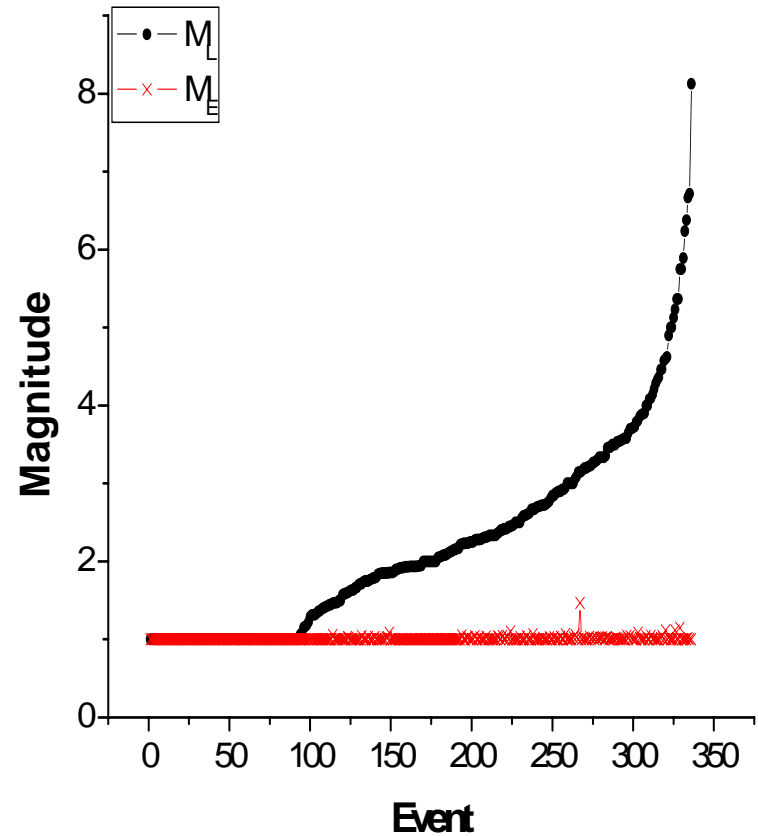
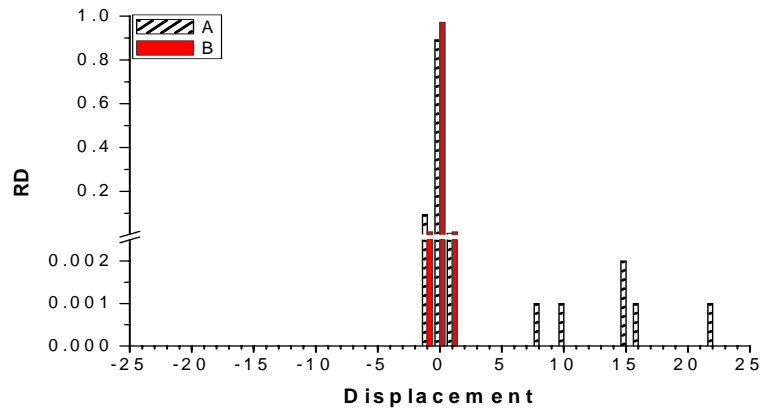
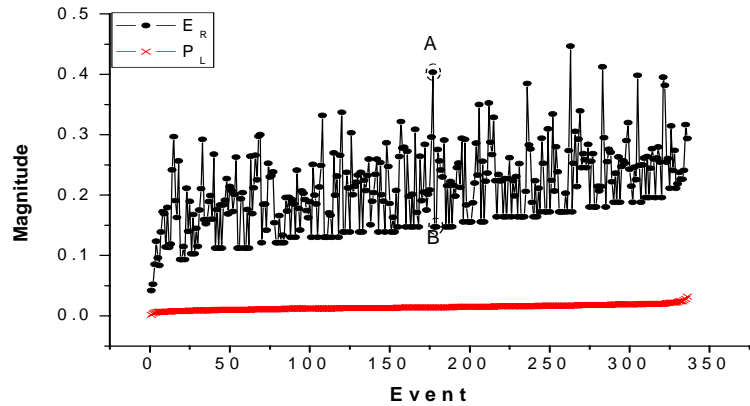
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Net	Mean of $E_R$	Maximize $E_R$ Value	$E_R > 0$	
			Times	Percentage
1	0.20	2.96	236	70.12
2	0.032	0.44	146	43.50
3	0.067	0.84	98	29.00
4	0.091	1.43	120	36.10
5	0.21	0.45	336	100

Note: The total number of measurement for each net is 336 hours(Sep 24 – Oct 8, 2005)

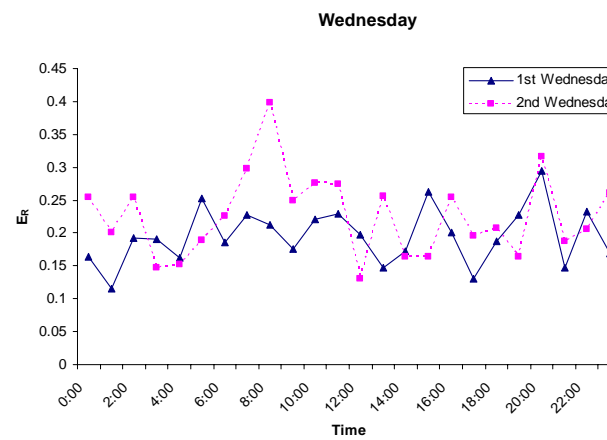
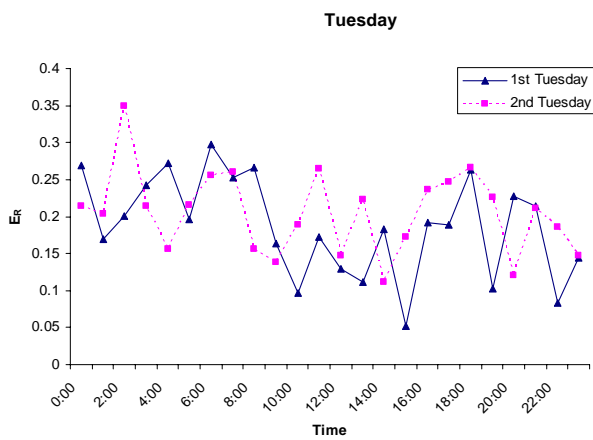
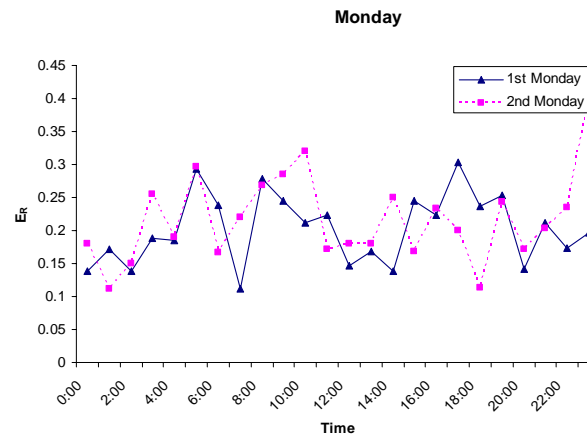
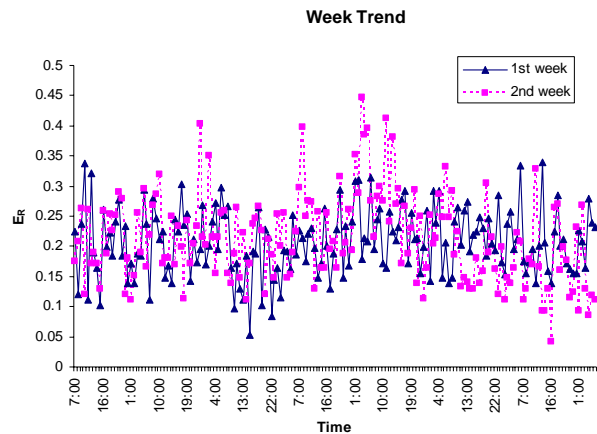


# Result – (3)



RD of points A and B (A – Oct 3rd 23:00 on Net – 5, B – Oct 4th 23:00 on Net - 5)

# Result – (4)



Observation over 2 weeks on Net – 5 (Sep 24 – Oct 8, 2005)

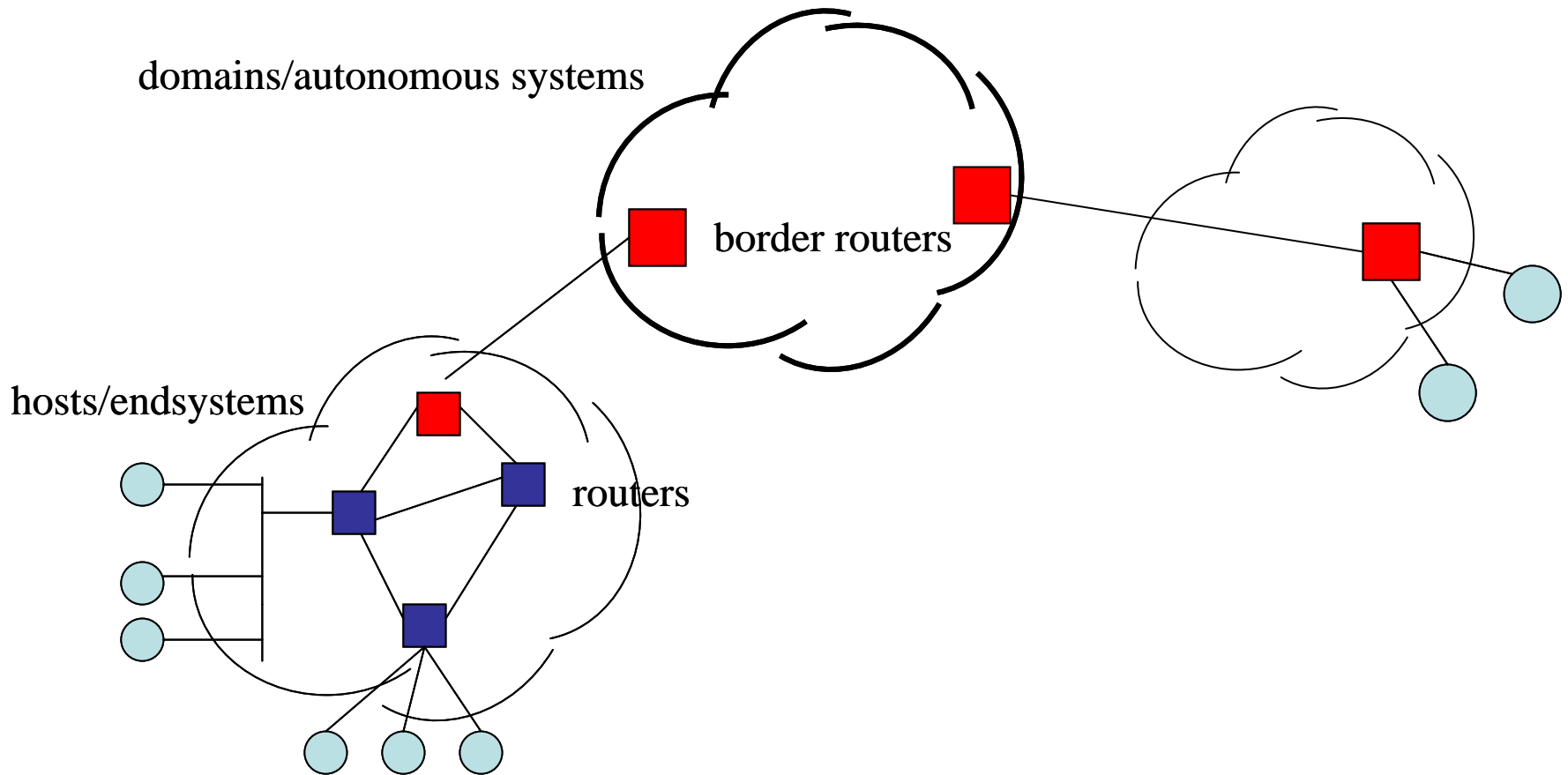
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# AS Topology View of Internet

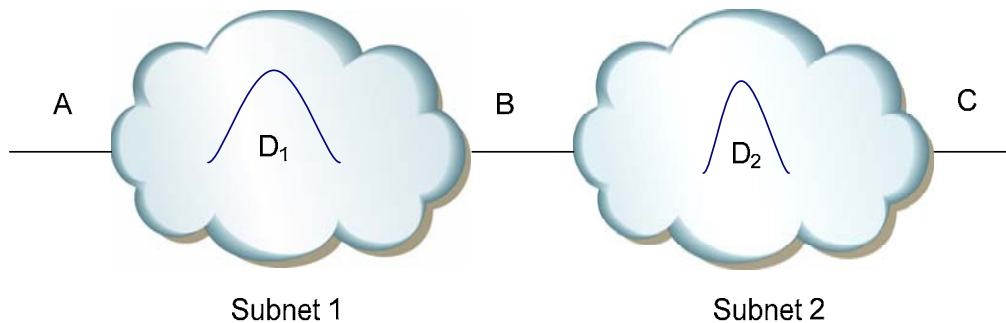
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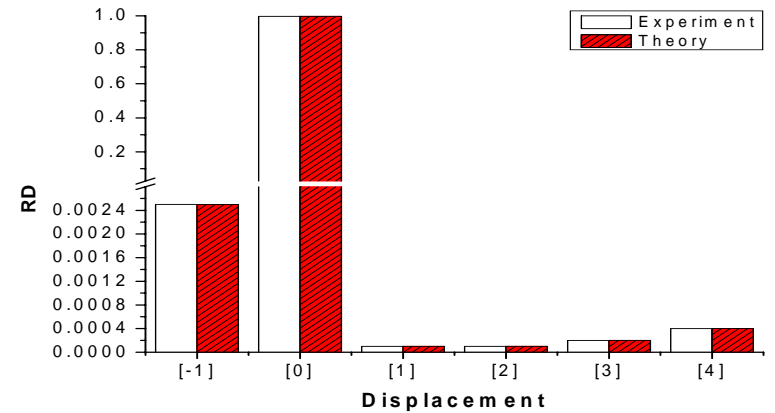
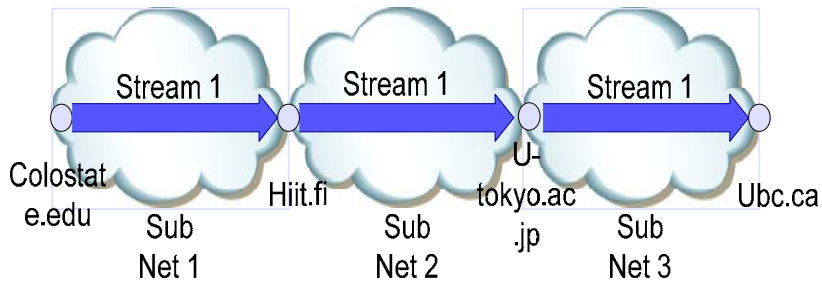
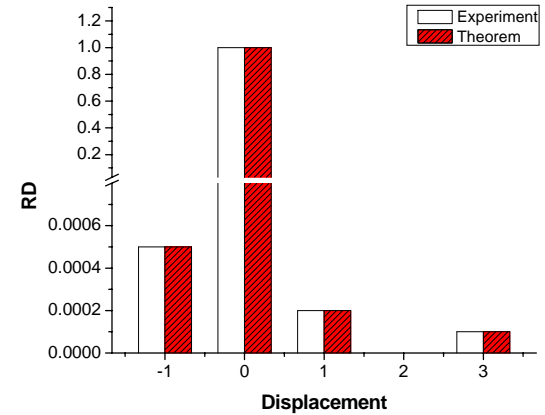
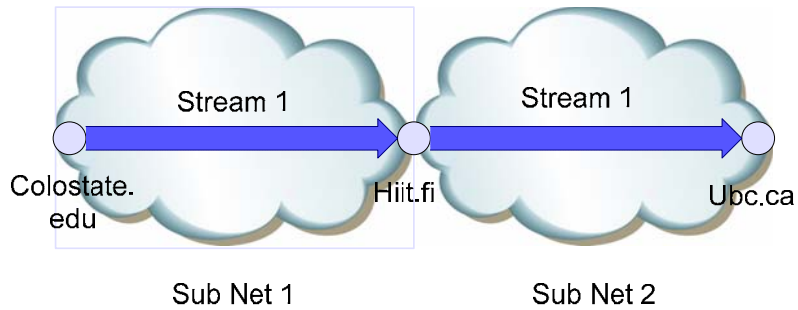
# Convolution between 2 subnets

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- Theorem: The reorder response  $\mathbf{J}[k]$  of a network formed by cascading two subnets, with reorder responses  $\mathbf{J1}[k]$  and  $\mathbf{J2}[k]$ , respectively, is given by the convolution of  $\mathbf{J1}[k]$  and  $\mathbf{J2}[k]$ , i.e.,  $\mathbf{J}[k] = \mathbf{J1}[k] * \mathbf{J2}[k]$ .*



# Verification over Internet



# CNSS Statement

- Conditions:

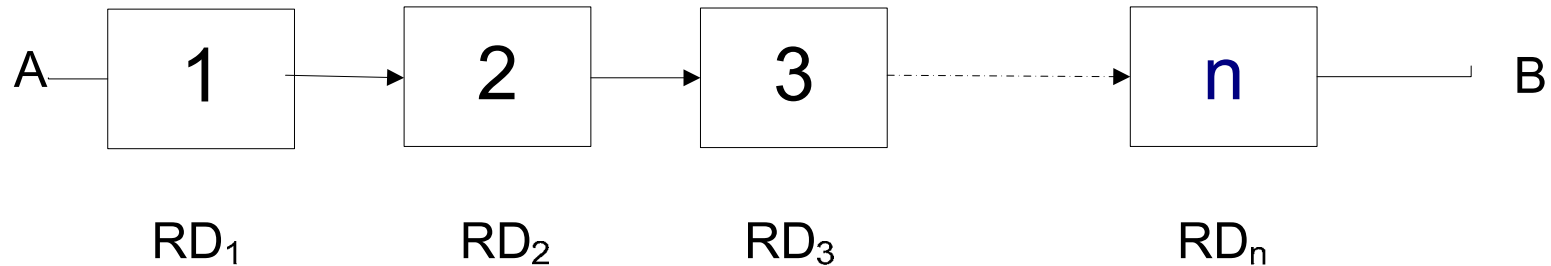
$$RD_i = RD_j, \forall i, j \in Z$$

$$\text{Var}(D_i) = \sigma_0^2$$

$$Y = \sum_{i=1}^n D_i$$

- Question: Can we evaluate following parameters ?

$$RD^{(AB)} \quad E_R^{(AB)}$$

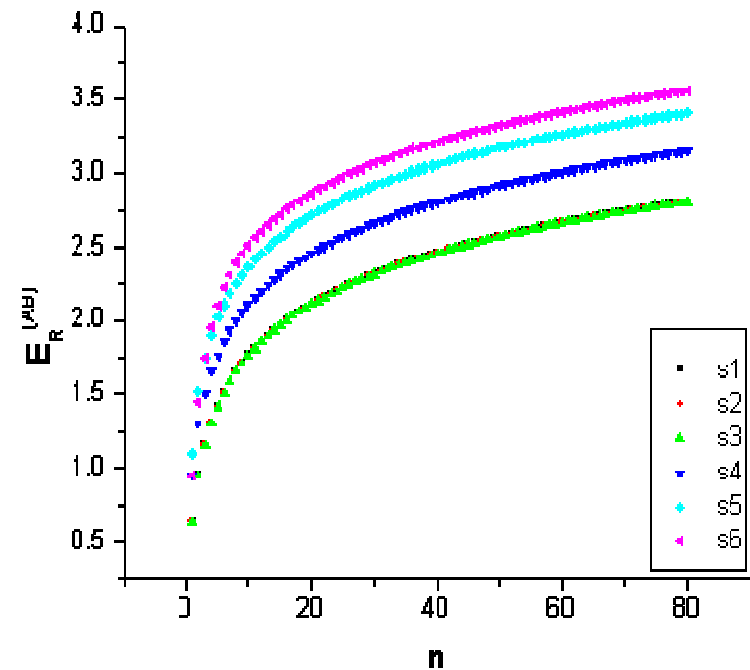


- For  $RD_i$ ,  $P\{D_i = j\} = RD[j], \forall j \in \square, j = -D_T, \dots, 0, \dots, D_T,$

# Simulation Result On CNSS

- Symmetric Group
- Symmetric means RD is about RD[0]
- $n = 80$

Case Name	-3	-2	-1	0	1	2	3
s1			0.1	0.8	0.1		
s2		0.1	0	0.8	0	0.1	
s3	0.1	0	0	0.8	0	0	0.1
s4			0.2	0.6	0.2		
s5			0.333	0.3334	0.333		
s6			0.45	0.1	0.45		

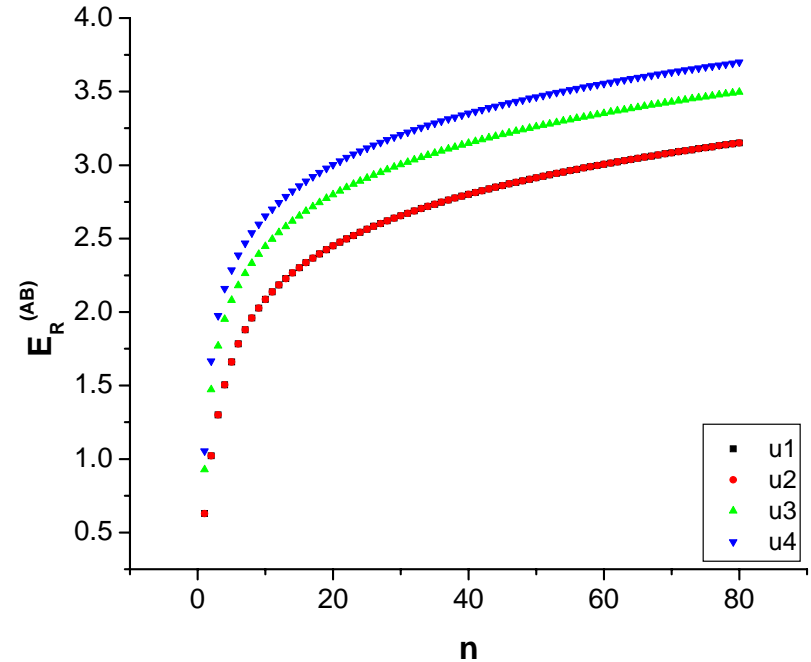




# Simulation Result On CNSS

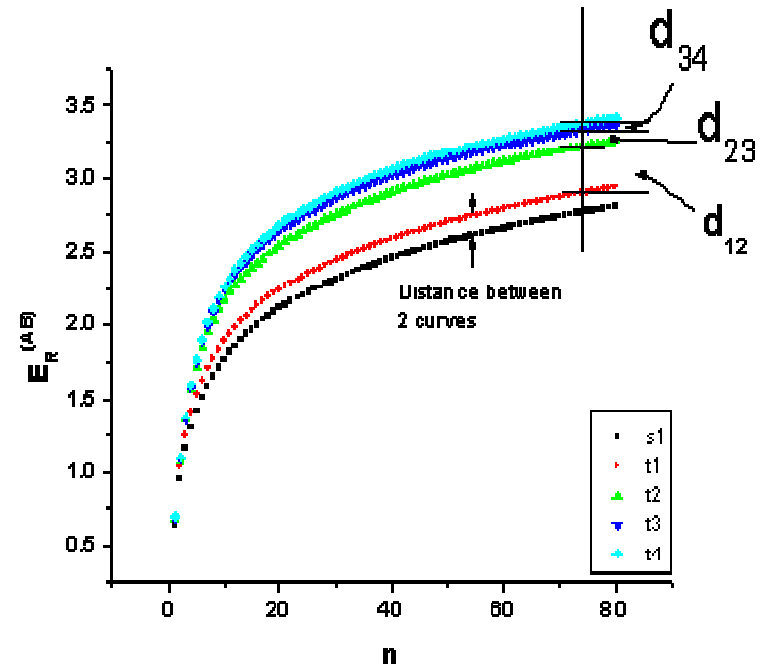
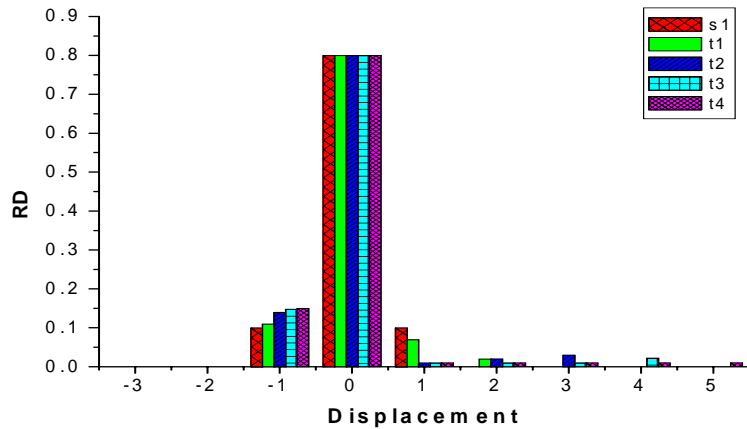
- Asymmetric Group
- $n = 80$

Case Name	-2	-1	0	1	2
u1	0	0.133	0.8	0	0.067
u2	0.067	0	0.8	0.133	
u3	0	0.267	0.6	0	0.1333
u4	0	0.4	0.4	0	0.2



# Simulation Result On CNSS

Case Name	-1	0	1	2	3	4	5
s1	0.1	0.8	0.1				
t1	0.11	0.8	0.07	0.02			
t2	0.14	0.8	0.01	0.02	0.03		
t3	0.148	0.8	0.01	0.01	0.01	0.022	
t4	0.15	0.8	0.01	0.01	0.01	0.01	0.01



# Theoretical Analysis

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- General Expression of RD on CNSS (By generation function express)

$$\sum_{k_1, k_2, k_3, \dots, k_m} \binom{n}{k_1, k_2, k_3, \dots, k_m} (RD[-D_T]s^{-D_T})^{k_1} \dots (RD[0])^{k_i} \dots (RD[D_T]s^{D_T})^{k_m}$$

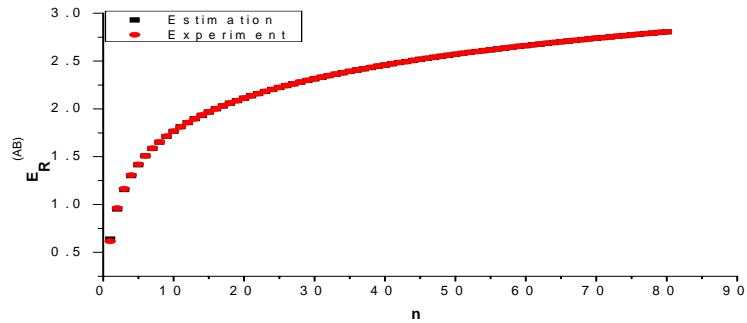
- Where  $\sum_{i=1}^m k_i = n$   $\binom{n}{k_1, k_2, k_3, \dots, k_m} = \frac{n!}{k_1! k_2! k_3! \dots k_m!}$

- Estimate of Reorder Entropy on CNSS

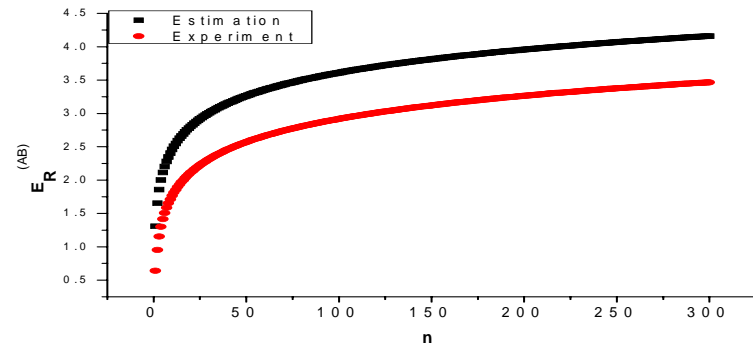
$$E_R^{(AB)} = \frac{1}{2} + \frac{1}{2} (\ln 2\pi) + \frac{1}{2} (\ln n) + \ln(\sigma_0)$$

# Comparison

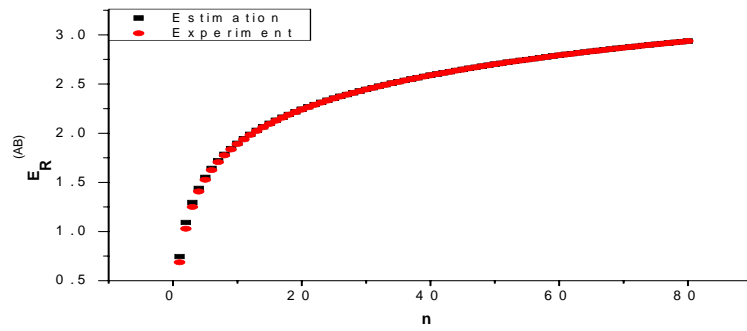
- s1



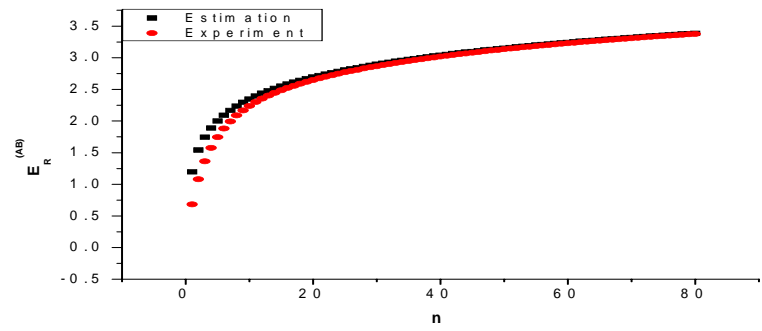
- s2



- t1



- t4



# Estimation on RD[0]

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$$RD[0] = P(Y > 0) - P(Y > 1)$$

$$= \Phi\left(\frac{1-nm}{\sigma_0\sqrt{n}}\right) - \Phi\left(\frac{0-nm}{\sigma_0\sqrt{n}}\right)$$

$$= \Phi\left(\frac{1}{\sigma_0\sqrt{n}}\right) - \Phi(0)$$

Case Name	s1	s2	s4	t1	t2	u4
Estimation value of RD[0]	0.099	0.049	0.070	0.087	0.060	0.0398
Experimental value of RD[0]	0.10006 0103	0.10006 0103	0.07046 9	0.08790 6	0.06355 9	0.04059 8

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# Simulation Parameters

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- Gamma Distribution
- BestFit 4.0 generate the Independent packet delay
- Use Reorder Entropy to evaluate packet reordering
- Changing the Inter Packet Gap
- Strategy

- Gamma Distribution

$$f(x; k, \theta) = x^{k-1} \frac{e^{-\frac{x}{\theta}}}{\theta^k \Gamma(k)}, \forall x > 0$$

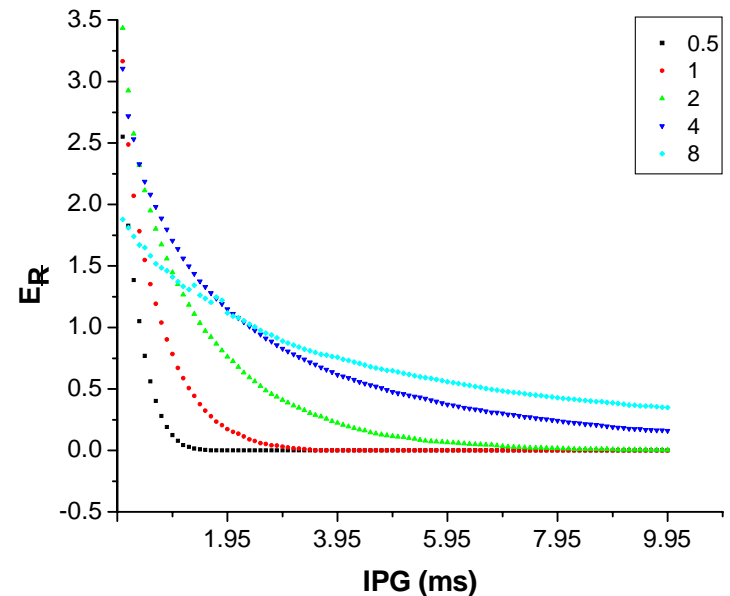
- Parameters

Parameters	Expression
Mean	$k\theta$
Variance	$k\theta^2$
Coefficient of Variation	$\frac{1}{\sqrt{k}}$

# Simulation Result

- Gamma-distribution parameters for Group 1 with fixing the mean at a constant value of 1008 millisecond (ms)

Mean Constant	Target Standard Deviation change ratio	Target Standard deviation	K	$\theta$
1007.86358	0.5	307.6417232	10.7328	93.905
1007.86358	1	615.2834464	2.6832	375.62
1007.86358	2	1230.566893	0.6708	1502.48
1007.86358	4	2461.133786	0.1677	6009.92
1007.86358	8	4922.267571	0.041925	24039.68

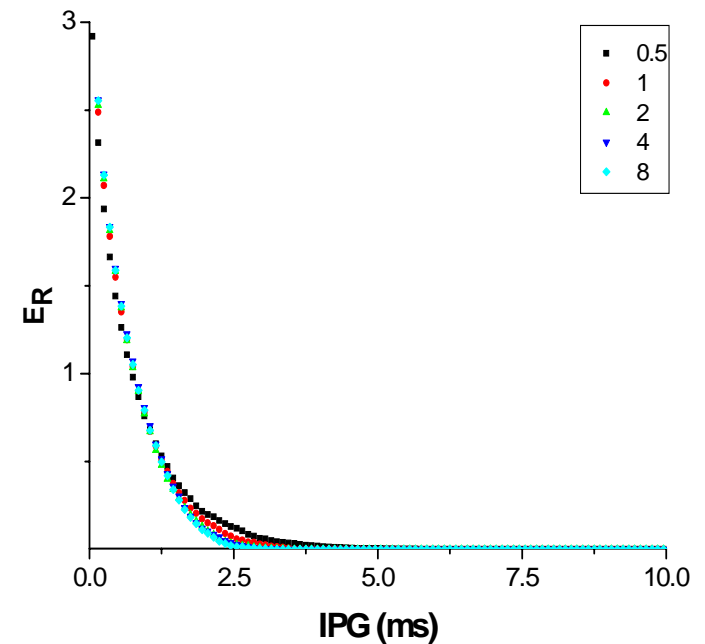




# Simulation Result

- Gamma-distribution parameters for Group 2 with fixing the SD at a constant value of 615 millisecond

Constant Standard Deviation	Target Mean change ratio	Target Mean	K	$\theta$
615.283446	0.5	503.931792	0.6708	751.24
615.283446	1	1007.863584	2.6832	375.62
615.283446	2	2015.727168	10.7328	187.81
615.283446	4	4031.454336	42.9312	93.905
615.283446	8	8062.908672	171.7248	46.9525



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# Summary

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- Some Internet path display the weekly and daily trend on packet reordering, where others are in random. Packet reordering is time varying
- Give the general expression of Reorder Density on CNSS and Estimation of Reorder Entropy of CNSS
- Simulation on IPG, packet delay and packet reordering, shows that higher SD of end-to-end packet delay results in a higher level of packet reordering. For the same packet delay distribution, the level of packet reordering decreases with the increase in Inter Packet Gap.

# Future

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- Could the Internet be an application of existing theory about entropy ?
- Is it possible to predict the network condition by packet reordering?

- 
- Questions ?
  - Thank You