

Single
Phase
Buck

Q_1 ON

L_1 stores i

Q_1 off

Q_2 ON

L_1 sources

load

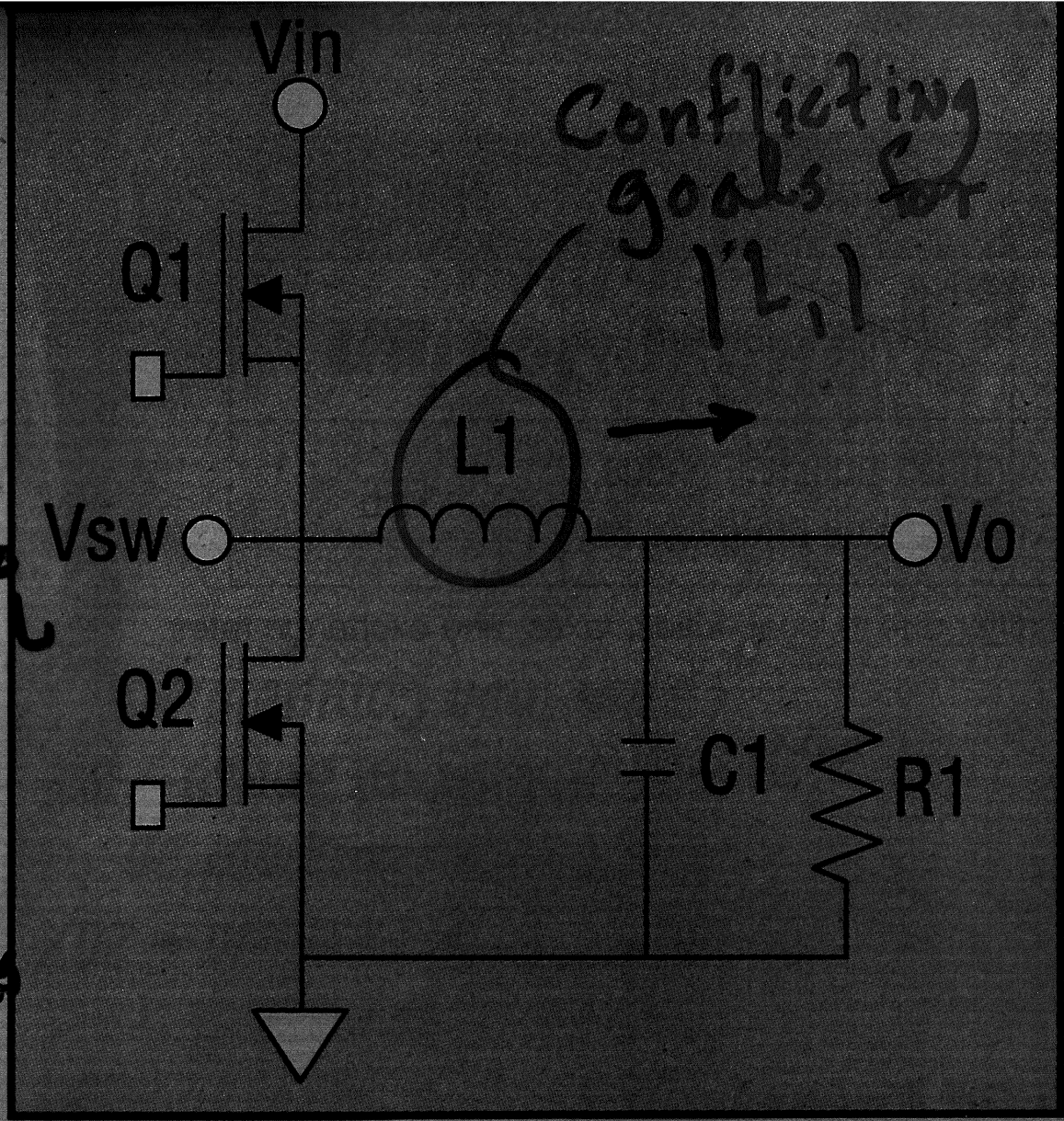


Fig. 1. Simplified schematic of a typical synchronous buck converter. The inductor current always flows through either Q_1 or Q_2 . During the on-time, Q_1 is ON, and inductor current increases. During the off-time, Q_2 is ON, and the inductor current decreases. At the on/off transition times, the inductor current has to quickly switch from one FET to the other one.

High L for low ripple

Low L for fast dI_{out}/dt

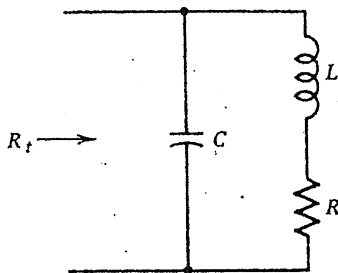
EE 576 Homework Set 10

- You have just graduated and started a new job at a semiconductor equipment manufacturer. You are now PAID to work on processes driven by RF generators at 13.56 MHz. These generators want to work into a 50Ω resistive load, but, amazingly, your process looks like a 5Ω resistive load.

You need to match the generator to the load, but are, unfortunately, mystified, until one of your friends points you to a book entitled "Solid State Radio Engineering" by Krauss, Bostian, and Raab. Use the circuit and "exact equations" in Table 3-3.1 from the book (see below) to make your 5Ω resistive load look like a 50Ω resistive load and show that you have gotten the correct L and C.

Alternatively, you look at the network below and write an expression for the input impedance, knowing it must be 50 Ohms or real impedance and zero Ohms of reactive impedance. With two equations and two unknowns –you are ready for Mathcad/Matlab etc. solutions. Show all work and document each step with comment statements.

TABLE 3-3.1 Design Formulas for the Resonant $RL\parallel C$ Circuit



Quantity	Exact Expression	Units	Approximate Expression, $Q_t \geq 10$
ω_o	$= \left(\frac{1}{LC} - \frac{R^2}{L^2} \right)^{1/2}$	rad/s	$\approx \frac{1}{\sqrt{LC}}$
Q_t	$\equiv \frac{\omega_o L}{R} = \omega_o C R_t$		$\approx \frac{1}{\omega_o C R}$
$\omega_o L$	$= \frac{1}{\omega_o C} \left(\frac{Q_t^2}{Q_t^2 + 1} \right)$	ohms	$\approx \frac{1}{\omega_o C}$
R_t	$= \frac{L}{C R} = \frac{Q_t}{\omega_o C}$ $= R(Q_t^2 + 1)$	ohms	$\approx Q_t^2 R = \omega_o L Q_t$
B		hertz	$\approx \frac{1}{2\pi C R_t} = \frac{R}{2\pi L} = \frac{f_o}{Q_t}$

1 ϕ Buck

I_{out} : 50A notebook
100A desktop
150A server

} $I^2 R$ losses
high for
one
path

Conflict / Compromise on single

"L" is necessary

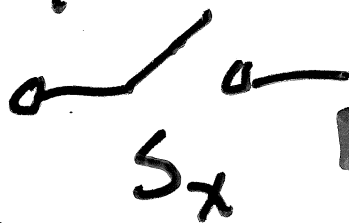
Big "L"

for small
 Δi_L

small "L"
for fast $\frac{di_L}{dt}$



Solution: "x" separate current paths each with own



and L_x
Shift phases
to reduce $|\Delta i_L|$

$$\sum_{x=1}^N i_x = i_{out}$$

Phase shift Δi_x to minimize
 Δi_{out}

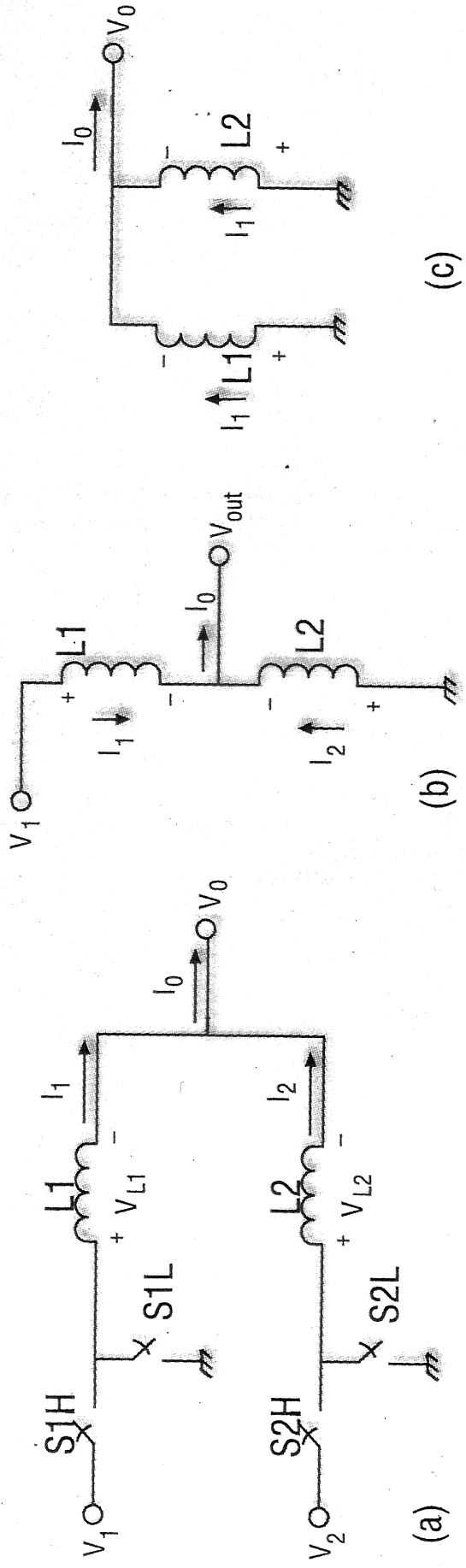


Fig. 2. A simplified schematic of a multiphase uncoupled buck regulator (a) illustrates the two basic switching actions. In state one (b), S1H and S2L are closed while S1L and S2H are open. The input then sources energy to L1 and the output, and L2 sources energy to the output. In state two (c), S1L and S2L are closed, and S1H and S2H are open. Thus, both inductors source energy to the output. These operations are reversed for states three and four (not shown).

$I^2 R$ loss @ 150 A server too high
for one path use several
parallel paths

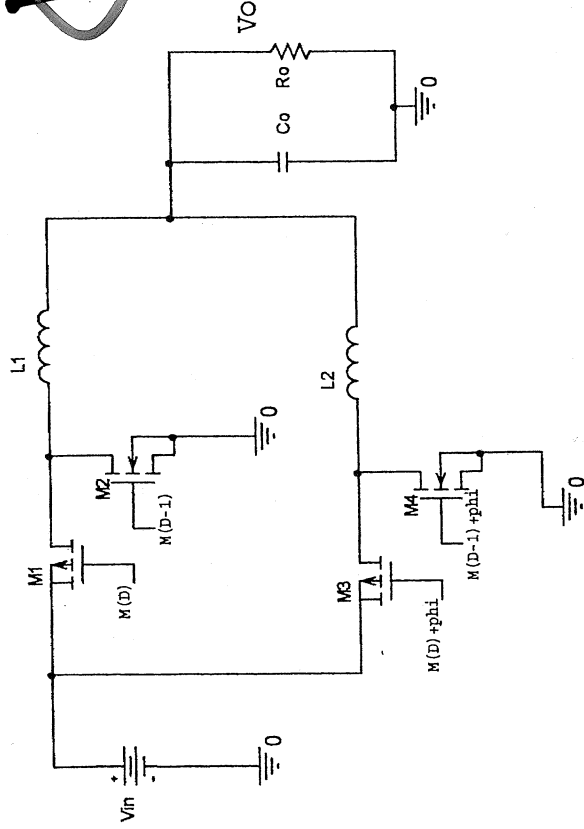
$I_{in} \downarrow$

yet I_{o} same

$I_M \downarrow$
 $I_{in} \downarrow$

loss due to $I_{in}^2 R_{in}$ as N^2
loss down as N^2

Multiphase Output:



- Reduces output ripple due to cancellation of inductor ripple currents
- Relaxes maximum current rating requirements of switches, inductors and caps
- Reduces stress and I^2R loss on input source by reducing amplitude of input current pulses

① State 1: 2ϕ $0 \rightarrow D T_{sw}$

$$di_1 = \frac{V_{IN}}{L_1} (1-D) D T_{sw}$$

$$di_2 = \frac{V_{IN}}{L_2} (D) D T_{sw}$$

$V_{IN} \xrightarrow{L_1} V_O \rightarrow$
 $\xrightarrow{L_2} V_O \rightarrow$
 $L_1 = L_2 = L$

$L_1 = L_2$ $di_{out} = di_1 + di_2$

$$di_{out} = \frac{V_{IN}}{L} (1-2D) D T_{sw} \quad \Delta t$$

② State 2: 2ϕ

$$t = D T_{sw} \rightarrow \frac{T_{sw}}{2}$$

ripple is at $2 f_{sw}$

$\xrightarrow{L_1} V_O \rightarrow$
 $V_{IN} \xrightarrow{L_2} V_O \rightarrow$

$$di_{out} = -\frac{V_{IN}}{L} (1-2D) D T_{sw} \quad \Delta t$$

Recall $di_{out} (1\phi) : \frac{V_{IN}}{L} (1-D) D T_{sw}$!

$$\frac{\Delta i_{out} (2\phi)}{di_{out} (1\phi)} = \frac{1-2D}{1-D}$$

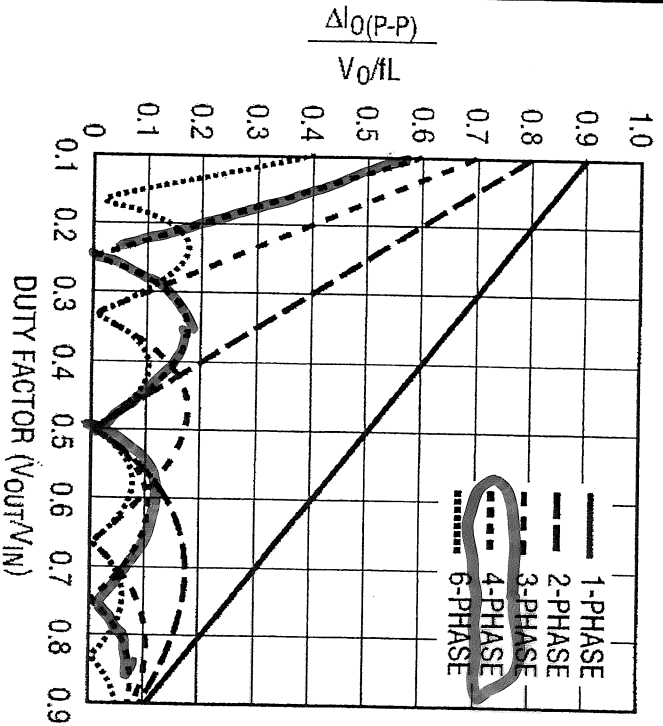
lower di_{out} for all D

OR

L reduced for same di_{out} but faster di_{in}/dt

Divout (multiphase) can be zero for same D Frequency and Phases

For $V_{in} = 5V$, $V_{out} = 1.8V$, $D \approx 0.35$



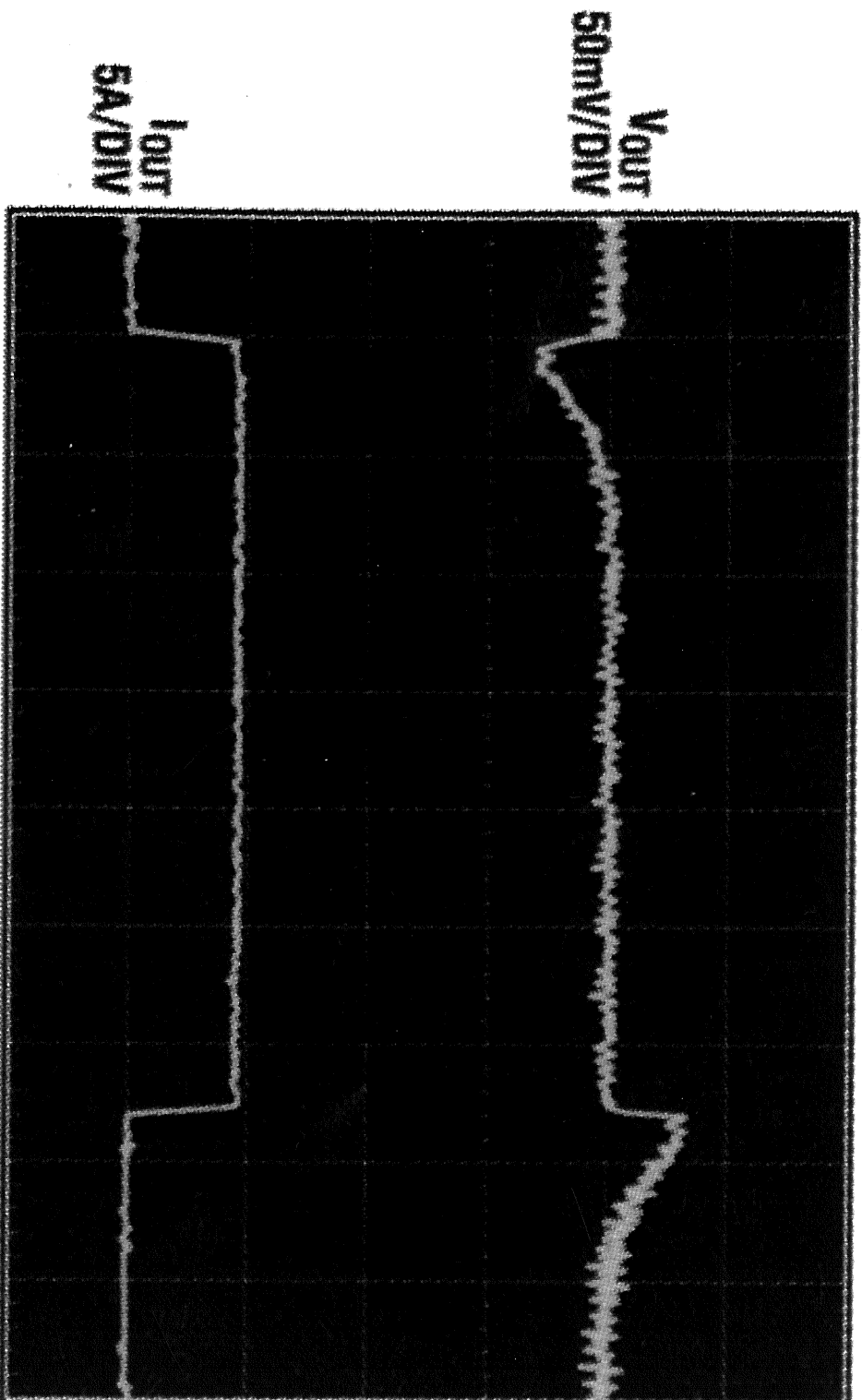
- Optimal number of phases 3 or 6
- Though 4 or even 2 phases also provides good output ripple cancellation versus a single phase

$$\Delta i_{out} = 0 @ D = 0.35$$

0.25
0.50
0.75

Ultrafast Transient Response

2% ΔV_{OUT} with a 5A Step



$V_{IN} = 12V$, $V_{OUT} = 1.5V$, 0A to 5A Load Step
($C_{OUT} = 3 \times 22\mu F$ CERAMICS, 470 μF POS CAP)