1 2	Advanced Deep Learning-Based Supervised
3	Classification of Multi-Angle Snowflake Camera Images
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## ABSTRACT

We present improvements over our previous approach to automatic winter hydrometeor 15 classification by means of convolutional neural networks (CNNs), using more data and improved 16 training techniques to achieve higher accuracy on a more complicated dataset than we had 17 previously demonstrated. As an advancement of our previous proof-of-concept study, this work 18 demonstrates broader usefulness of deep CNNs by using a substantially larger and more diverse 19 20 dataset, which we make publicly available, from many more snow events. We describe the collection, processing, and sorting of this dataset of over 25,000 high-quality multiple-angle 21 snowflake camera (MASC) image chips split nearly evenly between five geometric classes: 22 23 aggregate, columnar crystal, planar crystal, graupel, and small particle. Raw images were collected over 32 snowfall events between November 2014 and May 2016 near Greeley, 24 Colorado and were processed with an automated cropping and normalization algorithm to yield 25 224x224 pixel images containing possible hydrometeors. From the bulk set of over 8,400,000 26 extracted images, a smaller dataset of 14,793 images was sorted by image quality and 27 recognizability (Q&R) using manual inspection. A presorting network trained on the Q&R 28 dataset was applied to all 8,400,000+ images to automatically collect a subset of 283,351 good 29 snowflake images. Roughly 5,000 representative examples were then collected from this subset 30 31 manually for each of the five geometric classes. With a higher emphasis on in-class variety than our previous work, the final dataset yields trained networks that better capture the imperfect 32 cases and diverse forms that occur within the broad categories studied to achieve an accuracy of 33 96.2% on a vastly more challenging dataset. 34

# **Significance Statement**

Classification of precipitation, namely, deciding to which of the several typical classes of 36 winter hydrometeors the observed particles belong, can enrich our understanding of polarimetric 37 radar signatures of snow, as well as ice cloud processes and the resulting precipitation 38 production. The high-resolution photographs of snowflakes collected by the multi-angle 39 snowflake camera (MASC) are especially suitable for snowflake classification. However, 40 classifying particle types from MASC photographs by visual inspection is not practical given the 41 42 typical amounts of MASC data. We present advanced automatic deep machine learning-based 43 classification of MASC images using convolutional neural networks. This study demonstrates 44 broad usefulness of our approach yielding trained networks that achieve extremely high 45 classification accuracy on a large and diverse dataset from many snow events.

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## 47 **1. Introduction**

Snowflake classification is important for improved weather radar, assessment of storm 48 structure, and characterization of winter precipitation events from ground sensors (Zhang et al. 49 2011, Straka et al. 2000, Libbrecht 2017). Several types of in-situ image capturing devices used 50 for ground-based collection of data relevant to snowflake classification include the Two-51 Dimensional Video Disdrometer (Schönhuber et al. 2008), the Precipitation Instrument Package 52 (an improved version of the system in Newman et al. 2009), and the Multi-Angle Snowflake 53 Camera (MASC). We focus on snowflake images collected by MASC systems in the present 54 study. To allow researchers to study the microphysical characteristics of snowfall, relevant to a 55 56 storm's composition, the MASC captures high resolution images of falling hydrometeors from

several angles. These images can be processed to extract images of individual snowflakes from a
variety of perspectives, or even used to generate 3D models of hydrometeors automatically
(Kleinkort et al. 2017). A MASC system is capable of capturing tens to hundreds of thousands of
images during a single winter storm event, leading to datasets too large for manual classification.
This has been a major motivation for accurate, automated snowfall classification.

62 Existing approaches to automated snowfall classification from MASC images vary and 63 include the excellent work of Praz et al. (2017), our previous work (Hicks and Notaroš 2019), and an unsupervised technique (requiring no human input) from Leinonen and Berne (2020). The 64 65 multinomial logistic regression (MLR)-based method described in (Praz et al. 2017) has been demonstrated effective but requires careful definition and algorithmic extraction of several image 66 features from which classifications are made. This approach has achieved an outstanding 95% 67 classification accuracy, but may be somewhat rigid, relying on human-described features such as 68 morphological skeleton statistics, rotational symmetry, and gray-level co-occurrence. Older 69 supervised classification work in Lindvquist et al. (2012), similarly, applies principal component 70 analysis coupled with Bayesian and weighted nearest-neighbor techniques to classify ice-cloud 71 72 particles, typically achieving accuracies between 80% and 90%. We have previously presented 73 convolutional neural networks (CNNs) as a robust alternative that can easily be applied and generalized in a black-box manner without expert definition of features. Both methods, of 74 course, require manual input to generate training and test data labels. The work of Leinonen and 75 76 Berne (2020), on the other hand, automatically classifies snowflake images by exploring the latent space of generative, as opposed to predictive, models. Such unsupervised approaches are 77 extremely promising for discriminating and classifying different hydrometeor images in general, 78 79 but an unsupervised method inherently produces its own categories, rather than directly

80 assigning images to existing, known categories with which researchers are likely already81 familiar.

82 Accordingly, we offer improvements to our existing CNN-based, supervised approach 83 (Hicks and Notaroš 2019), using more data and improved training techniques to achieve higher accuracy on a more complicated dataset than we had previously demonstrated. As an 84 85 advancement of our previous proof of concept study, which used a geometric dataset focused on easily identifiable examples of each of the snowflake classes considered, a principal goal of this 86 work is to demonstrate broader usefulness of deep CNNs for automated snowfall classification 87 88 by using a larger dataset containing wider in-class variety. We present improved training methods and new, automated techniques for detection, cropping, and normalization of snowflake 89 images as well as quality and recognizability preprocessing of image data. From these 90 improvements, we demonstrate higher overall test accuracy on a vastly more challenging dataset 91 than that used in our previous work. Together, these improvements constitute an accurate, 92 efficient, and robust supervised machine learning approach to snowflake classification, using 93 deep neural networks and images collected by the MASC or another image-based particle 94 recording instrument or system. 95

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## 97 2. Data Collection and Image Processing

98 This section describes the collection of raw MASC images as well as the automated 99 cropping and normalization performed on raw images to isolate potential snowflakes present in 100 each image.

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#### 102 **2.1 Raw Image Collection**

103 The 3,458,848 raw images used to generate the training set were collected from several winter weather events between November 2014 and May 2016 using a modified MASC system. 104 105 The system was located at a surface instrumentation field site established under MASCRAD 106 (MASC + RADar) (Notaroš et al 2016; Bringi et al. 2017; Kennedy et al. 2018). This is the same 107 site and system used for data collection in Hicks and Notaroš (2019). The MASCRAD field site is located at the Easton Valley View Airport in La Salle, near Greeley, Colorado, shown in 108 109 Figure 1. The MASC system, along with other ground-level instrumentation at the site, is 110 situated within a double fence intercomparison reference (DFIR). Raw images from both winter storm events used in Hicks and Notaroš (2019) constitute a subset of the total raw image set used 111 in the present work. Details of the MASC system used are presented in Hicks and Notaroš 112 (2019). Although the MASC allows for collection of snowflake imagery from multiple angles to 113 114 help determine three-dimensional shape (Kleinkort et al. 2017), we did not make use of this feature directly for the present work. As described in Leinonen and Berne (2020), it is common 115 that a given snowflake will only be captured at usable quality by a single camera of a multi-116 117 camera system, the snowflake often out of focus or occluded in other fields of view, so limiting study to only snowflakes that appear at high quality in all fields of view substantially reduces the 118 119 number of useable examples. By limiting study to single-view cases, we were able to manuallyclassify thousands, rather than hundreds of snowflakes at a cost of increased ambiguity due to 120 lack of multi-angle data. Note that we did not explicitly remove cases where a single snowflake 121 was imaged from multiple angles when forming the dataset for the present work. 122

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#### 125 **2.2 Detection, Cropping, and Normalization**

126 As the MASC produces raw, wide field of view images, typically containing many snowflakes, it is necessary to isolate individual examples for classification. All images were 127 128 processed in grayscale (single channel). To detect possible flakes in each raw MASC image, we 129 first normalized the entire grayscale image, dividing all pixel values by the maximum brightness 130 value. An example of a normalized raw image is shown in Figure 2. We then converted the grayscale image into a binary image by application of a threshold. Pixels in the grayscale image 131 132 with brightness greater than or equal to the threshold were assigned value 1, and pixels less than 133 the threshold were assigned value 0. For the present work, this threshold was set to 0.1. We then set any pixels in the binary image with value 0 to 1 if they were within a 2-pixel radius (using 134 Chebyshev distance) of any pixel that had already been assigned value 1 in the previous 135 thresholding step. The example image from Figure 2 is shown after thresholding and application 136 137 of the 2-pixel radius in Figure 3. This radius was chosen by hand as a reasonable value. Next, we computed sets of connected components in the binary image. A connected component is any 138 group of active (value 1) pixels that form an unbroken group. If a connected component 139 140 contained fewer than 26 active pixels, it was discarded. For each connected component not discarded, we cropped a rectangular region from the original grayscale image corresponding to 141 its bounding box. Two such examples produced from Figure 3 are shown in Figure 4(a) and (d). 142 Cropped images were then contrast scaled linearly such that the top 1% of brightest pixels were 143 saturated. Figure 4(b) and (e) show cropped image examples from the previous step after contrast 144 scaling. Note that contrast scaling destroys some information theoretically available in the 145 images (by loss of absolute brightness and saturation of some pixels). However, we found that 146 brightness variations between flakes were dominated by differing lighting conditions, rather than 147

useful information like snowflake class, so contrast scaling was performed to give the network input for which pixel brightness variations are dominated by microphysical characteristics rather than lighting conditions. After scaling, any cropped image was rejected if the mean value of its pixels was greater than 0.5. We then centered each remaining cropped, scaled image on a 224x224 black background to produce final image chips. Examples are shown Figure 4(c) and (f). Cropped images that exceeded the 224x224 image chip sized were cropped to 224x224 pixels after centering. Camera configurations are

This approach to cropping and normalization was arrived at for several reasons. In 155 contrast to simply cropping a 224x224 pixel region centered on each connected component in an 156 image (or similar), we found that the above method significantly reduced the number of image 157 chips that contained multiple, physically disconnected snowflakes. In other words, during heavy 158 159 snowfall events, we found it was common for two or more snowflakes to appear within 224 pixels of each other. By cropping a tight bounding box as above, we were able to recover far 160 more closely spaced snowflakes into usable, unambiguous image chips. Rejection of cropped, 161 162 scaled images with mean pixel value greater than 0.5 rejected most crops of the sky and background that did not actually contain a snow particle. By also rejecting connected 163 components with pixel counts below 26, we avoided cases where a single bright pixel caused a 164 false detection. In general, the described cropping and normalization approach was able to detect 165 far more small particles, and dim, unrimed planar crystals than the approach used for Hicks and 166 Notaroš (2019). Application of this cropping algorithm to all raw MASC images from November 167 2014 to May 2016 produced 8,441,563 image chips. 168

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**3. Hydrometeor Classification Scheme and Training Sets** 

This section describes how the 8,441,563 224x224 pixel image chips extracted from raw 172 MASC images were automatically sorted to quality classes and how images from the best class 173 were manually sorted into the five geometric categories studied. A total of 25,199 examples were 174 manually sorted for the final geometric dataset covering 32 snowfall events, an event defined 175 176 here as a period during which no more than 24 hours passed between collection of any two image chips identifies as snowflakes during manual classification). All classification was 177 performed by a single analyst who reviewed each image at least three times. Overall, we are 178 179 confident the manual classifications used for training accurately represent the opinions of our analyst and have made this dataset available at Key et al. (2021). Note, however, that our use of 180 only one human analyst has potential to introduce more bias relative to other work for which 181 multiple humans performed analysis, such as Praz et al. (2017). We had originally planned to 182 also produce an expanded riming dataset in addition to the presented geometric dataset, but we 183 found that some riming degrees were insufficiently represented for production of a larger, 184 balanced riming dataset from our current pool of raw images. We hope to contribute such a 185 dataset in future work. 186

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## 188 **3.1 Quality and Recognizability Preprocessing**

The snowflake detection, cropping, and normalization method described in Section 2.2 remains imperfect. Therefore, many of the image chips produced contained bright points from a raw image that are not snowflakes. These included sources like glare, sensor noise, and sky/ground glow. In addition, operators of the MASC system occasionally forgot to turn off data collection while calibrating and testing the system after maintenance and redeployment. This led to captures of test probes, hands, coins, and other objects to occasionally appear in the raw imagedataset. Several examples of image chips due to non-flake objects are shown in Figure 5.

For image chips that contain snowflakes, there is an inherent range of quality. Some 196 flakes appear out of focus in raw images. Others are poorly cropped, either due to over-cropping 197 by the image processing method in Section 2.2, or because they originally appeared partially out 198 of field of view in a raw MASC image. We considered image chips containing snowflakes to fall 199 into four recognizability categories: Bad-Crop, Bad, Okay, and Good. Image chips in the Bad-200 Crop category are those where unambiguous recognizability of the imaged snowflake is made 201 202 difficult due to over-cropping by the processing method described in Section 2.2 or part of the flake appearing out of field-of-view in the raw image, leaving a substantial portion of the flake 203 absent from the image chip. Note that cases where a flake was simply too large to fit in a single 204 205 image chip were not included in the Bad-Crop category. In our manual exploration of the dataset, such flakes were almost exclusively in the AG class and easily identifiable despite cropping to 206 224x224 pixels. Rather, over-cropping by the processing described in Section 2.2 is typically due 207 208 to poor or uneven illumination of the flake causing the rectangular bounding box of the resulting connected component to not contain most of the pixels covered by the snowflake. Four examples 209 of Bad-Crop image chips are shown in the first column of Figure 6. Bad image chips are those 210 for which poor focus or poor illumination rendered the target snowflake unrecognizable. Image 211 chips containing more than one disjoint (non-aggregated) snow particle are also included in the 212 Bad category, regardless of lighting and focus. We consider two snow particles disjoint if they 213 were clearly identifiable as discrete, physically unconnected particles by our human analyst. Four 214 such examples are shown in the second column of Figure 6. Okay image chips were those that 215 216 contained a recognizable snowflake but suffered from mild blur or high background noise that

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made examination of microphysical characteristics difficult. Four examples of okay image chips
are shown in the third column of Figure 6. Good image chips were those that were free of
substantial over-cropping and clear enough to identify relevant microphysical features. Column
four of Figure 6 shows four examples of Good image chips.

To avoid wasting human time visually inspecting images that did not contain flakes or 221 were of quality too poor to use, we trained a preliminary quality and recognizability (Q&R) 222 classifier on a small, manually sorted subset of the 8,441,563 image chips. This classifier was 223 implemented by necessity to reduce the data volume needing manual inspection, and its results 224 were not further analyzed or verified in the present work. To train the Q&R classifier, we 225 collected at least 1,500 examples for each of five categories: Not-Flake, Bad-Crop, Bad, Okay, 226 and Good, with an emphasis on variety within each class. Counts per category for the Q&R 227 228 dataset are presented in Table 1 along with descriptions. When collecting example images, we included roughly equal numbers of examples from each geometric class in Okay and Good 229 categories to avoid biasing the classifier against a given geometric type. The Q&R classifier was 230 231 trained using the same methodology used for the geometric classifier in Hicks and Notaroš (2019). For training, 1,500 examples from each Q&R category were drawn randomly. The 232 trained Q&R classifier was then applied to all 8,441,563 image chips to sort each into Not-Flake 233 (3,791,326), Bad-Crop (723,550), Bad (3,062,288), Okay (582,333), and Good (282,001) 234 categories. Only image chips assigned by the Q&R network to the Good category were examined 235 to produce the geometric dataset for the present study. 236

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#### 239 **3.2 Geometric Classes**

A variety of attempts have been made to classify snowflakes (Nakaya and Sekido 1936, Magono and Lee 1966, Korolev and Sussman 2000, Grazioli et al. 2014, Vasquez-Martin et al. 2020). As in our previous work (Hicks and Notaroš 2019), we chose to use the scheme adopted by Praz et al. (2017) for training and testing of their multinomial logistic regression snowflake classifier. We summarize this scheme here.

The scheme uses the nine categories of snowflakes defined in Magono and Lee (1966), 245 with a few simplifications for data availability. Praz et al. (2017) additionally defined the 246 Aggregate and Small Particle classes. Aggregates are defined as single snowflakes that are the 247 248 result of in-air collision of two or more particles. Small Particles are snowflakes whose features are too small to categorize. Note that this is based on the subjective opinion of the analyst, rather 249 than a strictly defined size threshold. Simplifications from Magono and Lee (1966) and addition 250 of AG and SP classes resulted in 10 individual categories, of which only six were used in Praz et 251 al. (2017) due to data availability: Aggregates (AG), Small Particles (SP), Columnar Crystals 252 (CC), Planar Crystals (PC), Combination of Columnar and Planar Crystals (CPC), and Graupel 253 (GR). As in Hicks and Notaroš (2019), we chose to exclude the CPC class from the present study 254 due to data availability. We found only a few hundred clear examples of CPC in the Good Q&R 255 class. CPC appeared far less commonly than the next rarest class, GR, which had several 256 thousand Good Q&R examples. Image chips that fell into unconsidered categories, like CPC, we 257 simply omitted from consideration for the present work. 258

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## **3.3 Building the Geometric Dataset**

Our goal in collecting the geometric dataset for the present work was to establish a large, 262 highly varied collection of image chips in each of the five categories considered. Deep neural 263 networks, like that used in Hicks and Notaroš (2019) and the present work can achieve high 264 accuracies but require substantial training data to avoid over-fitting (Simonyan and Zisserman 265 2015, Szegedy et al. 2015). With tens of millions of parameters, deep CNNs like the ResNet-50 266 267 architecture (He et al. 2016) can store substantial quantities of information to learn highly complicated associations and trends (Zeiler and Fergus 2014). Care must therefore be taken to 268 train such networks on large enough datasets that they cannot simply memorize associations 269 270 between specific images and their labels or extract spurious trends.

Another important consideration is balance between classes during training. Unless special precautions such as class-specific learning rates are used (not used in the present study), training a neural network on a dataset biased toward a particular class will often bias the network toward that class. As an extreme example, consider a network trained on a dataset of 900 GR images and 100 PC images; the network can attain 90% accuracy on the training set simply by learning to label every image as GR. It is therefore important to present the network with roughly equal numbers of examples in each class during training.

To account for these factors, we limited the number of examples in our geometric dataset for each class to the maximum number of Good Q&R examples we could find for the rarest class considered. After CPC (not considered), GR was the rarest class, for which we could only find roughly 5,000 examples. Accordingly, we collected roughly 5,000 examples of each of the other classes considered, for a total of 25,199 examples. Exact image chip counts per class are presented in Table 2. Figures 7 through 11 show representative examples from the final AG, CC,

284 GR, PC, and SP sets, respectively. When collecting examples for each class, we put emphasis not only on archetypical examples, but also examples we considered good counterexamples to 285 possible oversimplifications of each class: e.g. AGs are always large, PCs always have six-fold 286 symmetry, or GR always has a smooth outline. Image chips were not included in the geometric 287 dataset if we could not determine an appropriate label based on information present in the image 288 chip alone, i.e. no multi-angle information was used during manual sorting. We note overall that 289 there is an inherent subjectivity in identification of snowflakes in single-view images, especially 290 for classes like GR (Figure 9), for which distinguishing from other heavily-rimed particles is 291 292 subjective, and SP (Figure 11), for which deciding unrecognizability of features due to small size is highly subjective. We did not avoid using backlit examples where available, although these 293 were rare, only occurring where a snow particle was imaged while falling in front of a 294 sufficiently bright glare point in the background. Due to their rarity, inclusion of backlit cases 295 likely did not have a substantial impact on accuracy of the trained network. Our analyst 296 recollects seeing at most a dozen backlit cases during manual classification, but such cases were 297 assigned no special designation or identifying information that would make quantification of 298 their impact possible without another manual review of the dataset. 299

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## **4. Convolutional Neural Networks Methodology**

A brief discussion of the network architecture is presented in this section. We also present a summary of the training method and hyperparameters used. Note that, although the network architecture remains the same as that in our previous work (Hicks and Notaroš 2019), hyperparameters for training differ.

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#### 4.1 Neural Network Architecture

308 We used an identical ResNet-50 architecture to that in Hicks and Notaroš (2019). The ResNet-50 architecture has been demonstrated as an excellent balance between speed and 309 310 accuracy for image classification tasks and is described in detail in (He et al. 2016). The residual 311 approach, in general, was groundbreaking at the time of its publication, as it presented an elegant 312 solution to the vanishing gradient problem that had previously limited scaling of CNN accuracy with increased depth. The use of residual connections (or similar), as described in (He et al. 313 314 2016) has since been widely adopted by deep learning researchers and practitioners. As in (Hicks 315 and Notaroš 2019), we used a ResNet-50 model that had been pretrained for general image classification on the ImageNet database (Russakovsky and Deng et al. 2015). We also 316 experimented with randomly initialized (no pretraining) versions of the same architecture but 317 found no substantial benefit. We therefore chose to only focus on the pretrained model for the 318 319 present work for easy comparison with (Hicks and Notaroš 2019). A necessary change made to the architecture was reduction in the number of outputs of the final, fully connected layer for our 320 substantially lower number of classes (the original ResNet-50 architecture trained on ImageNet 321 322 had 1,000 classes, not five). Weights in the modified fully connected layer were initialized randomly. 323

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#### **4.2 Training Method and Hyperparameters**

As in (Hicks and Notaroš 2019), network performance was determined by cross-entropy error, and network weights and biases were optimized by stochastic gradient descent to minimize this loss function. For training, validation, and testing, we again limited the number of examples used in each class to the number of examples available in the smallest class (in the present work, 330 GR with a total of 5,000 hand-classified image chips available). The examples used from classes 331 with raw counts larger than the minimum were drawn randomly. We again used a mini-batch size of 10. Beyond this, we made several changes to the hyperparameters and training method 332 333 used in (Hicks and Notaroš 2019). Our dataset was also substantially larger; the testing set alone, in this case, was comparable in size to the entire geometric dataset used for (Hicks and Notaroš 334 2019), roughly 1,450 examples. In the present study, we randomly selected 500 examples from 335 each class for a total of 2,500 testing examples. The remaining 22699 examples were randomly 336 partitioned into a training set ( $\sim 90\%$ ) and a validation set ( $\sim 10\%$ ), both evenly distributed among 337 338 the classes studied. The random partitioning between training and validation was unique to each training run. Only the training and validation sets were used for hyperparameter tuning, which 339 was performed by a mix of expert hand-tuning and small parametric sweeps and included tuning 340 of the mini-batch size, learning rate, and number of training epochs. We also trained for 341 substantially longer than our previous work, training for a total of 20 epochs, as opposed to 10. 342 The training set was shuffled (re-ordered) randomly every epoch. An epoch is defined as one 343 complete pass through the training set, so, the present training dataset containing many more 344 examples than that available in (Hicks and Notaroš 2019), this corresponds to roughly a 30-fold 345 346 increase in training time. We were able to extend the training time substantially due to prevention of overfitting by the larger training dataset used in the present work. As opposed to 347 the constant learning rate of 0.0003 used in (Hicks and Notaroš 2019), we began with a learning 348 rate of 0.001 which was then scaled by a factor of  $1/\sqrt{10}$  every five epochs. We found this led to 349 a small but noticeable improvement in final network accuracy. We expect improvements in 350 351 network accuracy could be further improved with additional hyperparameter tuning using more compute resources for large parametric sweeps. 352

### 354 **5. Results and Discussion**

This section presents and discusses the performance of the trained classification networks 355 on the test dataset. The final mean test accuracy achieved was 96.23% with a standard deviation 356 of 0.29% across 10 training runs, the individual test accuracies of which are presented in Table 3. 357 Only the order in which images were presented to the network and random partitioning of non-358 test images between training and validation differed between training runs. We expect we could 359 have achieved even higher accuracy if we had limited our dataset to only archetypal examples, 360 but this would have diminished the usefulness of the dataset and resulting trained model for 361 general snowfall classification tasks. 362

Figure 12 shows accuracy and loss of a typical trained network (test accuracy close to the 363 mean) on the training and validation set with respect to training iteration (and epoch, indicated 364 by alternating vertical bands) for a typical training run. There is no evidence of overfitting, and 365 366 validation accuracy increased nearly monotonically with iteration count. Overfitting, if present, would be apparent in Figure 12 as divergence of the black validation accuracy and blue training 367 accuracy curves. For the training run shown, the network achieved a validation accuracy of 368 96.1% and a test accuracy of 96.2%. We suspect the much larger size of the geometric dataset is 369 the dominant factor in improving performance over our previous work but did not have sufficient 370 compute time to perform a full parametric sweep to confirm this. We found that network 371 performance on the validation and training sets were comparable, indicating that training, testing, 372 and validation datasets all sampled the underlying distribution of snowflake geometries well. The 373 validation accuracy standard deviation for the 10 example runs shown in Table 3 was 0.42%, and 374 their mean validation accuracy was 96.26%. We attribute the larger validation accuracy standard 375

deviation, as compared to the test accuracy standard deviation, to random selection of the validation set for each training run (the test set did not change between runs). There was little variation between training runs, with the only nominal differences due to this random partitioning of the validation and training sets as well as random re-ordering of the training set during each epoch. Figure 13 shows a confusion matrix for the same network, the training progress of which is shown in Figure 12.

In general, trained networks would confuse PC and AG classes most often. We included 382 many difficult examples in the AG class that featured a prominent planar crystal with several 383 384 less-prominent particles that had adhered due to mid-air collisions, so confusion between the two classes seems understandable to us. Figure 14 presents examples of image chips misclassified by 385 the typical network from Figures 12 and 13. Overall, most misclassifications appear to be blatant 386 errors due to imperfection of the trained model, but several stand out as ambiguous cases or 387 possibly even human error. Figure 14, row 2, column 2, for instance, was assigned by the 388 network to the AG class, having been human labeled as a columnar crystal. Further inspection 389 390 indicates this snowflake may indeed be a simple aggregate or even a malformed planar crystal, suggesting this misclassification is due human error rather than network error. Figure 14, row 4, 391 column 3 shows a clear planar crystal adhered to a small aggregate of columnar crystals. 392 Although the planar crystal dominates the image chip, the aggregation present indicates the 393 network is correct to assign this image chip to the AG class. Figure 14, row 3, column 4 and row 394 5, column 2, respectively show a GR image chip misclassified as SP and a SP image chip 395 misclassified as GR, respectively. These two cases show the ambiguity of the SP class and the 396 difficulty of drawing a distinction between small GR flakes and relatively large, round SP flakes. 397 398 Figure 14, row 5, column 3 shows another ambiguous case. Human-classified as SP but network

- classified as CC, this particle shows possible CC-like features (dominant uniaxial crystal growth)but is barely too small for our analyst to assign confidently to the CC category.
- 401

## 402 6. Conclusions

This paper has presented improvements over our previous approach (Hicks and Notaroš 403 2019) to automated winter hydrometeor classification using deep convolutional neural networks. 404 Using improved training methods and a substantially larger and more complicated dataset from 405 many more snow events than in our previous study, we were able to achieve over 96.2% 406 407 accuracy on a test set of 2,500 images. We consider this result substantial for several reasons. The MASC is a high-throughput sensor, collecting tens to hundreds of thousands of detectable 408 snowflake images during a winter storm event, so even small accuracy improvements lead to a 409 410 substantial reduction in the total number of misclassified snowflake images. Namely, this is a  $\sim$ 40% reduction in the fraction of incorrectly classified snowflakes relative to the already very 411 412 high geometric classification accuracy result reported in our previous work and corresponds to a 2.8% increase in overall accuracy. Even more importantly, the dataset of 25,199 image chips 413 sorted by geometric class used in the present study differs substantially from that developed for 414 (Hicks and Notaroš 2019). As a proof of concept study, (Hicks and Notaroš 2019) used a 415 geometric dataset focused on easily identifiable examples of each of the snowflake classes 416 considered. To demonstrate the broader usefulness of deep CNNs for automated snowfall 417 418 classification, the dataset used in the present study is not only larger but also contains wider inclass variety. In using such a dataset, we have shown that, with a few modifications to the 419 network training process, the geometric classification method described in (Hicks and Notaroš 420 421 2019) can achieve higher accuracy on a vastly more challenging dataset. Finally, the paper has

422	presented several important components of the CNN-based, supervised approach to snowflake
423	classification, including an improved training method and hyperparameters for training; new
424	automated techniques for snowflake detection, cropping, and normalization of snowflake images;
425	and new quality and recognizability preprocessing of image data. The described methodologies
426	and techniques may be of great use to researchers and practitioners applying the same or similar
427	approaches to hydrometeor classification based on the images collected by the MASC or another
428	image-based particle recording instrument or system.
429	
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432	1344862 and AGS-2029806.
433	
434	Data Availability Statement
435	The dataset of MASC images generated for and used in this study has been made publicly
436	available at Key et al. (2021).
437	
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# Tables

528	Table 1. Category names, counts, and descriptions for the quality and recognizability dataset, a
529	balanced subset of which was used to train a presorting network using the methods of Hicks and
530	Notaroš (2019).

Category Name	Count	Description
Not-Flakes	7,020	Object other than a snowflake present in the image. Examples include sensor noise, glare, sky/ground glow, and calibration probes.
Bad-Crop	1,500	Likely snowflake present, but poor cropping leaves a substantial portion of the snowflake out of the image chip, interfering with geometric classification.
Bad	1,977	Likely snowflake present, but poor lighting or focus prevent identification. Image chips containing more than one disjoint (non-aggregated) snowflake are also assigned to this class, regardless of image quality.
Okay	2,796	Focus and lighting are good enough to identify coarse flake features, and likely geometric class, but are insufficient to capture microphysical characteristics.
Good	1,500	Lighting and focus are good enough to resolve microphysical characteristics and determine snowflake geometric class.

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**Table 2.** Number of examples in each class for the geometric dataset.

Class Name	Count
AG	5,038
CC	5,021
GR	5,000
PC	5,014
SP	5,126

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Table 3. Test accuracy results of 10 independent training runs. Note that training runs 5 and 6
producing test accuracies identical to two decimal places occurred by chance and was verified
not to be a mistake.

Run	Test Accuracy
1	96.56%
2	96.04%
3	96.24%
4	95.88%
5	96.00%
6	96.00%
7	96.20%
8	96.08%
9	96.68%
10	96.64%

540	Figure Caption List				
541					
542	Figure 1. MASCRAD Snow Field Site at Easton Valley Airport, near Greeley, Colorado, under				
543	the umbrella of CSU-CHILL Radar. MASC (top right), along with other surface instrumentation,				
544	is contained in the 2/3-scaled DFIR.				
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546	Figure 2. Example normalized raw MASC image. Several snowflakes can be seen in addition to				
547	background glare (center left) and subtle ground and sky glow (top and bottom). Note: ground				
548	and sky glow may not be visible in all prints or computer monitor settings.				
549					
550	<b>Figure 3</b> Example binary image produced by application of a brightness threshold and 5-pixel				
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551	radius to the normalized raw image in Figure 2. Possible snowflake silhouettes are now apparent.				
552	Background glare (center left) was rejected due to exceeding the mean brightness threshold				
553	Dimmer glare cases are reliably assigned to the Not-Flakes Q&R class.				
554					
555	Figure 4. Example crops and image chips extracted from the MASC image shown in Figures 2				
556	and 3. (a) Cropped image of a planar crystal. (b) Example crop from (a) after contrast scaling. (c)				
557	Final image chip produced from contrast scaled crop in (b). (d) Cropped image of an aggregate.				
558	(e) Example crop from (d) after contrast scaling. (f) Final image chip produced from contrast				
559	scaled crop in (e).				
560	Figure 5. Examples of image chips in the Not-Flakes quality and recognizability category. A				
561	description of this category is given in Table 1. First row (left to right): a coin; background glare;				

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562	sky glow seen between fence posts; a finger. Second row: a sensor probe; an out of focus sensor					
563	probe; part of a pair of calipers; a string. Third row: a metal ball; part of a mitten; background					
564	glare; amplified sensor noise. Fourth row: background glare; sky glow seen above fence posts;					
565	background glare; background glare.					
566						
567	Figure 6. Examples of Bad-Crop (first column), Bad (second column), Okay (third column), and					
568	Good (fourth column) image chips. Category descriptions given in Table 1.					
569						
570	<b>Figure 7</b> Examples of image chips in the aggregate $(AG)$ class of the final geometric dataset					
570	Figure 7. Examples of mage emps in the aggregate (AG) class of the final geometric dataset.					
571	All image chips in the final geometric dataset had been automatically categorized into the Good					
572	Q&R category. We placed emphasis on collecting a wide variety of sizes and forms of aggregate					
	with varying types of constituent particles.					
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**Figure 10.** Examples of image chips in the planar crystal (PC) class of the final geometric dataset. All image chips in the final geometric dataset had been automatically categorized into the Good Q&R category. We included difficult examples like row 1 column 2 where possible to help differentiate such PC cases from CC examples.

588

**Figure 11.** Examples of image chips in the small particle (SP) class of the final geometric dataset. All image chips in the final geometric dataset had been automatically categorized into the Good Q&R category. As small particles are, by definition, particles with features too small to classify, there is little interesting variety among the collected examples other than various shapes and degrees of riming.

594

Figure 12. Training progress for an example training run using the methods and hyperparameters
described in Section 4.2

597

Figure 13. Confusion matrix for the network trained in Figure 12 applied to the test set. A finalaccuracy of 96.2% was achieved. AG and PC were the most confused classes.

600

Figure 14. Examples of image chips misclassified by a trained network. Misclassified aggregates (first row), misclassified columnar crystals (second row), misclassified graupel (third row), misclassified planar crystals (fourth row), and misclassified small particles (fifth row) are shown with the label assigned by the network overlaid for each image chip.

# Figures

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607

**Figure 1.** MASCRAD Snow Field Site at Easton Valley Airport, near Greeley, Colorado, under

- the umbrella of CSU-CHILL Radar. MASC (top right), along with other surface instrumentation,
- 610 is contained in the 2/3-scaled DFIR.

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Figure 2. Example normalized raw MASC image. Several snowflakes can be seen in addition to background glare (center left) and subtle ground and sky glow (top and bottom). Note: ground and sky glow may not be visible in all prints or computer monitor settings.



Figure 3. Example binary image produced by application of a brightness threshold and 5-pixel
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622



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- Figure 5. Examples of image chips in the Not-Flakes quality and recognizability category. A 632
- description of this category is given in Table 1. First row (left to right): a coin; background glare; 633 sky glow seen between fence posts; a finger. Second row: a sensor probe; an out of focus sensor 634
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**Figure 6.** Examples of Bad-Crop (first column), Bad (second column), Okay (third column), and

641

<sup>639</sup> Good (fourth column) image chips. Category descriptions given in Table 1.



Figure 7. Examples of image chips in the aggregate (AG) class of the final geometric dataset.
All image chips in the final geometric dataset had been automatically categorized into the Good
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with varying types of constituent particles.



**Figure 8.** Examples of image chips in the columnar crystal (CC) class of the final geometric dataset. All image chips in the final geometric dataset had been automatically categorized into the Good Q&R category. We included a variety of sizes, forms, and degrees of riming. An example of a backlit snowflake is shown in row 2, column 2. Such cases were rare but were included whenever backlighting did not interfere with recognizability.



Figure 9. Examples of image chips in the graupel (GR) class of the final geometric dataset. All
image chips in the final geometric dataset had been automatically categorized into the Good
Q&R category. We included a variety of textures and sizes and also included melting examples
when available.



**Figure 10.** Examples of image chips in the planar crystal (PC) class of the final geometric dataset. All image chips in the final geometric dataset had been automatically categorized into the Good Q&R category. We included difficult examples like row 1 column 2 where possible to help differentiate such PC cases from CC examples. Emphasis was also placed on including examples that lacked easily identifiable six-fold symmetry.



**Figure 11.** Examples of image chips in the small particle (SP) class of the final geometric dataset. All image chips in the final geometric dataset had been automatically categorized into the Good Q&R category. As small particles are, by definition, particles with features too small to classify, there is little interesting variety among the collected examples other than various shapes and degrees of riming.





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Confusion Matrix						
AG	<b>471</b>	<b>2</b>	<b>1</b>	<b>14</b>	<b>1</b>	96.3%
	18.8%	0.1%	0.0%	0.6%	0.0%	3.7%
сс	<b>5</b>	<b>482</b>	<b>0</b>	<b>4</b>	<b>8</b>	96.6%
	0.2%	19.3%	0.0%	0.2%	0.3%	3.4%
GR GR	<b>3</b>	<b>0</b>	<b>491</b>	<b>1</b>	<b>1</b>	99.0%
	0.1%	0.0%	19.6%	0.0%	0.0%	1.0%
Output	<b>20</b>	<b>3</b>	<b>5</b>	<b>478</b>	<b>8</b>	93.0%
<sub>Dd</sub>	0.8%	0.1%	0.2%	19.1%	0.3%	7.0%
SP	<b>1</b>	<b>13</b>	<b>3</b>	<b>3</b>	<b>482</b>	96.0%
	0.0%	0.5%	0.1%	0.1%	19.3%	4.0%
	94.2%	96.4%	98.2%	95.6%	96.4%	96.2%
	5.8%	3.6%	1.8%	4.4%	3.6%	3.8%
	P.S.	c <sub>C</sub>	F	<i>و</i> ن	જ	
Target Class						

**Figure 13.** Confusion matrix for the network trained in Figure 12 applied to the test set. Each red or green cell corresponds to a target class (horizontal) and output class (vertical). Row 2, column 1, for instance, shows that 5 image chips in the test set with target class AG were assigned to the CC class by the trained network, and this corresponded to 0.2% of the entire dataset. The first five cells of the bottom row show accuracy (green) and error (red) for each target class. Row 6, column 1, for instance, shows that, of image chips in the test set with target class AG, 94.2% were classified correctly by the network while 5.8% were classified incorrectly. The first five

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cells of the rightmost column similarly show accuracy and error for each output class. Row 1, column 6, for instance, shows that, of image chips assigned by the network to the AG class, 96.3% were classified correctly while 3.7% were classified incorrectly. An overall network accuracy (all classes) of 96.2% is shown in the bottom right cell. AG and PC were the most confused classes.

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Figure 14. Examples of image chips misclassified by a trained network. Misclassified aggregates
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- 694 misclassified planar crystals (fourth row), and misclassified small particles (fifth row) are shown
- 695 with the label assigned by the network overlaid for each image chip.