

# Flyball governor differential equation solution

## Constants:

$$a := 1 \quad k := 500 \quad m := 0.5 \quad g := 32.2 \quad \omega := 10$$

## Equation of motion:

$$a \cdot \frac{d^2}{dt^2} \theta(t) + a \cdot \omega^2 \cdot \sin(\theta(t)) \cdot \cos(\theta(t)) - \frac{2 \cdot a \cdot k}{m} \cdot (1 - \sin(\theta(t))) \cdot \cos(\theta(t)) + g \cdot \cos(\theta(t)) = 0$$

## Equilibrium condition:

$$\theta_e := \text{asin} \left( \frac{2 \cdot a \cdot k - m \cdot g}{m \cdot a \cdot \omega^2 + 2 \cdot a \cdot k} \right) \quad \theta_e = 69.562 \text{ deg}$$

## Initial conditions:

$$\theta_0 := 75 \cdot \text{deg} \quad d\theta dt_0 := 0$$

## Solution of the equation of motion:

$$\Delta T := 9$$

Given

$$a \cdot \frac{d^2}{dt^2} \theta(t) + a \cdot \omega^2 \cdot \sin(\theta(t)) \cdot \cos(\theta(t)) - \frac{2 \cdot a \cdot k}{m} \cdot (1 - \sin(\theta(t))) \cdot \cos(\theta(t)) + g \cdot \cos(\theta(t)) = 0$$

$$\theta(0) = \theta_0$$

$$\theta'(0) = d\theta dt_0$$

$$\theta := \text{Odesolve}(t, \Delta T)$$

$$\theta(\Delta T) = 69.523 \text{ deg}$$

